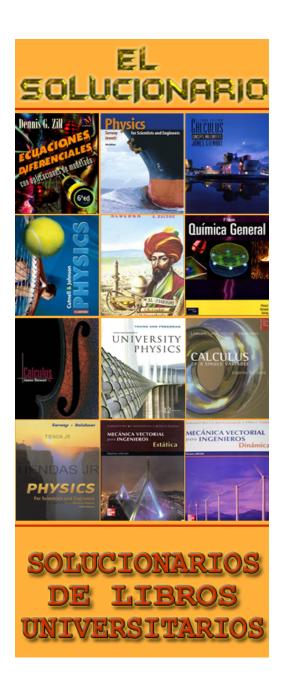


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VISITANOS PARA DESARGALOS GRATIS. Instructor's Manual to accompany

Applied Strength of Materials

Fifth Edition

Robert L. Mott



Upper Saddle River, New Jersey Columbus, Ohio

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APPLIED STRENGTH OF MATERIALS 5TH Ed. by Robert L. Mott

Options for Course Organization

INTRODUCTION

Course organization is one of the most important responsibilities for an instructor. Knowledge of the specific objectives of the program or programs of which the course is a part is critical, particularly with regard to the prerequisite knowledge and skills students are expected to have when they begin the course and the outcomes expected as they relate to career paths of the students and abilities required for successful completion of following courses.

With these overarching considerations in mind, this document attempts to provide options for how to structure a course in Strength of Materials using this textbook. Variables considered include specific prerequisites for mathematics, statics, centroids and moments of inertia, physics mechanics, and materials science. Comments are then presented about each of the 13 chapters of the book.

Users of previous editions of this book will notice significant changes in the arrangement of topic coverage in this edition, in response to feedback from colleagues and users, both instructors and students.

algebra and trigonometry. Additional skills in calculus are beneficial but not necessary.

Comprehension of virtually all topics in the book and completion of almost all problems for student solution require only algebra and trigonometry. The principles of strength of materials in each chapter are developed first with logical observations of the behavior of materials when subjected to particular forces, moments, and torques with specific support conditions. Typically, those observations are presented in the introduction to each chapter in the form of *The Big Picture* in which students are asked to observe structures and various devices with which they are familiar and to engage in simple activities from which they can discover underlying principles. Then the primary formulas governing the mathematical representation of those behaviors are stated along with the definition of variables and statements of limitations on the use of the formulas. For most concepts, a separate section is included that presents a more complete development of the formulas, often using differential and integral calculus. This is beneficial for students who have completed such mathematics courses and

- for instructors who prefer this approach. However, it is not essential to include coverage of these sections and they are marked [Optional] in the following chapter overviews.
- Statics: It is considered essential that students have fundamental understanding of forces,
 moments, vectors, and static equilibrium to learn adequately the principles of strength of
 materials and the problem solution techniques presented in this book. An extensive review of
 the principles of Statics is included in Appendix A-27 for students needing reinforcement.
 Also, the study of Physics Mechanics is beneficial and is typically included as a prerequisite
 to Statics.
- Centroids and Moments of Inertia of Areas: Many courses in Statics include these topics.
 However, there is some advantage in delaying this coverage until these concepts are needed for application to beam analysis within the study of strength of materials. This provides just-in-time coverage that flows naturally as presented in Chapters 5, 6, and 7 in this book. When a particular course requires prerequisite knowledge of Centroids and Moments of Inertia of Areas, Chapter 6 can be skipped. Having the material in the book should be useful for students to review as needed.
- Materials Science: It is recommended that students have good knowledge and abilities related to the structure and behavior of materials commonly used for structural and mechanical applications. A prerequisite course in materials science is recommended. However, it is practical for students to succeed in the use of this book with only the knowledge of the principles presented in Chapter 2 Design Properties of Materials. For those with good prerequisite knowledge, this chapter can be quickly reviewed with emphasis on properties of materials that will be needed in solution of problems in this book and a discussion of the extensive tables of such properties presented in Appendixes A-14 through A-20. Covered there are common metals, wood, and plastics. In addition, Section 2-12 on Composites and Section 2-13 on Materials Selection likely include useful information that may not have been included in other courses. Users of previous editions of this book report that the set of materials properties data in the Appendix and the coverage of composites are better than most other books in strength of materials. This provides a wider variety of materials to apply to problems and a better understanding of the differences among types of materials and their response to heat treatment or other processing variables.

POSSIBLE COURSE ORGANIZATIONS

The order of presentation of topics in this book is, in the opinion of the author, logical and would lead to a rather linear progression through the chapters in the order given. The primary options for course organization involve consideration of which topics are essential to the objectives of the specific course. Options are presented here in a chapter-by-chapter basis.

Chapter 1 – Basic Concepts of Strength of Materials

- Sections 1-1 through 1-12 should be covered completely in order to present a foundation for the study of later chapters, to present basic expectations for student performance, and to give students an overview of many of the Appendix tables related to the properties of areas and standard shapes used for structural and mechanical applications. [See Appendixes A-1 through A-13.]
- Sections 1-6 through 1-11 give the basic concepts of stress and strain for direct tension, direct compression, and direct shear.
- The emphasis is on analysis and the understanding of the ability of materials to resist
 external forces applied to them. This is necessary for progression into Chapter 2 on Design
 Properties of Materials where some additional material properties are discussed. These basic
 concepts are expanded upon in Chapter 3.
- Mention should also be made of Appendix A-26 Conversion Factors and Appendix A-27
 Review of the Fundamentals of Statics.
- Coverage of Section 1-13 Experimental and Computational Stress Analysis is optional and may depend on the connection of this course with companion laboratory courses.

Chapter 2 - Design Properties of Materials

Refer to the discussion of **Materials Science** given above in regard to prerequisite study. Most students will benefit from at least a quick review of all parts of this chapter and the related Appendixes. Those without prerequisite knowledge of materials will need more intensive study. Some considerations for coverage are discussed next.

- Students in mechanical, manufacturing, civil and construction programs all require sound knowledge of metals and plastics.
- Most would also benefit from coverage of wood, concrete, and composites.
- Section 2-12 [Optional] on Composites may be delayed until Chapter 7 is covered and linked with Section 7-12 on the design of beams to be made from composite materials.
- The section on Materials Selection gives approaches to relating the expected performance of a structure or product to the behavior of appropriate materials. The method featured here leads to consideration of a wide variety of materials and refers to other references giving more extensive treatment of the materials selection processes. Of particular note is the reference for Dr. Michael Ashby's book, *Materials Selection in Mechanical Design*.

Chapter 3 – Direct Stress, Deformation, and Design

This chapter builds on the basic introductory treatment of direct stresses from Chapter 1 and adds significant competencies in design of load-carrying members. Design stresses are defined and related to the yield strength or ultimate strength of the materials and to the manner of loading; steady, repeated, and impact or shock. Coverage can be grouped as follows:

The Big Picture, Activity, and Chapter Objectives

- Sections 3-2 through 3-6: Design of members under direct normal stresses, including the definition of design stress, design factor (factor of safety), and design approaches.
- Sections 3-7 through 3-11: Deformation, thermal stresses, members made from more than one material, and stress concentration factors for direct axial stresses
- Sections 3-12 and 3-13 on bearing stress, including design bearing stresses
- Section 3-14 Design Shear Stress

Users of previous editions of this book will note that, in response to feedback from colleagues and external reviewers, a significant re-ordering of topics has been done in this new 5th edition. For example, Bearing Stresses were formerly presented in Chapter 1 and deformations and related topics were covered in a separate chapter. It was recommended that both stress and strain (with deformations) be included in one chapter for each type of stress.

Chapter 4 – Torsional Shear Stress and Torsional Deformation

Coverage of this chapter can be groups as follows:

- Big Picture, Activity, and Objectives
- Section 4-2 on Torque, Power, and Rotational Speed: These topics should be review for most students but it has been found that careful study is required before applying them to stress analysis.
- Section 4-3 presents the fundamental torsional shear stress formula and demonstrates its application to the analysis of stresses.
- Sections 4-4 and 4-5 [Optional] use calculus to derive the torsional shear stress formula and the equations for polar moment for solid circular bars.
- Section 4-6 extends the coverage to hollow circular sections. While some calculus is used to develop equations for polar moment of inertia, the final equations are all that is required for problem solving.
- Section 4-7 presents an approach to design of circular members under torsion, extending the design stress concepts from Chapter 3 to include torsional shear strength of materials.
- Section 4-8: This section provides interesting and useful comparison of the behavior of hollow circular sections and emphasizes their efficiency as compared with solid sections.
- Section 4-9: The study of stress concentrations in torsionally loaded members is essential to proper design and analysis of shafts.
- Section 4-10: The twisting of circular bars is discussed with the application of the equation for torsional deformation.
- Section 4-11 [Optional] Torsion in noncircular sections is less frequently encountered in practice. However, it is important for students to understand that such shapes behave quite differently from circular sections.

Chapters 5 through 9: All these chapters deal with beams; members carrying loads perpendicular to their axes. Students should be advised to scan all five chapters to see the progression of topics and to observe how each chapter relates to the others.

Chapter 5 – Shearing Forces and Bending Moments in Beams

- The Big Picture, Activity, and Sections 5-1 through 5-9 are essential. On rare occasions, some programs include some of these topics in the Statics course.
- Section 5-10 [Optional] Free-Body Diagrams of Parts of Structures: Mastery of this topic
 gives students a better fundamental understanding of the behavior of load carrying members
 by visualizing the internal forces, moments, and stresses created by various external loads.
- Section 5-11 [Optional] Mathematical Analysis of Beam Diagrams: Here students apply
 calculus to derive equations for shearing force and bending moments from given beam
 loading and support conditions. This skill is required for later study of Section 9-7 Successive
 Integration Method for deflection of beams, which is, itself, optional.
- Section 5-12 [Optional] Continuous Beams Theorem of Three Moments: Students should, at least, understand that the behavior of beams with three or more supports is quite different from those with only two simple supports as covered in other sections of this chapter.
 Extensive study of this topic, however, would be most beneficial for the civil and construction fields where such beams are frequently applied in bridges and buildings.
- Note: This is one place where the Beam Calculator program supplied with this book can be used effectively for analyzing complex loading patterns after students have mastered the manual process of creating shearing force and bending moment diagrams. The 'Shear' and 'Moment' selections produce complete diagrams immediately after the beam loading and support conditions are defined.

Chapter 6 - Centroids and Moments of Inertia of Areas

This entire chapter may be skipped for those programs in which the coverage of this topic is included in a prerequisite course in Statics. However, review of the procedures for computing the location of centroids and the computation of moments of inertia of areas is typically required. This can be done by moving directly to Sections 6-5, 6-6, and 6-8 where sections commonly encountered in strength of materials are considered, especially those including standard structural shapes such as W-beams, channels, and angles.

For those programs that do not include this topic in prior courses, coverage of Sections 6-1 through 6-6 and 6-8 should be covered as a minimum. These skills are essential to the understanding of concepts in Chapters 7 – 11. Coverage of the other sections of this chapter are optional as discussed next.

Section 6-7 [Optional] uses calculus to derive the moment of inertia of an area, I.

- Section 6-9 [Optional] provides a useful method of analyzing shapes with all rectangular parts. The process can be implemented effectively in a spreadsheet.
- Section 6-10 [Optional] Radius of Gyration is an important property of an area and is most directly applicable to Chapter 11 on Columns. It may be desirable to delay the coverage of this topic to combine it with the study of columns.
- Section 6-11 [Optional] Section Modulus is an important property of an area and is most directly applicable to Chapter 7 on Stress Due to Bending. It may be desirable to delay the coverage of this topic to combine it with the study of beams.

Chapter 7 - Stress Due to Bending

- Sections 7-1 through 7-4 present the foundation material for the analysis of beams.
- Section 7-5 [Optional] uses calculus to derive the flexure formula. It can be skipped or discussed lightly for those programs where detailed use of the calculus is not expected.
- Sections 7-6 through 7-8 cover the transitions from analysis to design of beams.
- Section 7-9 covers stress concentrations in bending situations.
- Section 7-10 is critical, at least from the standpoint that students must understand that the
 flexure formula applies only to symmetrical sections or when the load path passes through
 the flexural center (shear center) of the section. Otherwise twisting combines with the
 bending stress, reducing the capacity of the beam.
- Section 7-11 on Preferred Shapes for Beam Cross Sections is designed to help the novice student understand better why certain shapes are preferred for beams.
- Section 7-12 [Optional] on beams made from composites presents mostly conceptual
 information about the advantages of composites in bending cases and how the shape can be
 optimized to make best use of the special properties of composites. This section refers back
 to Section 2-12 and it may be desirable to cover those two sections together at this point.
- Note: This is one place where the Beam Calculator program supplied with this book can be used effectively for analyzing bending stress produced by complex loading patterns after students have mastered the manual process making such calculations on more simple beams. The 'Stress' selection produces the complete diagram of bending stress distribution immediately after the beam loading and support conditions are defined. Students should compare this result with the bending moment diagram.

Chapter 8 – Shearing Stresses in Beams

- Sections 8-1 through 8-4 present the fundamental concepts and the general shear formula.
- Section 8-5 [Optional] uses calculus to derive the general shear formula. It can be skipped or discussed lightly for those programs where detailed use of the calculus is not expected.
- Section 8-6 shows the special shear formulas applicable to rectangular, circular, hollow, and thin-webbed sections (e.g. W-beams). These formulas are frequently used.
- Section 8-7 transitions the coverage of shear in beams from analysis to design.

 Section 8-8 on shear flow [Optional] is applicable to beam sections made from component shapes that are fastened, glued, or otherwise assembled where connections are subjected to shear.

Chapter 9 - Deflection of Beams

There appears to be a wide divergence of opinion about what types of beam deflection approaches to cover in a basic course in strength of materials. This book attempts to show all popular approaches and let individual instructors and program faculty members decide which is best for their programs.

Note: This is the place where the Beam Calculator program supplied with this book is most applicable. The complete deflection curve is produced immediately after the beam loading and support conditions are defined by selecting the 'Deflection' button. Comparison of the Deflection curve with the Shear, Moment, and Stress diagrams is advised.

That said, here are some factors to consider in course planning:

- Sections 9-1 through 9-4 present the basic concepts and the widely used formulas for beam deflection, using the extensive list of formulas from Appendixes A-23, A-24, and A-25.
- Section 9-5 gives students some experience in comparing the performance of several ways
 of supporting a given load with regard to the stresses and deflections that result. This should
 help the novice student gain a better 'feel' for what approaches are preferred in different
 applications.
- Section 9-6 extends the material in Section 9-4 to the permit use of beam deflection formulas to a much broader array of applications.
- Section 9-7 on the Successive Integration Method [Optional] provides a more analytical approach to deflection analysis. It requires the use of differential and integral calculus and should be combined with Section 5-11 Mathematical Analysis of Beam Diagrams. Mastery of these concepts would be expected for students who intend to continue their study of applied mechanics in later courses or graduate study. However, their application to typical design and analysis cases, especially those with multiple loads, is typically very cumbersome and it has become normal procedure to use commercially-available beam analysis software for such problems. The Beam Calculator program supplied with this book is a basic example.
- Section 9-8 Moment-Area Method [Optional] is preferred by some designers for applications that do not lend themselves to the use of formulas, superposition, or the successive integration approach. A notable example is the analysis of beams with varying cross sections as illustrated in this section.

Chapter 10 – Combined Stresses

The extent of coverage of the several topics in this chapter is best done by the individual instructor and/or program faculty members.

- Sections 10-1 through 10-6 give good introductory coverage of the issues presented when
 two or more types of stresses occur at a given point. They also tie material from previous
 chapters together to help students understand the distribution of stresses and the interactions
 involved. Combined normal stresses and combined normal and shear stresses are
 discussed.
- Sections 10-7 through 10-11 cover stress transformations, equations for stresses in any direction, principal stresses (maximum normal stress, maximum shear stress), and Mohr's circle.
- Section 10-12 covers the use of strain-gage rosettes to determine principal stresses and ties
 well with the preceding sections. It is also related to Section 1-13 Experimental and
 Computational Stress Analysis, and is useful for connecting this course with companion
 laboratory courses.

Chapter 11 - Columns

- This chapter is a succinct, but comprehensive coverage of column analysis.
- Included are basic concepts, Euler formula for long columns, J. B. Johnson formula for short columns, and non-centrally loaded columns (crooked and eccentrically loaded).
- A Column Analysis Spreadsheet is shown that facilitates the calculations.

Chapter 12 - Pressure Vessels

- Basic concepts for thin-walled spheres and cylinders are recommended as a minimum, using Sections 12-1 through 12-4.
- Sections 12-5 through 12-7 [Optional] present extended coverage of thick-walled pressure vessels.
- Sections 12-8 and 12-9 [Optional] present additional considerations for column design.
- Section 12-9 [Optional] discusses the advantages of applying composite materials to pressure vessels. Reference to Section 2-12 should be made for basic properties of composites.

Chapter 13 – Connections

This chapter covers bolted and riveted joints and welded connections.

APPLIED STRENGTH OF MATERIALS 5TH Ed. by Robert L. Mott

Software Included with the Book

INTRODUCTION

Two types of software on a CD-ROM are included with this book:

- 1. A set of 12 interactive video lessons that students can use to:
 - a. Review material from the text for a given topic
 - b. Observe the solution of a representative problem
 - c. Complete a quiz at the end of each module to test understanding
- 2. A versatile beam calculator program that allows:
 - a. The creation of a beam and its loading and support patterns
 - b. Analysis of:
 - i. Shearing force distribution
 - ii. Bending moment distribution
 - iii. Deflection of the beam at all points in the beam
 - iv. Stress due to bending at all points in the beam

The software was created by Professor Jack Zecher of Indiana University - Purdue University - Indianapolis (IUPUI) in Indianapolis, Indiana.

ADVICE ON THE USE OF THE SOFTWARE

As with any software, students are advised to read pertinent text material and master the fundamental principles of the subject and the methods of problem solution prior to using the software.

INTERACTIVE VIDEO LESSONS

The following lessons with guizzes are included in this software:

- 1. **NORMAL STRESS** Reviews the direct normal stress equation, σ = Force/Area for both tension and compression. Illustrates the calculation of direct normal stress on a member with multiple cross section sizes. Relevant to Chapters 1 3.
- 2. **DIRECT SHEAR** Reviews the direct shear stress equation, $\tau = Force/Area$ in shear, for both single shear and double shear. Relevant to Chapters 1 3.
- 3. **PUNCHING SHEAR** Reviews shearing stress that occurs in a cutting or punching situation using the direct shear stress equation, $\tau = Force/Area$ in shear, with emphasis on identifying the correct area in shear. Relevant to Chapters 1 and 3.
- 4. **POISSON'S RATIO** Reviews the definition of strain and the fact that strains in both longitudinal and transverse directions are created when a load-carrying member is subjected to direct normal stress. Reviews the definition of Poisson's ratio. Relevant to Chapters 2 and 3.
- 5. **STRESS CONCENTRATION** Reviews the concept of increased stresses occurring near sections of load-carrying members with abrupt changes in cross section. Illustrates the stress concentration factor for a member loaded in tension. Includes color graphic illustrations of stress lines around a hole and the plot of results of a finite element analysis. Relevant to Chapter 3.
- AXIAL DEFORMATION Reviews the deformation of members loaded in direct tension or compression using the formula, δ = FL/EA. Relevant to Chapter 3.
- 7. **THERMAL STRESSES** Reviews the property of coefficient of thermal expansion, α . Demonstrates the calculation of thermal expansion using the formula, $\delta = \alpha L(\Delta t)$ for a given change of temperature, Δt . Also demonstrates the stress created when members are restrained as temperatures change. Relevant to Chapter 3.
- 8. **STATICALLY INDETERMINATE** Reviews the principles of axial deformation and considers the case when two or more members, possibly made from different materials, are loaded together. Relevant to Chapter 3.
- 9. **TORSIONAL STRESS AND DEFORMATION** Reviews both the torsional shear stress equation, $\tau = Tc/J$ and the torsional deformation equation, $\theta = TL/GJ$. Illustrates calculations for a stepped shaft loaded by two torques and shows a torque diagram. Relevant to Chapter 4.
- 10. **BENDING STRESS** Reviews the bending stress equation, $\sigma = Mc/l$, along with shearing force and bending moment diagrams. A finite element analysis animation is included illustrating how bending stresses are produced as a section of a T-beam deforms. Relevant to Chapters 5 7.
- 11. **SHEAR IN BEAMS** Reviews shearing forces and stresses produced in beams along with bending. Illustrates the application of the beam shearing stress formula, $\tau = VQ/lt$, using a rectangular beam made from glued laminations. Relevant to Chapter 8.

12. **COMBINED NORMAL STRESSES** – Reviews the case when a member is subjected to simultaneous bending and direct normal stresses. Includes a finite element model of such a member. Relevant to Chapter 10.

Notes on the quizzes: After viewing the video of any module, the student may access an interactive quiz in which a situation similar to the example shown in the video is presented with data. The student must complete the analysis on paper and enter the result. The program determines whether the entered result is correct or not and reports back. Students are permitted to enter values twice before the correct solution is shown.

BEAM CALCULATOR

This versatile software permits students to perform analyses of beams with complex loading patterns and with many combinations of support conditions. Its use, after students have mastered the principles of beam analysis by hand calculations, facilitates the evaluation of multiple alternative designs for a beam to explore relationships among variables such as:

- Types of support and their placement relative to the applied loads
- Magnitude of the loads and their placement relative to the supports
- Beam materials and cross section properties such as modulus of elasticity, moment of inertia, and shape

Many more and more complex examples can be analyzed in a given amount of time, extending learning beyond the typical problems that are assigned for practice by hand calculations.

The software uses a finite element analysis-based process that divides the beam into 50 segments. Calculations of results are made for each of the 50 points and at any applied load or support. If the user desires that the results for any other point be given, a concentrated load of zero value may be placed at that point.

Features of the software include:

- Units Units of length are first selected by the user in either English (feet or inches) or Metric (meters or millimeters).
- 2. **Beam Properties** Beam properties are entered by the user for:
 - a Beam length
 - b. Modulus of elasticity, E, for the material of the beam
 - c. Moment of inertia, I, for the cross section shape and dimensions of the beam
 - d. Distance from the neutral axis of the cross section to the top of the beam
 - e. Distance from the neutral axis of the cross section to the bottom of the beam
- 3. **Supports** The type or types of supports and their placement are defined by the user. Up to 20 supports may be used in any combination of:
 - a. Roller support providing only vertical support
 - b. Pinned support providing vertical or horizontal support

- i. Note: Theoretically one roller support and one pin support should be provided for a simply supported beam to ensure equilibrium. However, this program permits only vertical concentrated or distributed loads and couples for which only vertical reactions are computed.
- c. Fixed support providing vertical and moment resistance, such as the support for a cantilever
- d. Before the analysis can proceed, the beam design must have a minimum of either:
 - i. Two pinned supports
 - ii. One pinned and one roller support
 - iii. One fixed support
- e. The user may modify any support type or location before analysis is performed. This feature facilitates correction of entered data or the exploration of several alternative designs.
- 4. **Loads** The user defines any combination of up to 20 loads by giving their placement and magnitudes. The load types available are:
 - a. Concentrated
 - b. **Distributed** Either uniformly or uniformly varying distributed loads can be used. The user enters the placement and magnitude (force per unit length) at the start and at the end of the loading.
 - c. Couple This is a concentrated moment applied at any point along the beam. A counterclockwise couple is considered positive.
- 5. **Analyze** After the beam is defined completely, the user selects the 'Analyze' button. If an incomplete or an excessive set of data are provided, the analysis will not be completed. The following analyses are completed:
 - a. Shear A complete shearing force diagram is shown under the beam design
 - b. Moment A complete bending moment diagram is shown under the beam design
 - c. **Deflection** A complete diagram of the shape of the deflected beam is shown
 - d. Stress The distribution of bending stress across the entire length of the beam is shown
 - e. Notes:
 - Values at any point on any diagram can be displayed by placing the cursor at the desired point.
 - ii. The ESC (escape) key must be used to stop the interaction with the currently displayed diagram before switching from one type of output to another.

Instructors Manual

APPLIED STRENGTH OF MATERIALS Fifth Edition

by

Robert L. Mott

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- for instructors who prefer this approach. However, it is not essential to include coverage of these sections and they are marked [Optional] in the following chapter overviews.
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- Centroids and Moments of Inertia of Areas: Many courses in Statics include these topics. However, there is some advantage in delaying this coverage until these concepts are needed for application to beam analysis within the study of strength of materials. This provides just-in-time coverage that flows naturally as presented in Chapters 5, 6, and 7 in this book. When a particular course requires prerequisite knowledge of Centroids and Moments of Inertia of Areas, Chapter 6 can be skipped. Having the material in the book should be useful for students to review as needed.
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- Sections 1-1 through 1-12 should be covered completely in order to present a foundation for the study of later chapters, to present basic expectations for student performance, and to give students an overview of many of the Appendix tables related to the properties of areas and standard shapes used for structural and mechanical applications. [See Appendixes A-1 through A-13.]
- Sections 1-6 through 1-11 give the basic concepts of stress and strain for direct tension, direct compression, and direct shear.
- The emphasis is on analysis and the understanding of the ability of materials to resist external forces applied to them. This is necessary for progression into Chapter 2 on Design Properties of Materials where some additional material properties are discussed. These basic concepts are expanded upon in Chapter 3.
- Mention should also be made of Appendix A-26 Conversion Factors and Appendix A-27
 Review of the Fundamentals of Statics.
- Coverage of Section 1-13 Experimental and Computational Stress Analysis is optional and may depend on the connection of this course with companion laboratory courses.

Chapter 2 - Design Properties of Materials

Refer to the discussion of **Materials Science** given above in regard to prerequisite study. Most students will benefit from at least a quick review of all parts of this chapter and the related Appendixes. Those without prerequisite knowledge of materials will need more intensive study. Some considerations for coverage are discussed next.

- Students in mechanical, manufacturing, civil and construction programs all require sound knowledge of metals and plastics.
- Most would also benefit from coverage of wood, concrete, and composites.
- Section 2-12 [Optional] on Composites may be delayed until Chapter 7 is covered and linked with Section 7-12 on the design of beams to be made from composite materials.
- The section on Materials Selection gives approaches to relating the expected performance of a structure or product to the behavior of appropriate materials. The method featured here leads to consideration of a wide variety of materials and refers to other references giving more extensive treatment of the materials selection processes. Of particular note is the reference for Dr. Michael Ashby's book, *Materials Selection in Mechanical Design*.

Chapter 3 - Direct Stress, Deformation, and Design

This chapter builds on the basic introductory treatment of direct stresses from Chapter 1 and adds significant competencies in design of load-carrying members. Design stresses are defined and related to the yield strength or ultimate strength of the materials and to the manner of loading; steady, repeated, and impact or shock. Coverage can be grouped as follows:

The Big Picture, Activity, and Chapter Objectives

- Sections 3-2 through 3-6: Design of members under direct normal stresses, including the definition of design stress, design factor (factor of safety), and design approaches.
- Sections 3-7 through 3-11: Deformation, thermal stresses, members made from more than one material, and stress concentration factors for direct axial stresses
- Sections 3-12 and 3-13 on bearing stress, including design bearing stresses
- Section 3-14 Design Shear Stress

Users of previous editions of this book will note that, in response to feedback from colleagues and external reviewers, a significant re-ordering of topics has been done in this new 5th edition. For example, Bearing Stresses were formerly presented in Chapter 1 and deformations and related topics were covered in a separate chapter. It was recommended that both stress and strain (with deformations) be included in one chapter for each type of stress.

Chapter 4 – Torsional Shear Stress and Torsional Deformation

Coverage of this chapter can be groups as follows:

- Big Picture, Activity, and Objectives
- Section 4-2 on Torque, Power, and Rotational Speed: These topics should be review for most students but it has been found that careful study is required before applying them to stress analysis.
- Section 4-3 presents the fundamental torsional shear stress formula and demonstrates its application to the analysis of stresses.
- Sections 4-4 and 4-5 [Optional] use calculus to derive the torsional shear stress formula and the equations for polar moment for solid circular bars.
- Section 4-6 extends the coverage to hollow circular sections. While some calculus is used to develop equations for polar moment of inertia, the final equations are all that is required for problem solving.
- Section 4-7 presents an approach to design of circular members under torsion, extending the design stress concepts from Chapter 3 to include torsional shear strength of materials.
- Section 4-8: This section provides interesting and useful comparison of the behavior of hollow circular sections and emphasizes their efficiency as compared with solid sections.
- Section 4-9: The study of stress concentrations in torsionally loaded members is essential to proper design and analysis of shafts.
- Section 4-10: The twisting of circular bars is discussed with the application of the equation for torsional deformation.
- Section 4-11 [Optional] Torsion in noncircular sections is less frequently encountered in practice. However, it is important for students to understand that such shapes behave quite differently from circular sections.

Chapters 5 through 9: All these chapters deal with beams; members carrying loads perpendicular to their axes. Students should be advised to scan all five chapters to see the progression of topics and to observe how each chapter relates to the others.

Chapter 5 - Shearing Forces and Bending Moments in Beams

- The Big Picture, Activity, and Sections 5-1 through 5-9 are essential. On rare occasions, some programs include some of these topics in the Statics course.
- Section 5-10 [Optional] Free-Body Diagrams of Parts of Structures: Mastery of this topic
 gives students a better fundamental understanding of the behavior of load carrying members
 by visualizing the internal forces, moments, and stresses created by various external loads.
- Section 5-11 [Optional] Mathematical Analysis of Beam Diagrams: Here students apply
 calculus to derive equations for shearing force and bending moments from given beam
 loading and support conditions. This skill is required for later study of Section 9-7 Successive
 Integration Method for deflection of beams, which is, itself, optional.
- Section 5-12 [Optional] Continuous Beams Theorem of Three Moments: Students should, at least, understand that the behavior of beams with three or more supports is quite different from those with only two simple supports as covered in other sections of this chapter.
 Extensive study of this topic, however, would be most beneficial for the civil and construction fields where such beams are frequently applied in bridges and buildings.
- Note: This is one place where the Beam Calculator program supplied with this book can be used effectively for analyzing complex loading patterns after students have mastered the manual process of creating shearing force and bending moment diagrams. The 'Shear' and 'Moment' selections produce complete diagrams immediately after the beam loading and support conditions are defined.

Chapter 6 - Centroids and Moments of Inertia of Areas

This entire chapter may be skipped for those programs in which the coverage of this topic is included in a prerequisite course in Statics. However, review of the procedures for computing the location of centroids and the computation of moments of inertia of areas is typically required. This can be done by moving directly to Sections 6-5, 6-6, and 6-8 where sections commonly encountered in strength of materials are considered, especially those including standard structural shapes such as W-beams, channels, and angles.

For those programs that do not include this topic in prior courses, coverage of Sections 6-1 through 6-6 and 6-8 should be covered as a minimum. These skills are essential to the understanding of concepts in Chapters 7 – 11. Coverage of the other sections of this chapter are optional as discussed next.

Section 6-7 [Optional] uses calculus to derive the moment of inertia of an area, I.

- Section 6-9 [Optional] provides a useful method of analyzing shapes with all rectangular parts. The process can be implemented effectively in a spreadsheet.
- Section 6-10 [Optional] Radius of Gyration is an important property of an area and is most directly applicable to Chapter 11 on Columns. It may be desirable to delay the coverage of this topic to combine it with the study of columns.
- Section 6-11 [Optional] Section Modulus is an important property of an area and is most directly applicable to Chapter 7 on Stress Due to Bending. It may be desirable to delay the coverage of this topic to combine it with the study of beams.

Chapter 7 - Stress Due to Bending

- Sections 7-1 through 7-4 present the foundation material for the analysis of beams.
- Section 7-5 [Optional] uses calculus to derive the flexure formula. It can be skipped or discussed lightly for those programs where detailed use of the calculus is not expected.
- Sections 7-6 through 7-8 cover the transitions from analysis to design of beams.
- Section 7-9 covers stress concentrations in bending situations.
- Section 7-10 is critical, at least from the standpoint that students must understand that the
 flexure formula applies only to symmetrical sections or when the load path passes through
 the flexural center (shear center) of the section. Otherwise twisting combines with the
 bending stress, reducing the capacity of the beam.
- Section 7-11 on Preferred Shapes for Beam Cross Sections is designed to help the novice student understand better why certain shapes are preferred for beams.
- Section 7-12 [Optional] on beams made from composites presents mostly conceptual
 information about the advantages of composites in bending cases and how the shape can be
 optimized to make best use of the special properties of composites. This section refers back
 to Section 2-12 and it may be desirable to cover those two sections together at this point.
- Note: This is one place where the Beam Calculator program supplied with this book
 can be used effectively for analyzing bending stress produced by complex loading
 patterns after students have mastered the manual process making such calculations
 on more simple beams. The 'Stress' selection produces the complete diagram of
 bending stress distribution immediately after the beam loading and support conditions
 are defined. Students should compare this result with the bending moment diagram.

Chapter 8 - Shearing Stresses in Beams

- Sections 8-1 through 8-4 present the fundamental concepts and the general shear formula.
- Section 8-5 [Optional] uses calculus to derive the general shear formula. It can be skipped or discussed lightly for those programs where detailed use of the calculus is not expected.
- Section 8-6 shows the special shear formulas applicable to rectangular, circular, hollow, and thin-webbed sections (e.g. W-beams). These formulas are frequently used.
- Section 8-7 transitions the coverage of shear in beams from analysis to design.

• Section 8-8 on shear flow [Optional] is applicable to beam sections made from component shapes that are fastened, glued, or otherwise assembled where connections are subjected to shear.

Chapter 9 – Deflection of Beams

There appears to be a wide divergence of opinion about what types of beam deflection approaches to cover in a basic course in strength of materials. This book attempts to show all popular approaches and let individual instructors and program faculty members decide which is best for their programs.

Note: This is the place where the Beam Calculator program supplied with this book is most applicable. The complete deflection curve is produced immediately after the beam loading and support conditions are defined by selecting the 'Deflection' button. Comparison of the Deflection curve with the Shear, Moment, and Stress diagrams is advised.

That said, here are some factors to consider in course planning:

- Sections 9-1 through 9-4 present the basic concepts and the widely used formulas for beam deflection, using the extensive list of formulas from Appendixes A-23, A-24, and A-25.
- Section 9-5 gives students some experience in comparing the performance of several ways
 of supporting a given load with regard to the stresses and deflections that result. This should
 help the novice student gain a better 'feel' for what approaches are preferred in different
 applications.
- Section 9-6 extends the material in Section 9-4 to the permit use of beam deflection formulas to a much broader array of applications.
- Section 9-7 on the Successive Integration Method [Optional] provides a more analytical approach to deflection analysis. It requires the use of differential and integral calculus and should be combined with Section 5-11 Mathematical Analysis of Beam Diagrams. Mastery of these concepts would be expected for students who intend to continue their study of applied mechanics in later courses or graduate study. However, their application to typical design and analysis cases, especially those with multiple loads, is typically very cumbersome and it has become normal procedure to use commercially-available beam analysis software for such problems. The Beam Calculator program supplied with this book is a basic example.
- Section 9-8 Moment-Area Method [Optional] is preferred by some designers for applications that do not lend themselves to the use of formulas, superposition, or the successive integration approach. A notable example is the analysis of beams with varying cross sections as illustrated in this section.

Chapter 10 - Combined Stresses

The extent of coverage of the several topics in this chapter is best done by the individual instructor and/or program faculty members.

- Sections 10-1 through 10-6 give good introductory coverage of the issues presented when
 two or more types of stresses occur at a given point. They also tie material from previous
 chapters together to help students understand the distribution of stresses and the interactions
 involved. Combined normal stresses and combined normal and shear stresses are
 discussed.
- Sections 10-7 through 10-11 cover stress transformations, equations for stresses in any direction, principal stresses (maximum normal stress, maximum shear stress), and Mohr's circle.
- Section 10-12 covers the use of strain-gage rosettes to determine principal stresses and ties
 well with the preceding sections. It is also related to Section 1-13 Experimental and
 Computational Stress Analysis, and is useful for connecting this course with companion
 laboratory courses.

Chapter 11 - Columns

- This chapter is a succinct, but comprehensive coverage of column analysis.
- Included are basic concepts, Euler formula for long columns, J. B. Johnson formula for short columns, and non-centrally loaded columns (crooked and eccentrically loaded).
- A Column Analysis Spreadsheet is shown that facilitates the calculations.

Chapter 12 – Pressure Vessels

- Basic concepts for thin-walled spheres and cylinders are recommended as a minimum, using Sections 12-1 through 12-4.
- Sections 12-5 through 12-7 [Optional] present extended coverage of thick-walled pressure vessels.
- Sections 12-8 and 12-9 [Optional] present additional considerations for column design.
- Section 12-9 [Optional] discusses the advantages of applying composite materials to pressure vessels. Reference to Section 2-12 should be made for basic properties of composites.

Chapter 13 - Connections

This chapter covers bolted and riveted joints and welded connections.

APPLIED STRENGTH OF MATERIALS 5TH Ed. by Robert L. Mott

Software Included with the Book

INTRODUCTION

Two types of software on a CD-ROM are included with this book:

- 1. A set of 12 interactive video lessons that students can use to:
 - a. Review material from the text for a given topic
 - b. Observe the solution of a representative problem
 - c. Complete a quiz at the end of each module to test understanding
- 2. A versatile beam calculator program that allows:
 - a. The creation of a beam and its loading and support patterns
 - b. Analysis of:
 - i. Shearing force distribution
 - ii. Bending moment distribution
 - iii. Deflection of the beam at all points in the beam
 - iv. Stress due to bending at all points in the beam

The software was created by Professor Jack Zecher of Indiana University - Purdue University - Indianapolis (IUPUI) in Indianapolis, Indiana.

ADVICE ON THE USE OF THE SOFTWARE

As with any software, students are advised to read pertinent text material and master the fundamental principles of the subject and the methods of problem solution prior to using the software.

INTERACTIVE VIDEO LESSONS

The following lessons with quizzes are included in this software:

- 1. **NORMAL STRESS** Reviews the direct normal stress equation, σ = Force/Area for both tension and compression. Illustrates the calculation of direct normal stress on a member with multiple cross section sizes. Relevant to Chapters 1 3.
- 2. **DIRECT SHEAR** Reviews the direct shear stress equation, $\tau = Force/Area$ in shear, for both single shear and double shear. Relevant to Chapters 1 3.
- 3. **PUNCHING SHEAR** Reviews shearing stress that occurs in a cutting or punching situation using the direct shear stress equation, τ = Force/Area in shear, with emphasis on identifying the correct area in shear. Relevant to Chapters 1 and 3.
- 4. **POISSON'S RATIO** Reviews the definition of strain and the fact that strains in both longitudinal and transverse directions are created when a load-carrying member is subjected to direct normal stress. Reviews the definition of Poisson's ratio. Relevant to Chapters 2 and 3.
- 5. **STRESS CONCENTRATION** Reviews the concept of increased stresses occurring near sections of load-carrying members with abrupt changes in cross section. Illustrates the stress concentration factor for a member loaded in tension. Includes color graphic illustrations of stress lines around a hole and the plot of results of a finite element analysis. Relevant to Chapter 3.
- 6. **AXIAL DEFORMATION** Reviews the deformation of members loaded in direct tension or compression using the formula, $\delta = FL/EA$. Relevant to Chapter 3.
- 7. **THERMAL STRESSES** Reviews the property of coefficient of thermal expansion, α . Demonstrates the calculation of thermal expansion using the formula, $\delta = \alpha L(\Delta t)$ for a given change of temperature, Δt . Also demonstrates the stress created when members are restrained as temperatures change. Relevant to Chapter 3.
- 8. **STATICALLY INDETERMINATE** Reviews the principles of axial deformation and considers the case when two or more members, possibly made from different materials, are loaded together. Relevant to Chapter 3.
- TORSIONAL STRESS AND DEFORMATION Reviews both the torsional shear stress
 equation, τ = Tc/J and the torsional deformation equation, θ = TL/GJ. Illustrates calculations for a
 stepped shaft loaded by two torques and shows a torque diagram. Relevant to Chapter 4.
- 10. **BENDING STRESS** Reviews the bending stress equation, $\sigma = Mc/l$, along with shearing force and bending moment diagrams. A finite element analysis animation is included illustrating how bending stresses are produced as a section of a T-beam deforms. Relevant to Chapters 5 7.
- 11. **SHEAR IN BEAMS** Reviews shearing forces and stresses produced in beams along with bending. Illustrates the application of the beam shearing stress formula, $\tau = VQ/lt$, using a rectangular beam made from glued laminations. Relevant to Chapter 8.

12. **COMBINED NORMAL STRESSES** – Reviews the case when a member is subjected to simultaneous bending and direct normal stresses. Includes a finite element model of such a member. Relevant to Chapter 10.

Notes on the quizzes: After viewing the video of any module, the student may access an interactive quiz in which a situation similar to the example shown in the video is presented with data. The student must complete the analysis on paper and enter the result. The program determines whether the entered result is correct or not and reports back. Students are permitted to enter values twice before the correct solution is shown.

BEAM CALCULATOR

This versatile software permits students to perform analyses of beams with complex loading patterns and with many combinations of support conditions. Its use, after students have mastered the principles of beam analysis by hand calculations, facilitates the evaluation of multiple alternative designs for a beam to explore relationships among variables such as:

- Types of support and their placement relative to the applied loads
- Magnitude of the loads and their placement relative to the supports
- Beam materials and cross section properties such as modulus of elasticity, moment of inertia, and shape

Many more and more complex examples can be analyzed in a given amount of time, extending learning beyond the typical problems that are assigned for practice by hand calculations.

The software uses a finite element analysis-based process that divides the beam into 50 segments. Calculations of results are made for each of the 50 points and at any applied load or support. If the user desires that the results for any other point be given, a concentrated load of zero value may be placed at that point.

Features of the software include:

- Units Units of length are first selected by the user in either English (feet or inches) or Metric (meters or millimeters).
- 2. **Beam Properties** Beam properties are entered by the user for:
 - a. Beam length
 - b. Modulus of elasticity, *E*, for the material of the beam
 - c. Moment of inertia, I, for the cross section shape and dimensions of the beam
 - d. Distance from the neutral axis of the cross section to the top of the beam
 - e. Distance from the neutral axis of the cross section to the bottom of the beam
- 3. **Supports** The type or types of supports and their placement are defined by the user. Up to 20 supports may be used in any combination of:
 - a. Roller support providing only vertical support
 - b. Pinned support providing vertical or horizontal support

- i. Note: Theoretically one roller support and one pin support should be provided for a simply supported beam to ensure equilibrium. However, this program permits only vertical concentrated or distributed loads and couples for which only vertical reactions are computed.
- c. Fixed support providing vertical and moment resistance, such as the support for a cantilever
- d. Before the analysis can proceed, the beam design must have a minimum of either:
 - i. Two pinned supports
 - ii. One pinned and one roller support
 - iii. One fixed support
- e. The user may modify any support type or location before analysis is performed. This feature facilitates correction of entered data or the exploration of several alternative designs.
- 4. **Loads** The user defines any combination of up to 20 loads by giving their placement and magnitudes. The load types available are:
 - a. Concentrated
 - b. **Distributed** Either uniformly or uniformly varying distributed loads can be used. The user enters the placement and magnitude (force per unit length) at the start and at the end of the loading.
 - c. Couple This is a concentrated moment applied at any point along the beam. A counterclockwise couple is considered positive.
- 5. **Analyze** After the beam is defined completely, the user selects the 'Analyze' button. If an incomplete or an excessive set of data are provided, the analysis will not be completed. The following analyses are completed:
 - a. Shear A complete shearing force diagram is shown under the beam design
 - b. **Moment** A complete bending moment diagram is shown under the beam design
 - c. **Deflection** A complete diagram of the shape of the deflected beam is shown
 - d. Stress The distribution of bending stress across the entire length of the beam is shown
 - e. Notes:
 - i. Values at any point on any diagram can be displayed by placing the cursor at the desired point.
 - ii. The ESC (escape) key must be used to stop the interaction with the currently displayed diagram before switching from one type of output to another.

CHAPTER 1 Basic Concepts in Strength of Materials

- 1-1 TO 1-15 ANSWERS IN TEXT.
- 1-16 W=m·g= 1800kg·9.81 m/s2=17658 kgm/s6=17.7xn3 N W= 17.7 kN
- 1-17 TOTAL WT. = $mq = 4000 kg \cdot 9.81 nn/s^2 = 39.24kN$ EACH FRONT WHEEL: $F_E = (\frac{1}{2})(0.40)(39.24kN) = \frac{7.85 kN}{11.77 kN}$ EACH REAR WHEEL: $F_R = (\frac{1}{2})(0.60)(39.24kN) = \frac{11.77 kN}{11.77 kN}$
- 1-18 LOADING = TOTAL FORCE/AREA

 TOTAL FORCE = 6800kg.9.8/m/s2=66.7 kN

 AREA = (5.0 m) (3.5 m) = 17.5 m²

 LOADING = 66.7 kN/17.5 m² = 3.81 kN/m² = 3.81 kPa
- 1-19 FORCE = WT = M.g = 25 kg. 9.81 m/5 = 245 N K = 5PRING SCALG = 4500 N/m = F/BL ΔL = F = 245 N = 0.0545 m = 54.5 x10 m = 54.5 mm
- 1-22 W=17.7 KN = 17700 N x 0.2248 LB/N = 3980 LB
- $\frac{1-23}{F_R} = 7.85 \text{ kN} \cdot 7850 \text{ N} \times 0.2248 \text{ LB/N} = 1765 \text{ LB}$ $F_R = 11.77 \text{ kN} = 11770 \text{ N} \times 0.2248 \text{ LB/N} = 2646 \text{ LB}$
- 1-24 LOADING = 3.81 kPa = 3.81 x 10 N x 0.224868 1 102 = 78.6 LB
- $\frac{1-25}{K} = \frac{245 \, \text{N} \cdot \text{O.2248 LB}/\text{N}}{N} = \frac{55.1 \, \text{LB}}{39.31 \, \text{IM}} = \frac{25.7 \, \text{LB}/\text{IM}}{N}$ $\Delta L = \frac{F}{K} = \frac{55.1 \, \text{LB}}{25.7 \, \text{LB}/\text{IM}} = \frac{2.14 \, \text{IM}}{N}$

$$\frac{1-26}{7} \quad m = \frac{N}{7} = \frac{2751 LB}{32.2 \, Ff/s^2} = 85.4 \, \frac{L6 \cdot s^2}{FT} = \frac{85.4 \, slocs}{87.2 \, slocs}$$

$$\frac{1-27}{7} \quad m = \frac{N}{3} = \frac{12800 LB}{32.2 \, Ff/s^2} = 398 \, \frac{L6 \cdot s^2}{FT} = \frac{398 \, slocs}{FT}$$

$$\frac{1-29}{FT} \quad p = |7200 \, Poi \times 6.895 \, RPo / Poi = 82.74 \, Rpo$$

$$\frac{1-30}{5} \quad \sigma = 2/600 \, Poi \times 6.895 \, RPo / Poi = 149,000 \, RPo = 149 \, MPo}{500 \, sloco} = \frac{94.5 \, MPo}{500 \, slocoo} = \frac{94.5 \,$$

1-41 LOAD ON SHELF =
$$W = mg = |840 Rg - 9.8 l m/s = |8050 N$$
 $W/2 = 9025 N ON EACH SIDE$
 $ZM_A = 0 = (9025N)(600 mm) - C_V(1200 mm)$
 $C_V = 45/2 N$
 $C = CV/aim 30^* = 9025 N$
 $T = \frac{P}{A} = \frac{C}{M} = \frac{9025 N}{MUZmm)^2/y} = \frac{79.8 M Ra}{MUZmm)^2/y} = \frac{1393 pai}{600}$
 $1 - 42$
 $T = \frac{P}{A} = \frac{70000 L6}{(3.5 m)^2} = \frac{803 pai}{(3.5 m)^2}$
 $1 - 44$
 $T = \frac{P}{A} = \frac{3500 N}{(3.5 m)^2} = \frac{803 pai}{800 mm}$
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$$\frac{1-46}{F} = \frac{200091}{6000} m R h^{2} = \frac{(0.01091)(0.40)(0.40)(3000)^{2}}{A}$$

$$F = \frac{23695}{A} N$$

$$A = \frac{17(16mm)^{2}}{4} + \frac{201}{201mm^{2}} = \frac{119Mpa}{4}$$

$$\frac{1-47}{A} = \frac{23695N}{A} = \frac{119Mpa}{4}$$

$$\frac{1-47}{A} = \frac{130mm^{2}}{A} = \frac{900mm^{2}}{900mm^{2}} = \frac{167Mpa}{4} TENSION$$

$$\frac{F_{0R}}{A} = \frac{150\times10^{3}N}{900mm^{2}} = \frac{167Mpa}{700mm^{2}} TENSION$$

$$\frac{F_{0R}}{A} = \frac{100x^{10}}{400mm^{2}} = \frac{77.8Mpa}{72.8Mpa} TENSION$$

$$\frac{F_{0R}}{A} = \frac{F_{00}}{1000mm^{2}} = \frac{110x^{10}}{900mm^{2}} = \frac{122Mpa}{72.8Mpa} TENSION$$

$$\frac{1-48}{A} = \frac{F_{00}}{A} = \frac{110x^{10}}{900mm^{2}} = \frac{122Mpa}{4} TENSION$$

$$\frac{1-48}{A} = \frac{F_{00}}{A} = \frac{110x^{10}}{900mm^{2}} = \frac{122Mpa}{201mm^{2}} TENSION$$

$$\frac{1-48}{A} = \frac{F_{00}}{A} = \frac{-7.52x^{3}N^{3}N}{91mm^{2}} = \frac{-35.7mpa}{25.7mpa} Compa.$$

$$FOR AG: F_{00} = -9.65 - 12.32 + 4.45 = -17.52 kN$$

$$\frac{F_{0R}}{A} = \frac{F_{00}}{A} = \frac{-7.52x^{3}N^{3}N}{91mm^{2}} = \frac{-35.7mpa}{25.7mpa} Compa.$$

$$FOR BC: F_{00} = -9.65 - 12.32 = -21.97 kN$$

$$\frac{F_{00}}{A} = \frac{F_{00}}{A} = \frac{-2.97x^{10}N^{3}N}{491mm^{2}} = \frac{-44.7mpa}{49.7mpa} Compa.$$

$$FOR CO: F_{00} = -9.65 RN$$

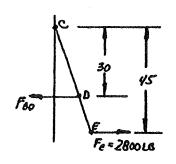
$$\frac{F_{00}}{A} = \frac{-9.65}{A} = \frac{7.65 N^{3}N^{3}}{201mm^{2}} = \frac{-48.0mpa}{48.0mpa} Compa.$$

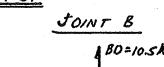
$$\frac{1-49}{A} = \frac{7}{16}[1.90]^{2} - \frac{1}{16}[1]^{2} = 0.799 m^{2} (12mpe-App. A-12)$$

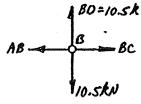
$$FOR AB: F_{AD} = 2500 + 2(8000 Cora30) = 163.5618$$

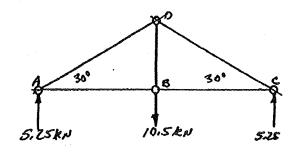
$$\frac{F_{AD}}{A} = \frac{F_{AB}}{A} = \frac{1635410}{0.799m^{2}} = \frac{20471 FS}{1635610} TENSION$$

$$\frac{1-50}{F_{BD}} = \frac{2800(45) - F_{BD}(30)}{F_{BD}} = \frac{4200 \text{ LB}}{4200 \text{ LB}} = \frac{323/\text{pai}}{760500}$$









STRESSES :

$$AB_{,}BC: G_{AB} = G_{BC} = \frac{9.09 \times 10^{3} N}{(12 \times 30) \text{mm}^{2}} = 25.3 \text{ MPQ} \quad TENSION$$

$$BD: G_{BO} = \frac{10.5 \times 10^{3} N}{(2 \times 10)(30) \text{mm}^{2}} = \frac{17.5 \text{ MPQ}}{(2 \times 10)(30) \text{mm}^{2}}$$

BD:
$$\sigma_{BO} = \frac{10.5 \times 10^3 N}{(2 \times 10)(30) mm^2} = 17.5 MPa TENSION$$

6000 1-52 EMA = 0 = 6000(6) +12000(12) -RF(18) RF = 10000 LB $2M_F = 0 = 12000(6) + 6000(12) - R_A(18)$ RA = 8000 LB 18 RA = AB sind = AB(O.F) AB = RA/0.8 = 8000/0.8 = 10000 LG COMP. AD= AB c= = 10000 (0.6)= 6060 LB TENS. 30=0 DE = AD= 6000LB BE sin 0 +6000 - AB sin 0 = 0 6000LB BE = AB sin 8 -6000 _ 10000 (0.8) -6000 = Z500 LB TENS. BC = AB COO + BE COSO = 10000 (0.6) + 2500 (0.6) = BC = 7500 LB COMP. A6= 10000 12000 LB BC = CF Coab CF = Bc/cose = 2500/0.6 = 12500 LB Comp. CE = 12000 - CF sin 0 = 12000-12500(0.8) = 2000L8 C CF= 12000 Lg EF = CF COLO = 12500 (0.6) = 7500LB TENS. STRESSES: Re = 10000 LB OBD =O

AREAS OF MEMBERS : (APP. A5, A6) AD, DE, EF - 2(0,484) = 0.968 142 OCE = 2000/0.484 = 4/32 pui BD, BE, CE - 0.484/N2 A6, BC, CF - 2(1,21) = 2.48/N2 NOTE: COMPRESSION MEMBERS MUST BE CHECKED FOR COLUMN BUCKLING

/2000

$$Ab = 20 \, \text{RN}$$

$$C = \frac{20 \times 10^3 \, \text{N}}{(20)^2 \, \text{mm}^2} = 50 \, \text{MPa}$$

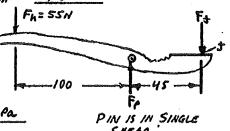
$$\frac{1-54}{0-100000} A = \pi(0.505)^{2}/4 = 0.200W^{2}$$

$$0 = \frac{F}{A} = \frac{12600L8}{0.200} M^{2} = 63.000 pm'$$

$$\frac{1-55}{\sigma = F/A = (52000 LB/4.41/N^2)} = \frac{1.41}{100} = \frac{1.41}{$$

$$\frac{1-56}{\sigma = f_A = 640 \times 10^3 N_{3557 mm^2}} = \frac{180 MPa}{100 MPa}$$

$$\frac{1-58}{2}$$
 $2F_3=0=55(145)-F_9(45)$



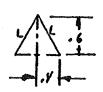
1-59 FROM PROB 1-46: F=23695 N

$$\frac{1-62}{A_s} \quad L = \sqrt{.4^2 + .6^2} = 0.721 \text{ in.}$$

$$A_s = \left[2(1.60) + it(0.8)/2 + 2(0.721) \right] 0.194$$

$$A_s = 1.144 \text{ in}^2$$

$$T = F/A_s = 45000 \text{ LB}/1.144 \text{ in}^2 = 39324 \text{ psi}$$

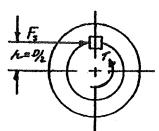


$$\frac{I-63}{F_s} T = F_s \cdot R$$

$$F_s = T/R = \frac{95 \, \text{N·m}}{35 \, \text{mm}/2} \cdot \frac{10^3 \, \text{mm}}{\text{m}} = 5429 \, \text{N}$$

$$A_s = b \cdot L = (00)(22) = 220 \, \text{mm}^2$$

$$T = F_3/A_s = 5429 \, \text{N}/220 \, \text{mm}^2 = 24.764 \, \text{Pa}$$



$$\frac{1-64}{A_5} = \frac{F_5}{F_6} = \frac{8000 \text{ LG.1M}}{10 \text{ M}} = \frac{6000 \text{ LG}}{1000 \text{ LG}}$$

$$A_5 = \frac{1}{5} \cdot \frac{1}{5} = \frac{10.50}{10.50} \cdot \frac{10.50}{10.50} = \frac{1110 \text{ pri}}{10.50}$$

$$\frac{1-65}{7} PIN DOUBLE SHEAR; As = 2(11(0.5)^{2}/1) = 0.393 m^{2}$$

$$T = F/A_{3} = 20000 LB/0.393 m^{2} = 50930 PSi$$

COLLAR SHEAR COLLAR FROM CONNECTOR BODY

$$A_S = \pi d t = \pi(0.875)(0.1875) = 0.51541H^2$$

$$T = f/A_S = 20000 LB/0.51541H^2 = 38800 PS/$$

$$\frac{1-66}{8_{V}} = 800(80) - 8_{V}(8)$$

$$B_{V} = 8000 L8$$

$$B = B_{V}/c_{F2W} = 85/3 L8$$

$$A_{S} = 2(m(0.375)^{2}/V) = 0.221 M^{2}$$

$$B/A_{S} = 85/3 L8/0.221 M^{2} = 38540 PS/$$

- 1-70 $A_3 = 2[T(12)^2/4] = 226.2 mm^2$ Two RIVETS SINGLE SHEAR $T = F/A_3 = D.2 \times 10^3 N/226.2 mm^2 = 45.1 MPa$
- $\frac{1-11}{T} = \frac{1}{4} \left[\frac{1}{12} \left[\frac{1}{12} \right]^{2} \right] = \frac{4}{52.4} \frac{1}{12} \frac{1}{$

CHAPTER 2 **Design Properties of Materials**

ONLY THOSE PROBLEMS REQUIRING NUMERICAL DATA ARE SHOWN.

- 2-14 Sm = 90ksi (62/MPA); Sy = 60ksi (4/4 MPA); 25% FLONG. BECAUSE % ELONGATION 75%, IT IS DUCTILE. (APP. A-14)
- 1020 HR: 36 % ELONGATION GREATER DUCTILITY 2-/5 1040 HR: 25 % ELONGATION
- AISI 1141 OOT 700: HIGH SULFUR ALLAY STEEL WITH 041% CARBON, QUENCHED IN OIL, TEMPERED AT 700'F. (APP. A-14)
- YES. Sy = 172 ksi @ OQT100, Sy = 129 ksi @ OQT 900 2-17 BY INTERPOLATION S, 2/50 kes @ OOT 300. (APP. A-14)
- E = 30×10 6 poi (2076PA) FOR ALL CARBON AND ALLOY STEELS. (APP. A-14)
- 2-19 WT = DENSITY = VOLUME = (0,283 L8/113) (1.0) (4.0) (14.5) 10 = 16.4LB
- (APP. A=14) VALUE OF LBM = VALUE OF LB FORCE (WT.)

 VOLUME = AREA * LENGTH = \$\frac{\pi}{\pi}(50)^2 \times 20 = 4.909 \times 0 mm^3 2-20 STEEL BAR (30) × 20 = 7.909 × 10 mm³

 MASS = 7680 kg × 4.909 × 10⁵ mm³ 1mm³ = 3.97 kg

WT = M.g = 3.77 kg. 9.81 m/s = 36.98 kg/m/s2 = 36.98 N

- MAGNESIUM WOULD BECAUSE IT HAS A LOWER E. Ensa 45 GPa; ET = 114 GPa; TI & STIFFER. (APP. A-15)
- 2-23 ALLOY OF ALUMINUM WITH SILIGN AND MAKNESIUM. HEAT TREATED TO TO TEMPER.
- 2-24 (APP. A-18) Sm DENSITY loxo Psi 0.10 LB/IN3 18 KS1 BKSI 41 6061-T4 35KSi 21 KSi 6061-16 45KSi 40KSi
- 2-29 Sut = 40Ksi; Suc = 140 Ksi (APR. A-17)
- Z-31 BENDING 03 = 1450 PSi; TENSION 03 = 850PSi; COMP. 1000 PSi PARALLA TO GRAW, 385 PSI PER PEN DICULAR TO GRAW; SHEAR To 95 PSI (APP. A-19)
- 2-32 2000 TO 1000 PSI (SECTION 2-10)

2-44 Graphite fibers.

2-45 S-glass, quartz fibers, tungsten fibers coated with silicon carbide.

2-51	Material	Specific strength (in)	Ratio to AISI 1020
	Graphite/Epoxy (High Strength)	4.86x10 ⁶	25.0
	Aramid/Epoxy Composite	4.00x106	20.6
	Boron/Epoxy Composite	3.60x10 ⁶	18.5
	Graphite/Epoxy (Ultra-hi mod)	2.76x106	14.2
	Glass/Epoxy Composite	1.87x10 ⁶	9.63
	Titanium Ti-6AI-4V	1.00x106	5.15
	AISI 5160 OQT 700 Steel	0.929x106	4.78
	Aluminum 7075-T6	0.822x106	4.23
	Aluminum 6061-T6	0.459x10 ⁶	2.36
	AISI 1020 HR Steel	0.194x10 ⁶	1.00
2-52	Material	Specific modulus	Ratio to
		(in)	AISI 1020
	Graphite/Epoxy (Ultra-hi mod)	8.28x10 ⁸	7.81
	Boron/Epoxy Composite	4.00x10 ⁸	3.77
	Graphite/Epoxy (High Strength)	3.45x10 ⁸	3.25
	Aramid/Epoxy Composite	2.20x108	2.07
	AISI 1020 HR Steel	1.06x10 ⁸	1.00
	AISI 5160 OQT 700 Steel	1.06x10 ⁸	1.00
	Titanium Ti-6AI-4V	1.03x10 ⁸	0.97
	Aluminum 6061-T6	1.02x10 ⁸	0.96
	Aluminum 7075-T6	0.99x108	0.93
	Glass/Epoxy Composite	0.66x10 ⁸	0.62

$$2-60$$
 $V_m = 1 - V_f = 1.0 - 0.60 = 0.40$

2-62 See Equations (2-1/1), (2-1/2), (2-1/3), (2-1/4)).

²⁻⁶¹ See Equation (2-1/0).

```
Use Equation (2-10): s_{uc} = s_{uf} V_f + \sigma_{m'} V_m
          Strain at which fibers would fail: \varepsilon_f = s_{uf} / E_f = (820 \times 10^3 \text{ psi})/(40 \times 10^6 \text{ psi})
                   \varepsilon_f = 0.0205
          Stress in matrix at this strain: \sigma m' = Em \epsilon = (0.56 \times 10^6 \text{ psi})(0.0205) = 11 480 \text{ psi}
          Then: s_{uc} = (820x \ 10^3 \ psi)(0.50) + (11 \ 480 \ psi)(0.50) = 415x10^3 \ psi
          Modulus of elasticity:
                                          E_c = E_f V_f + E_m V_m = (40 \times 10^6)(0.5) + (0.56 \times 10^6)(0.50)
                   E_C = 20.3 \times 10^6 \text{ psi}
          Specific weight: \gamma_C = \gamma_f V_f + \gamma_m V_m = (0.065)(0.50) + (0.047)(0.50)
                    y_c = 0.056 \text{ lb/in}^3
2-64 Given: V_f = 0.50; Fibers are high modulus carbon; Matrix is Epoxy
          See Table 2-/5 for data. V_m = 1 - V_f = 1.0 - 0.50 = 0.50
          Use Equation (2-16): s_{uc} = s_{uf} V_f + \sigma_{m'} V_m
         Strain at which fibers would fail: \varepsilon_f = s_{uf} / E_f = (325x \ 10^3 \ psi)/(100x10^6 \ psi)
                          \epsilon_f = 0.00325
         Stress in matrix at this strain: \sigma_{m'} = E_m \epsilon = (0.56 \times 10^6 \text{ psi})(0.00325) = 1820 \text{ psi}
         Then: s_{uc} = (325x \ 10^3 \ psi)(0.50) + (1820 \ psi)(0.50) = 163x10^3 \ psi
         Modulus of elasticity:
                                          E_c = E_f V_f + E_m V_m = (100 \times 10^6)(0.5) + (0.56 \times 10^6)(0.50)
                  E_c = 50.3 \times 10^6 \text{ psi}
         Specific weight: \gamma_C = \gamma_f V_f + \gamma_m V_m = (0.078)(0.50) + (0.047)(0.50)
                   \gamma_{\rm C} = 0.0625 \, \text{lb/in}^3
2-65 Given: V_f = 0.50; Fibers are aramid; Matrix is Epoxy
         See Table 2-15 for data. V_m = 1 - V_f = 1.0 - 0.50 = 0.50
         Use Equation (2-/e): s_{uc} = s_{uf} V_f + \sigma_{m'} V_m
         Strain at which fibers would fail: \varepsilon_f = s_{uf} / E_f = (500x 10^3 psi)/(19x10^6 psi)
                  \varepsilon_f = 0.0263
         Stress in matrix at this strain: \sigma_{m'} = E_m \epsilon = (0.56 \times 10^6 \text{ psi})(0.0263) = 14 740 \text{ psi}
        Then: s_{uc} = (500x \ 10^3 \ psi)(0.50) + (14 \ 740 \ psi)(0.50) = 257x10^3 \ psi
         Modulus of elasticity:
                                         E_C = E_f V_f + E_m V_m = (19x10^6)(0.5) + (0.56x10^6)(0.50)
                  E_C = 9.78 \times 10^6 \text{ psi}
         Specific weight: \gamma_C = \gamma_f V_f + \gamma_m V_m = (0.052)(0.50) + (0.047)(0.50)
                  \gamma_c = 0.0495 \text{ lb/in}^3
```

2-63 Given: $V_f = 0.50$; Fibers are high strength carbon-PAN; Matrix is Epoxy

See Table 2-15 for data. $V_m = 1 - V_f = 1.0 - 0.50 = 0.50$

Solutions to Problems 2-66 to 2-67: Some data approximated from Figure P2-66. Most accurate values are for Ultimate strength (b.)and % elongation (f). Elastic limit (d.) estimated between proportional limit (c.) and yield strength (a.) Modulus of elasticity (e.) computed from (Δ stress / Δ strain). Data are approximated Materials found from Appendixes A-13 through A-17 matching s_u, s_y, % Elongation, and E

- **2-66** a. $s_v = 73 \text{ ksi} \text{Offset}$
 - b. $s_0 = 83 \text{ ksi}$
 - c. $s_0 = 60 \text{ ksi}$
 - d. $s_{el} = 67 \text{ ksi}$
 - e. $E = 10.0 \times 10^6 \text{ psi}$
 - f. 11% Elongation
 - g. Ductile
 - h. Aluminum
 - I. 7075-T6
- **2-68** a. $s_v = 62$ ksi Offset
 - b. $s_u = 75 \text{ ksi}$
 - c. $s_p = 50 \text{ ksi}$
 - d. $s_{el} = 56 \text{ ksi}$
 - e. $E = 16.7 \times 10^6 \text{ psi}$
 - f. 15% Elongation
 - g. Ductile
 - h. Copper Alloy
 - I. C54400 Bronze-hard
- 2-70 a. No sy-Brittle
 - b. $s_u = 55 \text{ ksi}$
 - c. $s_p = 50 \text{ ksi}$
 - d. $s_{el} = 53 \text{ ksi}$
 - e. $E = 20.0 \times 10^6 \text{ psi}$
 - f. 0.5% Elongation
 - g. Brittle
 - h. Cast Iron
 - I. ASTM A48 Grade 60
- 2-72 a. $s_v = 35 \text{ ksi}$ Yield point
 - b. $s_u = 57 \text{ ksi}$
 - c. $s_0 = 30 \text{ ksi}$
 - d. $s_{el} = 27 \text{ ksi}$
 - e. $E = 26x10^6$ psi
 - f. 21% Elongation
 - g. Ductile
 - h. Structural Steel
 - I. ASTM A36

- **2-67** a. $s_y = 173$ ksi Yield point
 - b. $s_u = 187 \text{ ksi}$
 - c. $s_p = 162 \text{ ksi}$
 - d. $s_{el} = 168 \text{ ksi}$
 - e. $E = 29.0 \times 10^6$ psi
 - f. 15% Elongation
 - g. Ductile
 - h. Steel
 - I. AISI 4140 OQT 900
- 2-69 a. $s_v = 49 \text{ ksi} \text{Yield point}$
 - b. $s_u = 65 \text{ ksi}$
 - c. $s_p = 46 \text{ ksi}$
 - d. $s_{el} = 48 \text{ ksi}$
 - e. $E = 26.5 \times 10^6 \text{ psi}$
 - f. 36% Elongation
 - g. Ductile
 - h. Steel
 - I. AISI 1020 CD
- 2-71 a. $s_v = 53 \text{ ksi} \text{Offset}$
 - b. $s_u = 59 \text{ ksi}$
 - c. $s_p = 31 \text{ ksi}$
 - d. $s_{el} = 42 \text{ ksi}$
 - e. $E = 12.0 \times 10^6 \text{ psi}$
 - f. 5.0% Elongation
 - g. Borderline Brittle/Ductile
 - h. Zinc
 - I. Cast ZA-12
- 2-73 a. $s_v = 19 \text{ ksi} \text{Offset}$
 - b. $s_u = 40 \text{ ksi}$
 - c. $s_0 = 14 \text{ ksi}$
 - d. $s_{ei} = 17 \text{ ksi}$
 - e. $E = 6x10^6$ psi
 - f. 5% Elongation
 - g. Borderline Brittle/Ductile
 - h. Magnesium
 - I. ASTM AZ 63A-T6

2-74 a. $s_y = 155 \text{ ksi - Offset}$

b. $s_u = 170 \text{ ksi}$

c. $s_p = 142 \text{ ksi}$

d. $s_{el} = 149 \text{ ksi}$

e. $E = 16.5 \times 10^6 \text{ psi}$

f. 8% Elongation

g. Ductile

h. Titanium

I. 6AI-4V

2-76 a. $s_v = 80 \text{ ksi} - \text{Offset}$

b. $s_u = 90 \text{ ksi}$

c. $s_p = 62 \text{ ksi}$

d. $s_{el} = 71 \text{ ksi}$

e. $E = 26x10^6$ psi

f. 15% Elongation

g. Ductile

h. Stainless Steel

I. AISI 430 full hard

2-75 a. $s_y = 40 \text{ ksi} - \text{Offset}$

b. $s_u = 45 \text{ ksi}$

c. $s_p = 30 \text{ ksi}$

d. $s_{el} = 35 \text{ ksi}$

e. $E = 10.0x10^6$ psi

f. 17% Elongation

g. Ductile

h. Aluminum

I. 6061-T6

2-77 a. s_v = 80 ksi - Offset

b. $s_u = 95 \text{ ksi}$

c. $s_p = 55$ ksi

d. $s_{el} = 68 \text{ ksi}$

e. $E = 26x10^6$ psi

f. 2.0% Elongation

g. Brittle, but does yield

h. Malleable Iron

I. ASTM A220 Grade 80002

CHAPTER 3 Design of Members Under Direct Stresses

$$\frac{3-1}{\pi} = \frac{8.50 \times 10^{3} N}{\pi (10 mm)^{3}/y} = 10B MPa = 65 = 5y/2$$

$$REO'D Sy = 2 G_{0} = 2(108 MPa) = 216 MPa$$

$$ALUMINUM 2014-TY HAS Sy = 290 MPa (APPENDIX A - 18)$$

$$\frac{3-2}{(10)(30)} = 66.7 M R = 03 = 5 M/8$$

$$REQD SM = 8 03 = 8 (66.7 M Ra) = 533 M Ra PLUS GOOD DUCTILITY$$

$$AISI 1141 ANNEALED HAS SM = 600 M Ra; 26% ELANGATION. (A-14)$$

$$\frac{3-3}{3-3}$$
 $\sigma = \frac{9}{A} = \frac{1720 \text{ LB}}{(0.4014)^2} = \frac{10750 \text{ PS}}{8} = \frac{54}{8}$

REQD $\frac{5}{M} = \frac{8}{3} = \frac{8(10750)}{8} = \frac{86000 \text{ PS}}{8} = \frac{1}{8} = \frac$

$$\frac{3.4}{\pi} = \frac{1850 \, L6}{\pi \, (0.375 \, m)^2 / 4} = 16750 \, \text{poi} = 0.3 = 0.60 \, \text{Sy} \quad (A15C)$$

$$Read \, \frac{Sy}{\pi} = \frac{0.3}{0.60} = \frac{16750 \, \text{poi}}{0.60} = \frac{27900 \, \text{poi}}{0.60} = \frac{27900 \, \text{poi}}{0.60} = \frac{16750 \, \text{poi}$$

$$\frac{3-6}{b} \stackrel{\text{a)}}{\text{NO.1 GRADE DOUGLAS FIR HAS }} \frac{\text{ALLOW}}{\text{DALLOW}} = 1050 \text{PSi} \qquad (A-19)$$

$$10 \text{ USE NO.1 GRADE SOUTHERN PINE: }} \frac{\text{DALLOW}}{\text{DALLOW}} = 575 \text{ psi}$$

$$REDD \text{ AREA} = \frac{P}{\sigma} = \frac{5200 \text{ LB}}{515 \text{ LB}/M^2} = 9.04 \text{ JN}^2; \text{ USE 2XB UR YXY}}$$

$$0R \text{ TWO } \text{ ZXY}.$$

$$\frac{3-7}{\sigma} = \frac{9/4}{3} \cdot \frac{A = \frac{\rho}{\sigma} = \frac{6400 \text{ LB}}{12000 \text{ LB}/M^2} = 0.533 \text{ M}^2 = 170^2/4$$

$$\frac{REQD}{SPECIFY} = \frac{9/4}{18} \cdot \frac{170^2}{18} \cdot \frac{170^$$

- 3-9 FORCE ON SHELF = 1840 Ag. 9.81 m/s = 18050 N : 9025 N/S 10E

 Cy = Ay = 9025 N/2 = 4513 N

 C = Cy/Din 20° = 13 194 N

 C = FORCE IN ROD

 REDD A = C = 13194 N = 120 mm = 11 D = 14

 REDD D = 14A/T = 14(120 mm)/T = 12.4 mm

 SPECIFY D = 14.0 mm
- $\frac{3-10}{\Lambda} = \frac{P}{\Lambda} = \frac{70\,000 \, L^0}{\Pi(8.0 \, \text{IM})^2/4} = 13\,93 \, \text{PS} \, i = \frac{1}{4} \times \text{RATEO STRENATH (SEC. 2-10)}$ $REGIO \, RATEO \, STRENATH = 4(/393) = 55\,70 \, \text{PS} \, i$ $SPECIFY \, \underline{6000 \, PS} \, RATEO \, STRENATH$
- 1-11 LOAD ON EACH BLOCK = 29 500 L6/3 = 9833 LB

 O = P = 9833 LB = 803 PSi

 IF COMPRESSION IS PERPENDICULAR TO GRAIN, NO SUITMOLE WOOD LISTED.

 IF PARALLEL TO GRAIN: NO. / SOUTH. PINE OALL = 850 PSi

 NO. 2 DOIGLAS FIR OALL = 1000 PSi
- $\frac{3.72}{PREND} = \frac{PATED STRENGTH}{Y} = \frac{20.7 MPa}{7} = 5.18 MPa \quad (SEC. 2-10)$ $REND A = \frac{P}{\sigma} = \frac{1.50 \times 10^6 N}{5.18 N Imm} = 2.90 \times 10^5 mm = 170^7/Y$ $REND D = \sqrt{4A/A} = 607 mm ; SPECIFY 700 mm DIA.$
- $\frac{3-13}{A} S_{M} = 483 MPA = \sigma = P/A_{3}P = \sigma \cdot A \qquad (A-10)$ $A = \pi(12^{2}-10^{3})/4 = 34.56 mm^{2}$ $P = \sigma \cdot A = 483 \frac{N}{mm^{2}} \cdot 34.56 mm^{2} = 16.7 \times 10^{3} N = 16.7 \times N$
- 3-14 A = (40 mm) = 1600 mm 3 OALLOW. = 1.69 MPD. I GRAW (A-19)

 OBLOW. = 5.52 MPD. II GRAW (#2 HEMLOCK)

 P = O A = (1.69 N/mm²)(1600 mm²) = 2.70 kN 1 GRAW

 P = O A = (5.52 N/mm²)(1600 mm²) = 8.83kN 1/GRAW
- $\frac{375}{REOD} O_{3} = 0.60(50 \text{Ks}) = 30.0 \text{Ks} = P/A \quad (A15C) \quad (A-16) \quad S_{Y} = 50 \text{Ks};$ $REOD A = P/O_{3} = \frac{4000 \text{LB}}{30000 \text{LB}/M^{2}} = 0.133 \text{/N}^{2} = \Pi D^{2}/V \qquad IF D < 0.75 \text{/N}$ $REOD D = \sqrt{\frac{4A}{\Pi}} = \sqrt{\frac{4(0.133 \text{/N}^{2})}{\pi}} = 6.472 \text{/M}$ $SPECIFY D = \frac{7}{6} \text{/M}. \quad (0.4375 \text{/M}.) \quad OR \quad 0.500 \text{/M}. \quad (0k-0<0.75 \text{/M}.)$

- $\frac{3-16}{\sigma} = \frac{4-(2.65)(1.40) + 2\left[\frac{1}{2}(1.40)(0.5)\right] = 4.41/N^{2}}{4.41/N^{2}} = \frac{1179195i}{4.41/N^{2}} = \frac{52000 \text{ LB}}{4.41/N^{2}} = \frac{1179195i}{1179195i} = \frac{5000}{1179195i} = \frac{6.78}{1179195i}$
- 3-17 FOR SHOCK LOADING DUCTILE METAL! 03=5mc/12

 9= 1650 MPa/12 = 137.5 MPa (A-17)

 REDD A = P 135 x 13 N = 982 Mm = BH = B(28) = 28²

 REDD B = \[\frac{A/2}{82} = \frac{982}{2} = 22.2 mm; H = 44.4 mm

 SPECIFY B = 25.0 mm; H = 50.0 mm
- $\frac{3-18}{REDD} = \frac{5}{MB} = \frac{9}{9000} \cdot \frac{100}{18} = \frac{9}{1000} \cdot \frac{100}{1000} = \frac{9}{1000} \cdot \frac{100}{18} = \frac{9}{1000} \cdot \frac{100}{100} = \frac{9}{1000} \cdot \frac{100}{1000} = \frac{9}{1000} \cdot \frac{100}{1000} = \frac{9}{1000} = \frac{9}{1000} = \frac{9}{1000} = \frac{9}{1000} = \frac{9}{100$
- 3-19 $A = (80)(40) (60)(15) + \Pi(40)^2/4 = 3551 \text{ m/m}^2$ $O = P = 840 \times 10^3 \text{ N}$ $A = 3551 \text{ m/m}^2 = 180 \text{ MPa} = 0$ FOR OUTTLE METALS; $O_3 = 54/2$ REO'D. $S_y = 2(180) = 360 \text{ MPa}$ POSSIBLE METALS: AISI 1040 HR, $S_y = 4/4$ MPa (A-14)

 AISI 4140 ANNEALED, $S_y = 341 \text{ MPa}$ (A-14) $C54400 \text{ Bronze}, S_y = 343 \text{ MPa}$ (A-15)

 ALUMINUM 2014-76, $S_y = 441 \text{ MPa}$ (A-14)

 A131 1020 CD, $S_y = 441 \text{ MPa}$ (A-14)
- 3-20
 SEE PROB. 1-48: OMAX = -48.0 MPa COMPRESSION

 ON = 0.6 Sy = 0.6 (Z48 MPa) = 149 MPa (AISC) (A-16)

 OK FOR COMPRESSIVE STRESS.

 COLUMN BUCKLING SHOULD BE CHECKED.
- 3-21 \(\sigma = 50 \text{ MPA IN MEMBER AB SEE PROB 1-53.} \)
 \[\sigma = 5m/B \; Reo'O Sm = 80 = 8(50) = 400 \text{ MPA } \]
 \[ALUHINUM \(\text{ZO14-T4}, \text{Sm = 427 MPa}; \(\text{ZO'O ELONG.} \)
 \[\left(A-18 \right) = \text{SM = 427 MPa}; \(\text{ZO'O ELONG.} \)
- 3-22 A = 0.944 /N2; 03 = 0.60 Sy = 0.60 /36000 esi) = 2/600 esi PALLOW. = 03 · A = (2/600 LB/N2) (0.444 /N2) = 203910 LB

3-27 (CONTINUED) MASS = VOL * DENSITY * A *L * DENSITY STEEL: MASS = (88.8 mm3) (630 mm) (7650 Reg/m3) 1 1/m2 = 0.420 kg ALUMS MASS = (266.3)(630)(2770)/109=0.465 Ag $A = \Pi D^{2}/Y = \Pi (12)^{2}/Y = 113.1 mm^{2}; O = F/A = 17000 N/113.1 mm^{2} = 150 MPa$ $S = \frac{FL}{EA} = \frac{(17.0 \times 10^{3} N)(220 mm)}{(207000 N/mm^{2})(113.1 mm^{2})} = 0.160 mm$ Low - DK Factorial Forester3-29 a) Ti-6AL. 4V: E= 114 GPa= 114000 MPA = 114000 N/MM2, SY=1070 MPa 8= FL = (114000 N)(1250 mm) = 0.851 mm; 0= # =78,1 MPa LOW-OK b) AISI 501 00T 1800 STERSI . E = 200 GPA = 200 000 N/mm, Sy=93/MBa 8= FL = (5000)(1250) = 0.488 mm 3-30 REO'D. A= F 35000 LB 2/620 N2: USE LYXY X/4; A=/94/N2 8 - Ft - (25000 LB)(13.0FT)(12/N/FT) = 0.097 /H

3-31 ELONGATION: S. FL . (450 L6) (8.40 IN)

COMPRESSION: S. FL . (50) (8.40)

(30×10 L6) (1.25) (1.25) ... 0.000 45 IN

(30×10 (30×10) (.25) ... 0.000 45 IN

STRESS OF = FE/A = (450) 0.03125 = 14400 PS; <54 FOR ANY STEEL REPEATED LEAD: 00 = Sub/8; SMMIA 8(14.4KSi) = 115KSi, AISI 1141 OQT 1100, SM=116KSI

 $\frac{3-32}{MOSECTION!} = \frac{1000}{1000} = \frac{1000}{1000} = 0.0033M$ $\frac{MOSECTION!}{5000} = \frac{1000}{1000} = \frac{10000}{1000} = 0.0033M$ $\frac{MOSECTION!}{50000} = \frac{10000}{1000} = \frac{100000}{1000} = \frac{10000}{1000} = \frac{100000}{1000} = \frac{10000}{1000} = \frac{100000}{1000} = \frac{10000}{1000} =$ TOTAL: ST = SI + S3 = 0.0278 IN

3-33 A= 11(B=01) N=11(1252+11267)/4=0.23/411 F = SEA = (0.050M)(10 X10 LE/IN)(0.2314 IN) = 32/4 LB 0 = F/A = 3218 10/0.23/4 1N2 = 13 900 85/ TOO HIRH-A = TT (0.1-041)/y = TT(0.75'-0.563')/y = 0.1928/N2 0= F/A = Z500 LO / 0.1928/112 = 12964 PS/ = 02 = 51/2; Sy=25 930 PS/ ALUMINUM 3003-HIE HAS SY = 27000 /S/ E= FL = (25006)(8.75 FT)(14N/FT) = 0.136 /N

3-40 00 = F/4 = 64000 L8/50.27 100 = 1273 051; LET 02>400 = 5092 psi USE for = 6000 PS i RATED: THEN E = 4.7 X/0 PS; (SEC Z-10)

Α = Π(8) / Y = 50.71 IN ; Α = 6.02 IN (APP. A-9); ET = 29 X/0 PS; S = Sc +ST = (64000 LB) (3.0 FT) (1211/FT) + (64000) (86) (11) STRUCTURAL STEEL 8=0.00981N + 0.0378 N = 0.0476 IN , 07 = 64060 = 10 631 PS ; < Sy 6.02 FOR ASTM A36 $\frac{3-41}{2} \text{ a) } 8 = \frac{FL}{EA} = \frac{(120L6)(10.5FT)(12N/FT)}{(17N/6L6/N^2)(0.00322N^2)} = 0.276/N.$ A = TO 1/4 = T(D,OH) 1/4 = 0.00322 142 0 = F/A = 12010/0.00322 in= 37300 PSi; CLOSE 10 Sp= 44000 PSI b) $\sigma = f = \frac{200 \, \text{L}^{0}}{0.00322 \, \text{IN}^{2}} = 62 \, 200 \, \text{PS} / \text{3 THIS EXCEEDS THE$ ULTIMATE STRENATH OF THE WIRE. IT SHOVLD BREAK. $\frac{3-42}{6} = \frac{61}{60} = \frac{2518/0.000(0.75) m^2}{(2518)(25F7)(1214/F7)} = \frac{5556}{600} \frac{65}{600}$ 3-43 F= OALLOW'A = (550LR/M2)(12.25/N2) = 6737LB S=FL = (673718 X 10.75FT)(121H/FT) == 0.0551H 3-44 A= (2002-1502)= 12500 mm2 F= O A = (-200 N/mm) (17500 mm)=-3 5 x/0 N=-3,50 MN 8 = 0 L = (200 N/min) (1800 mm) =-2.18 mm 3-45 A = 110 /4 - 11 (3.0) 2/4 = 7.07 mm 2: (ASSUME MASS OF PLATE IS SMALL) F= SEA = (6.0 Mm Y 110 000 N/Mm2) (7.07 Mm2) = 1296 N 0= F/A = 1296 N/202 mm = 183 MPa (LESS MANSY) m = W/9 = 12 96 N/9.8 m/5 = 132 N.5 2/m = 132 & g 3-46 0=50MPa (PROB 1-53): 8 = 0-6/8 = (50 H/mm) (1250 mm) = 0.906 mm Thermal Deformation and Thermal Stress S=&L(at)= 6.0 x10-6 of +)(80 FT)(1400F) x(121N)/FT = 0.806 /N 3-47 S= XL(at) = (1.3 x10 -6 x-1)(12 000 mm)(77'2) = 10.4 mm 3-48 0= EX(At)= (207 X109 PAX /1.3x/06 12-1)(7)12)=180 MPa HIGH! 3-49 8= al(at)= (1.3x10-6°C-11625mm)(156°C)= 1.10 mm 3-50 3-51 a) 8= dl(be)= (11.3x10606-1)(625 mm)(650) = 0.459 mm b) 0=EX(At) = (201x109PAY 11.3x10.6 8-1)(918)=213 MPa 3-52 S= X L(bt)= (60 x 10 6 of 4) (140 ft) (80 f) (12 11/ ft) = 0.806 in.

THIS IS THE TOTAL WIOTH. EACH END COULD BE D.4/IN.

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3-53 DECK COULD EXPAND BY A TOTAL OF O.SO IN WITHOUT STRESS.
      REOD. DE = 5 = 0.50/H (6.0×10-6°F7)(/40 FT)(/21H/FT) = 49.6 °F
       t2=t, +0t=30+49.6= 79.60F
       REMAINING BE 110 F-79.6 F = 30.40F
       O= EX(bt) = (3.8 ×106 B1) (6.0 ×10 47) (30.44) = 693 BSi
3-54 Dt= 116 'F-60 'F= 60 'F
8= & L(Dt) = 6.0x10 6 47)(40x/2/N)(50'F) = 0.504 M
        8 = 17 (55.300) - 17 (55.110) = 0.2 T AMA (CHANGE IN CARCUA FERENCE)
        Dt = 3 = 0.2 x mm = 214.8 °C
        t1=t, + Dt = 20 + 2/4.8= 234.8 °C
       FOR FIRST PART OF COOLING, RING IS UNRESTRAINED UNTIL
        ITS DIAMETER GETS TO 55.200 mm. &= 55.300-55.200=0100000
        Dt = 8 = 0.100 mm = 101.2 °C
         tz= t,-bt= 234.8 °C-/07.2'C= 127.6°C
        ADDITIONAL DE= 127.6-20=107.6 C
         0 = EX(At) = (193 x/0 PR) (16.9 x 10 4 Y-1)/107.6'C) = 35/ MPM
3-57 Sease = ALGE) = (20,5/0 °C-1)(4200 mm)(75°C)= 6.46 mm
        SES = AL(At) = (10.4×1069-1)(4500mm)(758) = 3.51 mm
3-58 &= XL(At) = (6,5x10-6 OF+ X40x12/N)(1900+)=0.593/N
        INITIAL EXPANSION OF O. 10 mm IS UN RESTRAINED.
3-59
        REO'D At = & = 0.10 mm = 15.9°C
         t2=t,+4t = 20 % + 15.9 % = 35.9 %
         ADD. Dt - 70 C - 35.9 C = 34.1 C - RESTRAINED
         T = E A Bt = (45x10 Pa)(25,2x10 6 °C")(34.1 °C) = 38.7 MPa
3-60 O= Eddt = (20) x 10 12 X 11.3 X 10 6 °C-1) (90°C) = 211 MPA
        S. = 10.505 - 10.500 = 0.005 IN UNLESTRAINED
         Dt, = 8 = 0.005 /N = 36.6 °F
         t2= t, +At, = 75+36.6 = 111.60F
         ADD. AT = 400-111.6 = Z88HOF-RESTRAINED
         C= EALAT) = (10x106 PSI) (13.0 X106 PF-1)(288.4 P) = 37 500 PSI
          FOR 6061-TV, SA = 35000051, BAR SHOVLD FAIL.
          ALSO, BEGAUSE BARIS IN COMPRESSION IT MAY BUCKEE.
3-62 Sp = OLIST)=(53.0×10-1 0F7)(30.0 M)(2/2-65)'F=0.2337 IN.
      ST: = AL(Lt) = (5,3 x/6 47)(30.0 m)(N7 4) = 0.0234 M
     ton 0 = 0.2103 = 0.00876
                                                      0.21031H.
        0 = 0.502dex.
```

$$\frac{3-64}{8r} \frac{707AL}{8r} = \frac{0.50mm}{0.00050m} = \frac{8s}{88}$$

$$\frac{8r}{8r} = \frac{4s}{4s} = \frac{8r}{4s} = \frac{0.0005m}{4s^{2}} = \frac{0.0005m}{4s^{2}} + \frac{8r}{4s^{2}} = \frac{0.0005m}{4s^{2}} + \frac{8r}{4s^{2}} = \frac{0.0005m}{4s^{2}} + \frac{8r}{4s^{2}} + \frac{11.90m}{4s^{2}} = \frac{11.45}{11.45} = \frac{11.45}{11.4$$

3-66 WHEN HEATED, WIRE WOULD RELAX.

$$\Delta t = \frac{\sigma}{E\alpha} = \frac{40 \times 10^6 \, Pa}{(193 \times 10^9 \, Pa)(16.9 \times 10^{-6} \, C^{-1})} = 12.3 \, ^{\circ}C$$

$$t_2 = t_1 + \Delta t = 20 \, ^{\circ}C + 12.3 \, ^{\circ}C = 32.3 \, ^{\circ}C$$

Members Made from Two Materials

$$\frac{3-68}{E_s = 9.74 \text{ in}^2 (APRA-9)}; A_c = (5.0 \text{ in})^2 = 25.0 \text{ in}^2$$

$$E_s = 30 \times 10^6 \text{ is}; E_c = 4.7 \times 10^6 \text{ ps}; (SEC Z-10)$$

$$LET O_c = O_{dc} = 1500 \text{ Ps}; THEN O_5 < O_{ds} = 21600 \text{ ps};$$

$$F = \frac{O_{dc}[AsEs + A_cE_c]}{E_c} = \frac{1500 \text{ Ps}; [(9.74)(30 \times 10^6) + 25(4.7 \times 10^6)]}{9.7 \times 10^6}$$

$$E_c = \frac{9.74 \times 10^6}{9.74 \times 10^6}$$

$$F = 130,800 \text{ LB}; CHECK O_5 = O_c = \frac{1500}{9.74} = 9575 \text{ ps};$$

$$\frac{3-69}{6} \quad \text{LET } O_{c} = 1500Psi \; ', \; O_{S} = O_{c} = \frac{E_{S}}{E_{c}} = 1500 \; \frac{30}{4.7} = 9575Psi \cdot \underline{OK}$$

$$\frac{F}{O_{c}} = \frac{A_{S}E_{S} + A_{C}E_{C}}{E_{C}} = \frac{A_{S}E_{S}}{E_{C}} + A_{C} = A_{S} = \frac{30}{4.7} + A_{C} = 6.38A_{S} + A_{C}$$

$$A_{S} = b^{2} - (b - 2t)^{2} = b^{2} - [b - 2(0.5)]^{2} = b^{2} - (b - 1)^{2} = b^{2} - b^{2} + 10 + 2b - 1$$

$$A_{C} = (b - 1)^{2} = b^{2} - 2b + 1$$

$$\frac{F}{\sigma_{c}} = 6.38[2b - 1] + b^{2} - 2b + 1 = b^{2} + 10.77b - 5.38$$

$$\frac{F}{\sigma_{c}} = \frac{500000}{1500} = 333.3 = b^{2} + 10.77b - 5.38$$

$$b^{2} + 10.77b - 338.7 = 0$$

$$BY \; \text{QUAD RATIC } EQN., \; b = 13.81M$$

3-71
$$W = m w = 2265 kg \cdot 9.81 m/s^{2} = 22.22 \times 10^{3} N^{2} \cdot As = 2.4e$$
 $1F Gs = 552 Mla / 2 = 276 Mla ; THEN GC = GS \cdot \frac{E_{c}}{E_{S}} = 226 \cdot \frac{134}{200} = /81 Mla$
 $GC_{ALLON} = \frac{5}{2} / 2 = 1000 / 2 = 500 Mla OK$
 $GC = \frac{PEc}{AsEs + AcEe} = \frac{PEc}{2AcEs + AcEe} = \frac{PEc}{AcC2Es + Ec}$
 $Ac = \frac{PEc}{GEC2Ec + Ec} = \frac{E2.22 \times 10^{3} N}{(18169a)} (2(200 + 131) Gla)$
 $D = \sqrt{\frac{44}{\pi}} = \sqrt{\frac{4(30.3)}{\pi}} = 6.20 mm = 41.8E OlA$

- 2) ADDITIONAL LOAD AVAILABLE: P2 = 350 KN-77. ZHAN=272.76 KN
- 3) BOTH MEMBERS DEFLECT THE SAME AMOUNT UNDER Pr $S_A = S_S : \frac{P_A \succeq_A}{E_A A_A} = \frac{P_S \succeq_A}{E_S A_S} \left(L A \circ L_S \right)$ $P_A = P_S \frac{E_A A_A}{E_S A_S} \circ P_S \frac{(69 GA)(1539 V Amm^2)}{(20) GP_A)(3600 mm^2)} = 1.425 P_S$

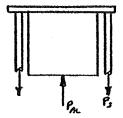
6IN SCH 40 1108: As = 5.581 IN 2 (25.4) Mm 2/IN) = 3600 Mm 2 0 - 0 - 0 = 272 71 811 APP A-12 (SI)

5) TO FAL LOAD ON ALUM: PA, " PI + PA = 77.24 + 160.28 = 237.52 kN

6) STRESSES!

$$S = \frac{Ps}{As} = \frac{1/2.48 \times 18 M}{3600 \text{ most}^2} = \frac{31.24 \text{ mPa}}{31.24 \text{ mPa}}$$
 $O_A = \frac{PAF}{AA} = \frac{Z^{31.52} \times 10^8 \text{ N}}{15.394 \text{ norm}^2} = \frac{15.43 \text{ mPa}}{15.43 \text{ mPa}}$

- 1) THE NUT MOVES 1.25 MM IN ONE TURN
- 2) THE FORCE CREATED CAUSES THE TUBE TO SHORTEN AND THE BOLTS TO GET LONGER. EAL + ES = 1.25 mm; AND LAL = LS
- 3) THE COMPRESSIVE FORCE IN THE TUBE EDVALS THE TENSILE FORCE IN THE BOLTS PAL "PS (ON ALL FOUR BOLTS)
- 4) AAL= TU (1502-1382) = 2714 mm As = 411 (102)/4 = 314 mm



6) STRESSES!

$$\sigma_{S} = \frac{P_{S}}{A_{S}} = \frac{134000 \, N}{314 \, \text{mM}^{2}} = \frac{427 \, \text{mpc}}{2714 \, \text{mm}}$$

$$\sigma_{AL} = \frac{P_{AL}}{A_{AL}} = \frac{134000 \, N}{2714 \, \text{mm}^{2}} = \frac{49.4 \, \text{mpc}}{49.4 \, \text{mpc}}$$

$$\sigma_{c} = \frac{PE_{c}}{AsEs + AcE_{c}} = \frac{(S0000 \text{ Lo})(2.7 \text{km}^{2} \text{Psi})}{(4.43 \text{lm}^{2})(27 \text{ km}^{2} \text{Psi})} = 320 \text{ Psi}$$

$$As = 4.43 \text{lm}^{2}; Ac = \pi(12)/4 - 4.43 = 108.7 \text{lm}^{2}$$

$$\sigma_{s} = \sigma_{c} \cdot \mathcal{E}_{e/E_{c}} = (320 \text{Psi})(29/2.7) = 3437 \text{ Psi}$$

$$No \ TE: E_{s} = 29 \times 10^{6} \text{ Psi} \ \text{For STAUCTURAL STEEL}$$

$$E_{c} = 2.7 \times 10^{6} \text{ Psi} \ \text{For Coh Crete with } S_{c}^{i} = 2000 \text{ poi}$$

$$RATED$$
(SEE SEc. 2-10)

3-76 tie Zo'c Li= 225,0 mm E FINAL = 205°C. ALVM 6061-TY, Sy=110MPa. a) TEMP. AT WHICH BAR TOUCHES PLATE 8=0,50 mm = &L(BE) Dt, = \frac{8}{\alpha L} = \frac{0.50mm}{(23.4 \tau 10 \cdot 2-1)(225,0mm)} = 95.0 \cdot C tz=t, +At= 20+95= 115°C NOSTRAIN AT THIS TEMP. b) ADDITIONAL Stz = 265°C - 115°C = 90.0°C REGURAINED. 0= E & (st) = (69 x/09 Pa)(23.4x106 2-1)(90.02) O = 145 × 106 Pa = 145 MPa > SY MATERIAL WOULD YIELD-FAILURE

COMPRESSION 3-77 (a) t,=20°C. L,= 2.400 m, ALUM. 2014- T4, L2=2.405 m 8= Lz-L1 = 2.405-2.400 = 0.005m = 5.00 mm = d L (AG) $\Delta t_1 = \frac{8}{4L_1} = \frac{0.008 m}{(23.0 \times 10^{-6} \text{ °C}^{-1})(2.400 m)} = 90.6 \text{ °C}$ $t_2 = t_1 + \Delta t_1 = 20 + 90.6 = 1/0.6 \text{ °C}$ (b) INCREASE 30°C. t3= 110.6°C +30=140.6°C RESTRAINED. 0= Ed &tz = \$3 x109 Pa)(23.0x1064-1)(3006) 0 = 50.4 × 10 6 Pa = 50.4 MPa COMPRESSION (C) Sy = 290 MPa FOR ZO14-T4, SAFE AGAINST YIELDING. BUT BUCKLING SHOULD BE CHECKED. 8 max = 0.50 mm. REPEATED AXIAL TENSILE LOAD. SPECIFY MAX. PERMISSIBLE LOAD. 4140 OOT 1300. E= 207 GPA a) DEFORMATION: $\xi = \frac{FL}{FA}$. THEN $F_{MAX} = \frac{SEA}{L}$ $A = 30 \times 20 = 600 \text{ m m}^{2}, L = 700 \text{ m m}$ $F_{MAX} = \frac{6.50 \text{ m/m} \times 207 \times 10^{9} \text{ N}}{(700 \text{ m/m})} \frac{100^{2}}{(10^{3} \text{ m/m})^{2}} \frac{100^{2}}{(10^{3} \text{ m/m})^{2}}$ FMAX = 88.7 X 103 N = 88.7 RN (b) STRESS', Od = SM/8 = 814MON/8 = 101.8MPa = F/A

> FMAX = Od · A = (101.8 N/mm²) (600 mm²) = 61000 N = 61.0 kN STRESS GOVERNS THE DESIGN. FMAX = 61.0 kN

FORCE ANALYSIS. m= 4200 kg. W=m q= (4200 hg)(9,81m/s)=41200N=41.2kH

VECTOR TRIANGE IS A RIGHT TRIANGLE,

STRESS:
$$P = 10.0 \text{ mm}$$
; $A = \pi p_{yy}^{2} = 78.54 \text{ mm}^{2}$
 $O = \frac{F}{A} = \frac{AB}{A} = \frac{33.75 \times 10^{3} \text{M}}{78.54 \text{ mm}^{2}} = 429.7 \text{ MPa}$

ASSUME STATICLOAD, Od = SV/Z

REO'D Sy = 20 = 2 (429.7 M/a) = 859 M/a.

SPECIFY AISI 4140 OQT 1100, 84= 903 MPA

DEFORMATINE

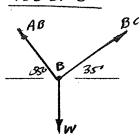
$$S_{AB} = \frac{(AB)L_1}{EA}$$
; $S_{BC} = \frac{(BC)(L_2)}{EA}$

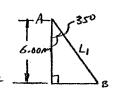
$$L_{1} = \frac{6.00 \, \text{m/cos 35} = 7.32 \, \text{m}}{63.75 \times 10^{3} \, \text{N}) (7.32 \, \text{m})} \times \frac{(10^{3} \, \text{m/m})^{2}}{(207 \times 10^{9} \, \text{N/m}^{2}) (78.54 \, \text{mm}^{2})} \times \frac{(10^{3} \, \text{m/m})^{2}}{m^{2}}$$

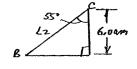
$$\delta_{BC} = \frac{(BC)Lz}{EA} = \frac{(23.63 \text{ NO}^3 \text{ N})(10.46 \text{ m})}{(207 \times 10^9 \text{ N/m}^2)(79.54 \text{ m/m}^2)} \times \frac{(10^3 \text{ m/m})^2}{m^2}$$

$$\left[Lz = 6.00 \text{ m/cos 55}^4 = 10.46 \text{ m}\right]$$

FBD OF B







3-82 AISI 1040 CD, Sy = B2KSi. LET $\sigma = 0.9 Sy = 73.8KSi = \frac{F}{A}$ L = 2.00 IN i $A = \frac{ITD^2}{4} = \frac{IT(0.50S/N)}{4} = 0.200 IN^2$ $E = 30 \times 10^6 PSi = 30 \times 10^3 KSi$ $S = \frac{FL}{EA} = \frac{CL}{E} = \frac{0.3.8 KSi}{30 \times 10^3 KSi} = 0.00492 IN = 8$ $STRAIN = \frac{8}{L} = 0.00492 IN/2.00 IA = 0.00246 IN/M. = 6$ $F = C \cdot A = (73.8 \times 10^3 LB/IN^2)(0.200 IN^2) = 14760 LB = F$ DISTANCE BETWEEN GASE MARICS = 2.00 IN FS = 2.00049 IN

PROBLEMS 83-90 FOLLOW SIMILAR SOLUTION PRICEDURE.
RESULTS SUMMARIZEDON FOLLOWING PAGE.

NYLON 66 PLASTIC. TENSILE STRENGTH = S_{M} = 83 MPa LET $G = 0.5 S_{M} = 0.5 (83 MPa) = 41.5 MPa$ L = 50 m m. $A = t.W = (12.5 mm)(16.0 mm) = 200 mm^{2}$ $E = 2900 MPa = 2900 M/mm^{2}$ $S = \frac{FL}{EA} = \frac{GL}{E} = \frac{(41.5 mPa)(50 mm)}{2900 MPa} = 0.7155 mm = S$ $STRAIN = E = \frac{8}{L} = 0.7155 mm/somm = 0.0143 mm/mm = E$ $F = 0.A = (41.5 N/mm^{2})(200 mm^{2}) = 8300 N = 8.30 RN = F$ DISTANCE BETWEEN GAGE MARKS = 50 mm + $S = S_{M} =$

PROBLEMS 92-99 FOLLOW SIMILAR SOLUTION PROCEDURE.

RESULTS SUMMARIZED ON FOLLOWING PAGE.

NOTEL DATA FROM TABLE 2-13 FOR PROBLEMS 96-99 REQUIRE

CONNERSIONS AS SHOWN IN LOWER TABLE ON FOLLOWING PAGE.

SOLUTIONS TO PROBLEMS 3-82 TO 3-90 Metals										
Prob.	Material	s _y	0.9*s _y	E	L.,	A	Elong.	Length betw. gage	Strain	Force
No.		(ksi)	(ksi)	(ksi)	(in)	(in²)	(in)	marks (in)	(in/in)	(lb)
	AISI 1040 CD	82	73.8	30000	2.000	0.200	0.00492	2.0049	0.00246	14760
3-83	AISI 5160 OQT 700	238	214	30000	2.000	0.200	0.01428	2.0143	0.00714	42840
	AISI 501 OQT 1000	135	122	29000	2.000	0.200	0.00838	2.0084	0.00419	24300
	C17200 Ber. Copper, hard	145	131	19000	2.000	0.200	0.01374	2.0137	0.00687	26100
3-86	Magnesium AZ63A-T6	19	17.1	6500	2.000	0.200	0.00526	2.0053	0.00263	3420
3-87	Zinc ZA 12	47	42.3	12000	2.000	0.200	0.00705	2.0071	0.00353	8460
3-88	Steel ASTM A572 Gr 65	65	58.5	29000	2.000	0.200	0.00403	2.0040	0.00202	11700
3-89	ADI Grade 4	155	140	24000	2.000	0.200	0.01163	2.0116	0.00581	27900
3-90	Aluminum 5154-H38	39	35.1	10200	2.000	0.200	0.00688	2.0069	0.00344	7020

SOLUTIONS TO PROBLEMS 3-91 to 3-101					Plastics and Composites						
Prob.	B#-4		Length							Mary and the Control of the Control	
l	Material	Su	0.5*s _ս	E	L	Α	Elong.	betw. gage	Strain	Force	
No.		MPa	MPa	MPa	(mm)	(mm²)	(mm)	marks (mm)	(mm/mm)	(kN)	
3-91	Nylon 66, dry ⁺	83	41.5	2900	50.0	200	0.71552	50.716	0.01431	8.30	
3-92	ABS, high impact [⁺]	34	17	1720	50.0	200	0.49419	50.494	0.00988	3.40	
3-93	Acetal copolymer ⁺	55	27.5	2830	50.0	200	0.48587	50.486	0.00972	5.50	
3-94	Polyurethane elastomer [⁺]	34	17	690	50.0	200	1.23188	51.232	0.02464	3.40	
3-95	Phenolic [⁺]	45	22.5	7580	50.0	200	0.14842	50.148	0.00297	4.50	
3-96	Glass/epoxy composite#	786	393	27580	50.0	200	0.71250	50.713	0.01425	78.6	
3-97	Aramid/epoxy composite [#]	1379	690	75845	50.0	200	0.45455	50.455	0.00909	137.9	
3-98	Graphite/epoxy, High s _u #	1917	958	135832	50.0	200	0.35279	50.353	0.00706	191.7	
3-99	Graphite/epoxy, High E#	1103	552	330960	50.0	200	0.08333	50.083	0.00167	110.3	
+	From Appendix A20						0.0000	00.003	0.00107	110.3	

Pro	Problems 3-96 to 3-99: Data conversion of units										
Prob. No.		s _u ksi	s _u MPa	E ksi	E MPa						
3-96	Glass/epoxy composite	114	786	4000	27580						
	Aramid/epoxy composite	200	1379	11000	75845						
	Graphite/epoxy, High s _u	278	1917	19700	135832						
3-99	Graphite/epoxy, High E	160	1103	48000	330960						

Stress Concentrations for Direct Axial Stresses

- 3-100 D=40.0mm, dg=35.0mm, L=3.0mm, F=46RN=46000N

 D/dg=40/35=1.14; N/dg=3.0/35=0.086; Kt=2.3 APP. A 22-1

 ONOM= F Trdg/4 = 46000N

 Tr(35)2/4 mm² = 47.8 MPa; OMAX=Kt ONOM=(2.3) 47.8=110MPa
- 3-101 D=1.50 in, dg=1.25 in, h=0.12 in, F= 10300 LB

 D/dg=1.50/1.25=1.20; h/dg=0.12/1.25=0.096, Kt=2.40 APP. AZZ-1

 Onon= F 10300 LB 8393 Psi; Onax= Kt Onon= 2.40(8393)= 20 140 Psi
- $\frac{3-102}{D} D = 0.40 \text{ in } dg = 0.35 \text{ in } R = 0.040 \text{ in } F = 1250 \text{ lb} \quad use APP. A22-1$ $\frac{D}{dg} = 0.40 / 0.35 = 1.14; \frac{h}{dg} = 0.04 / 0.35 = 0.114; \quad Ke = 2.05$ $\frac{C_{N0M}}{T dg^{2}/4} = \frac{1250 \text{ lb}}{T (0.35)^{2}/4} = 12990 \text{ Pei}; \frac{C_{N0M}}{T (0.35)^{2}/4} = \frac{1250 \text{ lb}}{T (0.35)^{2}/4} = \frac{1250 \text{ lb}}{T$
- 3-103 D=10.0 mm, dq=8.6 mm, h=1-20mm, F=5500 N USE APP. AZZ-1

 D/dq=10/8=1.25; M/g=1.2/8=0.15; Kt=2.05; ONOM= /Hdg/4

 ONOM= 5500 N

 T(8) 1/4 mm² = 109.4 MPa; OMAX = Kt ONOM = 2.05(109.4) = 224 MPa
- 3-104 H = 2.50/N, N=2.20/N, N=0.25/2=0.125/N, F=17,500 LB USE APPA-22-3

 H/h=2.50/2.20 = 1.14; N/h = 0.125/2.20 = 0.057; ONOM = 1/th; t=0.400/N; Kt=1.96

 ONOM= 17500 LB
 (0.40 X 2.20) N = 19886PSi; OMAX = Kt ONOM = (1.96)(19886) = 38 980 PSi
- 3-105 H = 60 mm, h = 55 mm, t = 10 mm, h = 6/2 = 3.0 mm, F = 75 kN, USE ARR. ADD-3

 H/h = 60/55 = 1.09; 12/h = 3/55 = 0.055; Kt = 1.75; ONON = F/th

 ONON = 75000 N
 (10)(55) mm = 136.4 MPa; OMAX = Kt ONON=(1.75)(136.4) = 239 MPa
- 3-106 H=25 mm, h=22 mm, t=3.0 mm, h=5/2=2.5 mm, F=6800N USE APPAZZ-3 H/h=25/22=1.14, h/h=2.5/22=0.114, Ke=1.67; Omen=F/th ONON=6800N = 103.0 MPa; Omax=Kt Onon=(1.67)/03=172 MPa
- $\frac{3-107}{H} = 0.80 \text{ in }; h = 0.50 \text{ in }; h = 0.7/2 = 0.10 \text{ in }; t = 0.12 \text{ in }, F = 1800 \text{ lb}, USG APP. A22-3}$ $\frac{3-107}{H/n} = 0.80/0.50 = 1.60; h/n = 0.10/0.50 = 0.20; k + = 1.76; \sigma_{nom} = F/th$ $\sigma_{nom} = \frac{1800 \text{ lb}}{(0.12)(0.50)} = 30000 \text{ si}; \sigma_{max} = k_t \sigma_{nom} = (1.76)(30000) = 52.800 \text{ psi}$
- 3-108 D=50 mm, d=40 mm, r=6.0 mm, F= Z30 kN= Z30 000 N, USEAPPA 22-2 D/J=50/40=1.25; h/J=6/40=0.15; Kt=1.65; OTHER = F/1107/4 OTHER = Z30 000 N T(40)8/4 mm² = 183 MPa; OTHER = (1.65)(183)=302 MPA

- 3-109 D=2.50 IN, d=1.75 IN, L=0.25 IN, F=4BK=48000 LB, USEAPPAZZ-Z

 D/J=2.55/1.75=1.43; 12/3=0.25/1.75=0.143; Kt=1.66; ONOM= F/H d2/4

 ONOM= 48000 LB

 H(1.75) 1/4 IN2 = 19956P3; OMAX=Kt ONOM= (1.66)(19956)= 33127P3;
- 3-110 D=0.38 IN, d=0.32 IN, L=0.02 IN, F=375LB USE APP. A22-2.

 D/d=0.38/0.32=1.19; h/d=0.02/0.32=0.063; Kt=1.91 ONOM= F/1732/4

 ONOM= 375 LB

 T(0.32)2/4 IN2=4663 PSi; ONAX=Kt ONOM=(1.91)(4663)=8906 PSi
- 3-111 D=10.0 mm, d=8.0 mm, 12=0.50 mm, F=1600 N, USE APR. A22-2

 D/d=10/8=1.25; 12/d=0.5/8=0.063; Kt=2.00; ONOM=1/HJ2/4

 ONOM=1600N = 21.83 MBa; OMAX=KtONOM=(2.00)(31-83)=63.7 MPa
- $\frac{3-1/2}{4/w} = 2.50 \text{ IN}, t = 0.400 \text{ IN}, d = 1.75 \text{ IN}, F = 14200 LB. USE APPAZZ-4}$ $\frac{d}{w} = 1.75/2.50 = 0.70; K_t = 2.05, O_{NOM} = F(w-d)t \frac{CURVE A}{(2.50-1.75)(0.4)} = 47323 PSi; O_{MAX} = K_t O_{NOM} = (2.05)(47333) = 97.030 PSi$
- $\frac{3-1/3}{4/w} = 60 mm, t = 8.00 mm, d = 40 mm, F = 65 kN, USE APP A22-4, CURVEA$ $\frac{3-1/3}{4/w} = \frac{40}{60} = 0.67; Kt = 2.05; O_{NOM} = \frac{F}{(w-d)} t = \frac{65000N}{(60-40)(8)} = 406 MPa$ $O_{MAX} = Kt O_{NOM} = (2.05)(406) = 833 MPa$
- $\frac{3-114}{d/w} = 18 mm$, t=2.50 mm, d=8.00 mm, F=2250 M USE APP. 22-4, CURVE A d/w=8/18=0.444; Kt=2.20; $O_{NOM}=F/(w-d)t=\frac{2250 N}{(8-8)(7.5)}=90.0 mPa$ $O_{MAX}=Kt$ $O_{MOM}=(2.20)(90)=198 MPa$
- $\frac{3-115}{4} \quad w = 0.60 \text{IN}, \quad t = 0.088 \text{IN}, \quad d = 0.25 \text{IN}, \quad F = 475 \text{LB} \quad \text{USE APP.22-4, CURVEA}$ $\frac{3-115}{4} \quad w = 0.25/0.60 = 0.417; \quad \text{Ke} = 2.22; \quad \sigma_{\text{Nom}} = \frac{7}{4} \quad \text{We} = \frac{475 \text{LB}}{(0.4 0.25)(0.188)} = 15,422 \text{Bs};$ $\frac{\sigma_{\text{MAX}}}{\sigma_{\text{Nom}}} = \frac{15}{4} \quad \text{We} =$
- $\frac{3-1/6}{d/0} = 50 \text{ mm}, d = 20 \text{ mm}, F = 120 \text{ NN} = 120,000 \text{ N} \quad \text{USE APP. A 22-5, CURVE A}$ $d/0 = 20/50 = 0.40; Kt_g = 5.0; O_{NOM} = \frac{120000N}{T(50)^{2}/4} = 61.1 \text{ MPa}$ $O_{MAX} = Kt O_{NOM} = (5.0)(6/.1) = 306 \text{ MPa}$
- 3-117 D=2.001N,d=0.751N, F=22500 B., USE APP. A22-5, CURVE A

 d/D=0.75/2.00=0.375; Ktg=4.75; ONON=F/HDB/N=22500 LB = 7162 PS;

 OMAX=Ke ONON=(4.75)(7162)=34020 PS;

- $\frac{3-118}{d/o = 0.63 \text{ in, } d = 0.35 \text{ in, } F = 2800 \text{ LB, } USE APP. A22-5, CURVE A}{d/o = 0.35/0.63 = 0.556 \text{ j. Ktg.} = 6.95 \text{ of } \frac{F}{\pi 0^2/4} = \frac{2800 \text{ LB}}{\pi (0.63)^2/4} = 8982 \text{ PS} \text{ i}$ $O_{MAX} = Ke O_{Nom} = (6.95)(8982) = 62425 \text{ es} \text{ i}$
- $\frac{3-1/9}{3-1/9} D = 12 mm d = 7.25 mm F = 7500N USE APP. A22-5, CURVE A$ $\frac{3}{10} = \frac{7.25}{12} = 0.604; Kt = 8.00; \sigma_{Nom} = \frac{F}{\pi 0^2/4} = \frac{7500N}{\pi (12)^2/4} = 66.3 MPa$ $\frac{\sigma_{MAX} = Kt \sigma_{Nom} = (8.00)(66.3) = 531 MPa}{100}$
- $\frac{3-120}{LET \ O_{MAX}} = 25000 \ N, REPEATED, AISI 4140 OQT 1100 STEEL, SN = 1014 MPG.$ $LET \ O_{MAX} = O_{d} = \frac{S_{M/N}}{NN} \ THEN \ N = \frac{S_{M/O_{MAX}}}{N} = \frac{F}{MOLE!} \frac{d}{d} = \frac{10}{2} =$
- 3-121 USE APP. A22-2. D=9mm; d=6mm, r=0.50mm, D/d=9/6=1.50, r/d=0.5/6=0.83 Kt=1.95; Omax=Kt Onon=1.95 900 N T(6)=1/9 = 62.1 MPa
- 3-122 F=36kN=36000N, USE APP. A22-2, D=85mm, d=75mm, h=3.0mm

 P/d=85/75=1.13; A/d=3/75=0.04; Ke=1.95; ONOM=Frd=1/4

 OMAX=KE ONOM=1.95 36000N

 TT(75) 7/4mm= 15.9 MPa
- 3-123

 HOLE: D = 1.06 IN; $d = \alpha = 0.50 IN$; d = 0.50; K = 6.1 APR AD2-5 $O_{MAX} = Ke O_{q} = 6.1 \frac{F}{\pi D^{2}/4} = \frac{6.1F}{\pi (1.0)^{2}/4} = 7.77 F$ FILLET | STED: LET K = 1.70; $O \leq 7.77 F = K + F/A$; $REQ'D A = \frac{KeF}{7.77F} = \frac{1.7F}{7.77F} = 0.219 IN^{2} = 9 + d^{2}/4$ $d = \sqrt{\frac{4A}{\pi}} = \sqrt{\frac{4(0.219 IN^{2})}{17}} = 0.528 IN SPECIFY$ THEN D/d = 1.00/0.528 = 1.89 AND $K = 1.7 \implies N/d = 0.17$ THEN $\Delta = 0.17 d = 0.17 (0.528) = 0.090 IN SPECIFY$
- 3-124

 F = 8.25 RN REPERTED. CASE B-SPECIFY MATERIAL.

 Omax = ke Onom = ke · F = ke 8.25 x/03 N = ke(21.7MPa)

 APP A21-1: h/dg = 4.0 mm/22 mm = 0.182; b/dg = 30/22 = 1.36:ke=1.65

 Omax = ke · Omon = 1.65(21.7MPa) = 35.8 mPa

 LET Omax = Od = 5 n/B, REOD Sn = 8 Od = 8(35.8MPa) = 286 MPa

 SPECIFY ALUMINUM 60 61-T6. Sn = 310 MPa, 17 40 ELONG. OR ANY STEEL

2-125

FIGURE P3-125 AISI 1141 OQT 1100, SM = BOOMPA, Od = SM/B REPEMBED LAND,

Omin KE F/A. FALLOW = OBA/KE

MIDDLE SECTION! A = (100MM) (6 mm) = 60 mm. M = 1.5 mm = 0.15

APP, A22-3, N/h = 16 mm/10mm = 1.60. KE = 1.90

FALLOW = OB. A = (100N/mm²) (60mm²) = 3158 N

AT PIN: APP, A22-4! CURVEB o. M = 16 mm, d = 6 mm, d = 6 = 0.375

KE = 3.15. A = (M-d) t = (16-6) (6) = 60 mm²

FALLOW = OB. A = (100N/mm²) (60 mm²) = 1967 N = FALOGU

3.15

SPECIFY MATERIAL. O = KEF/A. OB = SM/12 SHOCK

AT HOLE: APP A22-5 CURVEA. 4/D = 13/20 = 0.40. KE = 5.0

A = MD² = M(30mm²) = 707 mm² GROSS AREA

LET OMAX = OB = SM = KEF A REQ.D SW = 12 KEF = 12 (50) (12.6 KB²N)

PEOD. SM = 1070 MPA

AT FILLET: APP A22-2. N/B = 12 KEF = 12 (50) (12.6 KB²N)

REQ.D. SM = 170 MPA

AT FILLET: APP A22-2. N/B = 12 (18 mm²) = 254 mm²

REQ.D. SM = 17 KEF = 17 (18 mm²) = 254 mm²

STRESS AT FILLET GOVERNS: SM = 128 MPA2 STOEDNEADON

SPECIFY: AISI 4140 OQT 900. SM = 1289 MPA2 STOEDNEADON

Bearing Stress

3-127

A) W6x15 ON STEEL PLATE & A6 4.43 IN (APP. A-7)

08 = F/A8 = 26000 LB/443 112 = 5869 PSI

- B) STEEL PLATE ON CONCRETE: Ab=(12) = 144 111 = 151 | 151
- C) CONCRETE PIER ON CONCRETE FOOTING & AG=(B) = 324 M2

 CG = F/AD = 26000 LB/324 M2 = 80.2 PSi
- D) CONCRETE FOOTING ON SOIL? A6=(36)2= 1296 IN2
 (66= F/A6 = 26000 LB/1296 IN2=20.1951

3-128

- a) PIPE ON FLOOR: A = \$\frac{\pi}{4}(2.375^2-2.067^2)=1.075112^2 \sigma_6 = \frac{\pi}{A_6} = \frac{2350L8}{1.075 m^2} = \frac{2181 \pi_5}{2181 \pi_5} \quad \text{(APP. A-12)}
- b) 2.375 IN DIA-ROUND PLATE : A = 2.375 (4) = 4.43 IN2 03 = F/A = 2350 L8/4,430 IN2 = 530 PS/

- 3-129
- a) BOLT HEAD ON WASHER: $A_b = A_{Hex} A_{Z0}$ (See APP. A-1) $A_b = 0.866(0.75)^2 \pi(0.562)^2/\gamma = 0.739 \text{ M}^2$ $C_b = F/A_b = 385 LB/0.239 \text{ M}^2 = 1610 PSi$
 - b) WASHER ON WOOD: Ab = \$ (1.3752-0.562) =1.237112 Ob = \$ |Ab = 385LB/1,237112 = 31105/
- 3-/30 DATA FROM PROB. /-64: F=8000LB, L=2.25IN, h=0.375IN.

 06= F/Ab = 8000LB/(2.25)(0.375/2)IN2 = 18 963 PSi
- 3-131 DATA FROM PROB. 1-65: F=20 000 LB, F16. P1-65
 - a) PIN/TUBE & A6 = Dp (0-1) = (0.50) (1.25-0.875) = 0.1875 IN.2 06 = F/A6 = 20000 LB/0.1875, N2 = 106 700 PSi (VERY HIGH)
 - b) COLLAR/TUBE: Ab = \$\frac{4}{7}(0^2-d^2) = \frac{4}{7}(1.25^2-0.875^2) = 0.626/N^2

 Ob = \frac{F}{Ab} = \frac{20000}{0.626} \ldots \frac{2}{10^2-d^2} = \frac{4}{7}(1.25^2-0.875^2) = 0.626/N^2
- $\frac{3-/32}{\sigma_b} = F(a_b = 10.2 \times 10^3 \text{ M/360 mm}^2 = 28.3 \text{ M/0.}$
- 3-133 FROM FIG. P1-71
 - a) ON MIDDLE PART: Ab = 2 dt, =(2)(12)(15)=360 mm² = 01 = F/Ab = 10.2 ×103N/360 mm² = 28.3 MPa
 - b) ON OUTER PARTS: Ab = 4 dt = (4)(12)(10) = 480 mm²

 Ob = F/Ab = 10.2 ×10²N/480 mm² = 21.25 MPa
- $\frac{3-134}{\sigma_{b}=\sqrt{4}} F14. P3-134: A_{b}=\sqrt{0} \times (6) + \frac{1}{2} \left(\frac{1}{4}\right) \left(10\right)^{2} = 99.3 \, \text{mm}^{2}$ $\sigma_{b}=\sqrt{4} = \frac{535 \, \text{N}}{99.3 \, \text{mm}^{2}} = \frac{5.39 \, \text{MPa}}{2}$
- 3-135 W= 90 kN TOTAL; 45kN ON TWO LEGS; 22.5 kN ON EACH LEG

 a) STER PLATE: OF = 22.5 x 10 N (0.10 m) = 2.25 MPL

 (0.10 m) = 2.25 MPL

 FOR A36 STEEL: ON = 0.95; = 0.9(248 MPL) = 223 MPL

 OL
 - b) TOP OF CONCRETE: $A_b = 2 (0.20m)^{\frac{1}{2}} 0.080 \, m^2 (TWO LEGS)$ $O_b = \frac{45 \times 10^3 N}{0.08 \, m^2} = 0.563 \, MPA$

(CONTINUED)

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3-135 (CONTINUED)
                    RONCRETE: 2000 PSi = 2.0KSi x 6.395 MPa/A;= 13.79 MPa= fc'
       (TABLE 3-6) - 4 = 0.34 ft An/A, = 0.34 U3.79AMA) 0.30 = 9.08MPA OK
                C) SOIL! OF = 45 x103 N = 22.5 kPa
                    ON COMPACT GRAVEL OD = 380 APA OK (TABLE 3-7)
        ON SOFT ROCK: OW = 480 KPA = 480 KB N/m2
                                                  (TABLE 3-7)
        REGO. A = P = 160 x103 N = 0.333 m2 = 52
         RED'D. SIDE DIMENSION 1 5 = 0.571 MM
3-137.
        Ra = (5y-13) (0.03dl) = (66-13)(0.03)(3.00)(16.0) = 33.1 kies
                                                  -(EQ. 3-23)
       Ra= (46-13) $0,03)(3.00)(16.0) = 475 KIBS
3-139 a) Ra = (36-13) (0.03) (5.00) (8.00) = 27.6 Kirs
       b) Ra= (46-13)(0.05)(5.00)(8.00) = 39.6 xies
3-140 LOAD ON EACH FOOT = F = 10 0 00/4 = 2500 LB
        Ab= 1-51 IN2 (TABLE A-9 2x2x14)
        Ob = F/Ab = 2500 LB/1.51 IN2 = 1656 PSi
        REOD A = F/OL = 2500/400 = 6.25 IN? USE SQUARE PLATE
        SIDE = VAL = V6.25 IN2 = 2.50 IN
3-141 ALLOWABLE REACTION = Ra FROM EQ. 3-23.
        Ra= (5y-13) (0.03)(d)(1)
                                     U.S. CUSTOMARY UNITS
          Sy = 36 KS1
          d = 2 (200mm) (1.01N/25.4mm) = 15.75 IN.
          L= (150mm)(1.011/25.4mm) = 5.91 14.
         Ra = (36-17) · (0.03 1(15.75)(5.91) = 64.2 kies
         Ra = (64.2 KIRS) (4.448 RN/KIR) = 285 MN
```

OR-USING EQ 3.24 FORSE UNITS

Sv= 248 MPa

d=21=2(200 mm)= 400 mm, L= 150 mm

Ra = (248-90)(3.0×10-5)(400)(150) = 284 RN

36

$$\frac{3-142}{O_b} = \frac{F_b}{A_b} \cdot F_b = 28500 \, \text{M/4 LEAS} = 7/25 \, \text{M/LEGA} \cdot A = 1.44 \, \text{IN}^2$$

$$O_b = 7/25 \, \text{M/1.44 IN}^2 = 4948 \, \text{psi} = 06$$

3-143 CONCRETE FLOOR.
$$f_c = 3000 psi$$
, $O_{bd} = 0.34 f_c /A_1$,

BUT $O_{bd}_{MAX} = 0.68 f_c / BECAUSE Ar/A_1 > 74$. $F_b = 7125 ll$.

 $O_{bd} = 0.68 (3000) = 2040 psi = F_0/A_b$. $REQ'O Ab = F_0/O_{bd}$
 $A_{bm,N} = 7125 ll/2040 l/m^2 = 3.49 lN^2 \frac{3}{1000}$

TRIANGULAR AREA: $A = \frac{1}{2}(3)(3) = 4.50 lN^2$

WED PAD TO BOTTOM OF EACHLEG.

$$\frac{3-144}{A_b} = (3.50)(7.50) = 26.25 IN^2, F_b = O_{bb}A_b \cdot O_{bd} = 55 \rho si$$

$$F_b = (55 M/_{IN^2})(26.25 IN^2) = 1444 M = F_b ALLOWABLE$$

$$\frac{3-145}{0}$$
 4-IN SCH. 40 PIRE, $A_b = 3,1741N^2$, $O_{bd} = 0.68 \, \S_c^i$ OH LARGE FLOOR

 $O_{bd} = 0.68 \, (4000 \, psi) = 2720 \, psi$
 $F_b = O_{bd} \cdot A_b = \left(2.720 \, M/N^2 \right) \left(3.1741N^2 \right) = 8633 \, M = F_b \, ALLOWABLE$

3-146 DATA FROM PROB 3-145
$$O_{bd} = 2720 \text{ psi} = Fb/Ab$$
 $F_b = 10(8633 \text{ ll}) = 86,330 \text{ ll}$
 $REQD. A_b = Fb/O_{bd} = 86330 \text{ ll}$
 2720 ll/m^2
 $TRY SQUARE PLATE: A_b = b^2$.

 $D_{min} = TA_{bmin} = \sqrt{31.74} \text{ in}^2 = 5.63 \text{ ln}$
 $USE b = 6,0 \text{ in} SQUARE PLATE:$

Direct Shear Stress

$$\frac{3-147}{REO'O} P = F/A_3 = F/(8/H)(A)_3' LETT = T_3 = 6000PS_1'$$

$$REO'O A = \frac{F}{(8/H)(T_3')} = \frac{2/000L8}{(8/H)(6000L8/H)^2} = 0.438/H$$

- 3-149 FROM PROB. 1-59: F= 23695 N; T= 151 MPa. ON PIN.

 LET T= Tj = Sy = 151 MPa. "REGIO. Sy " BT = B(151) = 1708 MPa.

 POSSIBLE STEEL: A15/4/40 OUT 100, Sy=1462 MPa; 12% ELONG.
- 3-150 As=(\pio)(t)= 11(70)(0) mm = 503 mm =

 T = Sus = 0.82 Su = 0.82(448mp) = 361mp = 367 N/mm =

 REGO. F = T: As = 361 N . 503 mm = 185 kN
- 3-15) T= SAS = 165 MPA GIVEN IN APP. ATT

 REGO. F= T:As = 165 M. . 503 MART = 83 RN
- 3-152 7=5Ms = 0.90 5M = 0.90 (331MA) = 298 MPa COPPER RED'D, F = T. As = 298N, . 563 mm = 150 KH
- 3-153 T=SMS = 0.82 SM = 0.82 (bZIMPA) = 509 MPA REO'D, F = T.As = SO9 N . 503 MM2 = 256 KN
- 3-154 F= T.As: LET TE SMS = 0.82 SM = 0.82(448MA)=367MA.

 As = [2(35mm) + IT(8mm)][5:0 mm] = 476 mm

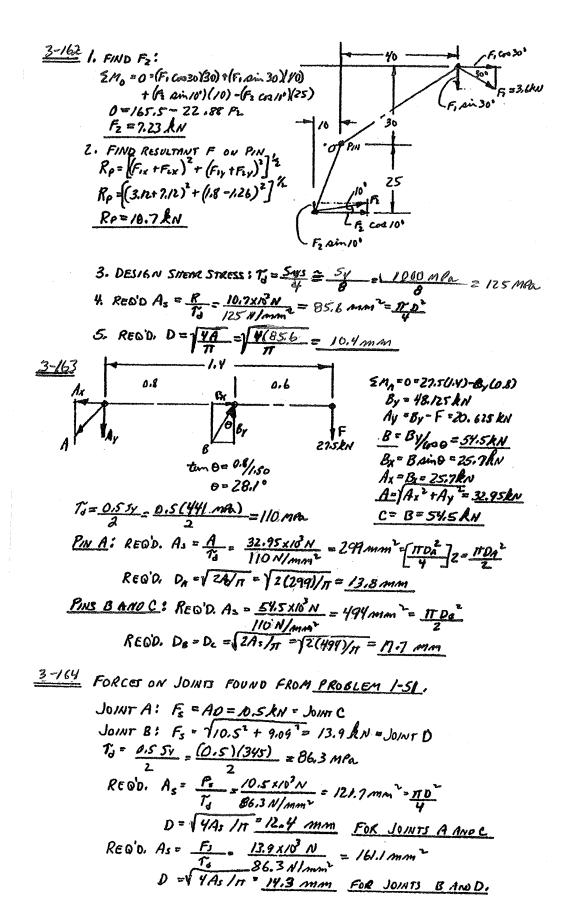
 F = (361 N/mm) 1476 mm²) =175 KN
- 3-155 F. TiAs: LET To Sus = 16KS; (FROM AM. A-19)

 As = 1.144 M2 (SEE PROB. 1-62)

 F = (16 000 LB/M)(1.144/M2) = 18 300 LB
- 3-156 As = B.S.IA)(3.0 IN) = ID.S.IN?

 T' = F = 1800 LB = 171 PSi (WASAFE)

 MAXIMUM ALLUWABLE SHEAR STRESS LISTED IN TABLE A-19 IS 95851.
- 3-157 F= T'As: LET T= Sus = 0.82 Su = 0.82 (97000 PSi)=7.9 540 PSi F = T'As = (79540 18/10) (7.5/N · 0.105/N) = 62 650 LB
- 3-158 LET T = 5m3 = 0.82 (SA) = 0.82)(263 000 PSi) = 215 660 PSi F = T.As = (215 660 LB/IN) (7.5.0.105) IN = 169 800 LB
- 3-159 LET T = SAS = 0.82 SA = 0.82 (185 00051) = 151 700 05; F = T.A. = (151 700 LB/IN) (7.5.0.105) IN2 = 119 500 LB
- 3-160 C36000 BMSS: LET T= Sm. = 0.9 (70000 P3i) = 63000 P3i F= T.A. = (63000 LB/N) (7.5.0.105) N° = 49,600 LB
- 3-161 ALUM. 5154. H32: LET T = Sus = 152 000 PS 1 F = T. As = (152 000 LB/A) (7.5.0.105) IN = 119 700 LB



$$\frac{3.165}{2M_{W}} = 53 \cos 20^{\circ} = 46.8 \text{ M.}$$

$$\frac{2M_{W}}{6} = 0 = 280(46.8) - F_{L}(6)$$

$$F_{L} = 2/88 \text{ LB}$$

$$\frac{2M_{L}}{6} = 280(52.8) - R_{W}(6)$$

$$R_{W} = 2468 \text{ LB}$$

$$\frac{2468 \text{ LB}}{48} = \frac{2468 \text{ LB}}{28018} = \frac{6275 \text{ RSi}}{15 \text{ IN DOUBLE SHEAR}}$$

- $\frac{3-166}{A=p.t.} = \sum_{i=1}^{n} A = \sum_{i=1}^{n} A_{i} A_{i} + \sum_{i=1}^{n} A_{i} + \sum_{$
- 3-161 IMPACT: $T_3 = \frac{S_{Y^2}}{12} = \frac{90 \, \text{KSi}}{12} = 7.50 \, \text{KSi} = 7500 \, \text{GSi}$ $A_5 = 2 \, \pi 0^2 / y = \pi 0^2 / 2$ $REOD. A_5 = \frac{500 \, \text{LB}}{7500 \, \text{LB} / \text{M}^2} = 0.0667 \, \text{M}^2 = \pi 0^2 / 2$ $REOD. D = \sqrt{\frac{2A_5}{H}} = \sqrt{\frac{2(0.0667)}{10.0667}} = 0.706 \, \text{M}^2 \cdot \text{SPECIEY } D = 0.250 \, \text{M}.$
- $\frac{3-168}{F_{ALLOW}}$ FALLOW. ON EACH BOLT: $F=A_5$ $T_d=\frac{\pi(1.25)^2m^2}{m^2}$. ROODLE $T_d=\frac{\pi}{2}$ $T_d=\frac{\pi}{$
- 3-169 COMPUTE FORCE REQUIRED TO PUNCH OUT THE SHAPE IN

 FIGURE P3-169 T = F/A & F = TA. LET $T = S_{MS}$ Alsi 1020 CD, $S_M = 75 Msi$. $S_{MS} = 0.82 S_M = 0.82 (75) = 61.5 Ksi$ A = SHEAR AREA = PERIMETER * THICKNESS = $p \cdot t : t = 0.085 IN$ $P = 1.0 + 1.0 + 2.0 + \sqrt{1^2 + 1^2} + 0.50 + T(0.5)/2 = 6.70 IN$ $A = p \cdot t = (6.70)(0.085) = 0.569 IN^2$. $F = S_{MS} \cdot A = (6.5 \times 10^3 M / IN^2)(0.569 IN^2) = 3500 M = F$
- $\frac{3-170}{P=TA=Sas\cdot A. 6061-t4. Sas=24ksi-APP.A-17.t=0.101N}$ $P=4(1.25)+3(0.5)+17(1.50)/2=8.861N^2; A=p.t=0.8861N^2$ $F=S_{NS}\cdot A=(24x10^3 ll/1N^2)(0.8861N^2)=21,260 ll=F$
- $\frac{3-171}{P} = T \cdot A = S_{MS} \cdot A \cdot S_{MS} = 1/0 MPa \cdot A = P \cdot t, t = 3,0 mm$ $P = 30 + 60 + \sqrt{20^2 + 40^2} + \sqrt{10^2 + 40^2} = 176 mm \cdot A = 527.9 mm^2$ $F = S_{MS} \cdot A = (1/0 N/mm^2)(527.9 mm^2) = 58.06 \cdot RN = F$

- 3-172 F=T.A=SMS.A. AISI/040 CD. SM=669 MPa. SMS=,825M=549MPa A=p.t.t=1,60mm.p=50+30+2(20)+17(20)/2=151,4mm A=(157,4mm)(1.60mm)=242 mm². F=549N,242 mm²=133.kN
- $\frac{3-173}{5ns} F = T.A = Sns \cdot A \cdot A1SI 1080 OQT 900. Sn = 1234 MPa$ Sns = 0.82 Sn = 0.82 (1234 MPa) = 1012 MPa $A = \rho \cdot t \cdot t = 0.80 mm, p = 60 + 2\sqrt{15^2 + 15^2} + 22 + 17 (4) = 139 mm$ $A = (137 mm)(0.80 mm) = 109.6 mm^2, F = (1012 \lambda/mm^2)(109.6 mm^2)$ F = 110.9 RN
- $\frac{3-174}{A=p.t.} F=T.A=SMS.A-ALVM 5154-H38.SMS=193MPQ.$ A=p.t. t=2.00mm.POUTSIDE=2(120)+2(50)=356mm PINSIDE=TY(15)+2[2(15)+2(10)]=/47.1mm $TOTAL P=PO+Pi=503.1mm.A=p.t=(503.1\chi2.0)=1006mm^2$ $F=SMS.A=(193N/mm^2)(1006mm^2)=194.2NN=F$
- $\frac{3-175}{F1RST STEPS} P = P_{INSIDE} = 147.1 mm \cdot A = P \cdot t = (47.1)(2.0) = 294.2 mm^{2}$ $F_{i} = Sms \cdot A_{i} = (193 N)_{mm^{2}} (294.2 mm^{2}) = 56.8 kN = F_{i}$ $\frac{2ND STEP}{F_{2}} P = P_{OVTSIDE} = 356 mm \cdot A_{2} = (356)(2.0) = 7/2 mm^{2}$ $F_{2} = Sms \cdot A_{2} = (193 N)_{mm^{2}} (7/2 mm^{2}) = 137.4 kN = F_{2} = ANSWG2$

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Problems with More Than One Kind of
Direct Stress and Design Problems
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Direct Stress and Design Problems

$$\frac{3-176}{4}$$
 $T = 5000 LB-IN;$ FORCE ON SIDE OF KEY = $F = \frac{T}{R} = 5000/1.125 = 4444 LB.$

SHEAR: $T = F_{As} = F_{b}L$

Let $T = T_{a} = \frac{0.55y}{2} = \frac{(0.5)(Hossesi)}{2} = \frac{16000Psi}{2}$

REOD. $L = \frac{F}{b} = \frac{4444 LB}{(0.50mVeauls/in^2)} = \frac{0.556iN}{2}$

BEARING:
$$\sigma = \frac{F}{A_b} = \frac{F}{(N_2)(L)}$$

LET $\sigma = \sigma_{bd} = 0.95y = 0.9(64 60081) = 57.600 8i$
 $RED'D. L = \frac{F}{(N_2)} \frac{9444}{(0.59)_{2}} (536018/11)^{2} = 0.309 IM.$

$$\frac{3-177}{V} = \frac{SHEAR! \ TWO \ PINS, EACH IN DOUBLE SHEAR; \ A_3 = 4[n0]_3 = 170^2}{V = \frac{F}{A_3}! \ FOR \ STATIC \ LOAD, \ T = 17 = 0.55 \text{N}_2 = 0.5182000) = 20500 \text{PS}_1}$$

$$REOD. \ A_3 = \frac{F}{T_3} = \frac{42000 \ \text{LB}_{100}}{20500 \ \text{LB}_{100}} = 2.049 \ \text{Inz} = 170^2$$

$$REOD. \ D = \sqrt{A_3/\pi} = \sqrt{2.049 \ \text{M}^3/\pi} = 0.808 \ \text{In}.$$

$$SPECIFY \ D = 1.00 \ \text{N}.$$

CHECK BEARING:
$$O_{bd} = (0.9)(S_V) = 0.9(82000 PS;) = 73 800 PS;$$
 $O_{b} = \frac{C}{A_{b}} = \frac{C}{(0)(2L)}$

REQ'D. $L = \frac{F}{(0)(2)(G_{bd})} = \frac{42000 L0}{(0.0M)(2)(73800 L9/M^2)} = \frac{0.285M}{VERY SMALL}$

a) TENSION IN MEMBER I AT PIN HOLES:

$$A_{\pm} = 2[(20-12)(14)] = 224 \text{ mm}^2$$

$$\sigma = \frac{F}{A} = \frac{20\times10^3 \text{ N}}{224 \text{ mm}^2} = 89.3 \text{ M/a} \quad Too \text{ H/GH}$$
FOR 6061-T4: $\sigma_0 = 5y/2 = 145 \text{ m/a}/2 = 72.5 \text{ m/a}$

b) BEARING AT THE PIN - MEMBER I $O_b = \frac{P}{A_b} = \frac{20 \times 10^3 N}{(12)(14)(2) Mm^2} = 59.5 MPa$ FOR 6061-TY; Obd = 0.65 Sy = 0.65 (145 MA) = 94.3 MAR OR

C) BEARING AT THE PIN - MEMBER Z $O_b = \frac{P}{A_b} = \frac{20 \times 10^3 N}{(12)(20) mm^2} = 83.3 MPa$

FOR 2014-TY; OB = 0.65 Sy = 0.65 (290 MPG) = 189 MPG OK

- d) PIN IN BEARING: MEMBER 3 Obmas = 83.3 MPA AT MEMBER 2 FOR 2014-96; Qu = 0.65 Sy = 0.65 (414 MPA) = 269 MPA OK
- C) PIN IN SHEAR DOUBLE SHEAR As = 11 (12)2(2) = 226 mm T= P/As = 20×103N/226 mm = 88.4 MPa FOR 2014-T6; T3 = 0.554 = 0.5(414 MA) = 103 MPA OK

3-179 a) SHEAR OF PIN: T= F/As: LET T=7; SAS - OBESM - 082(97) = 9,94 KSi

FALLOW = To: As = 9940 LB . 271 (0.63) TW2 6260 LB

- b) BEARING: OF = F/AB : LET OF = GH = 0.9 SY = 0.9(82) = 73.8KS [

 FALOW, = OH 'A = 73800LB = (0.63)(2X0.38)/N^2 = 35.340LB
- C) TENSION: $G = \frac{F}{A_{t}} \cdot k_{t}$; LET $G = G_{0}^{*} \cdot \frac{SM}{B} = \frac{97}{2} = 12$. 125 µsi $A_{t} = (1.50 0.63)(2)(0.38) = 0.66/1R^{2}$ $K_{t} = FROM APP. A 22 4 CURVEB; <math>d/M^{*} = 0.63/1.50^{*} = 0.42$; $K_{t} = 2.83$ $F_{ALLOW} = \frac{G}{3} \cdot A_{t} = \frac{(12125 LB/M^{2} \times 0.661 M^{2})}{2.83} = \frac{2832 LB}{K_{t}}$

3-180

FIG. P3-180 RIVETED PLATES. ASSUME STATIC LOAD

6061-T6 PLATES: Sy = 40KSi , Sn = 45KSi 17% ELONGATION

2014-T4 RIVETS: SMS = 38KSi , Sy = 42KSi

- a) SHEAR OF RIVERS: $T_d = \frac{5}{N} \frac{1}{1} \frac{1}{1} \frac{38}{1} \frac{1}{1} \frac{1}{1} \frac{9.50}{1} \frac{1}{1} = \frac{9.50}{1} \frac{1}{1} \frac$
- b) TENSILE STRESS ON PLATE: OF = SY/3 = 40 MSi/3 = 13.3 KS;

 O = F/A. A = [3.0 IN 2(0.5 IN)] 0.375 IN = 6.75 IN²

 F = Of A = (13333 M) (0.75 IN²) = 10000 M
- C) BEARING ATRIVETS/HOLES: $O_b = \frac{E}{A_b} = 0.65 \text{ Sy}$ $O_{bd} = 0.65 (40 \text{ Ks}) = 26 \text{ KS} i \text{ ON PLATE}$ $A_b = 2(0)(t) = (0.50)(375)(2) = 0.375 \text{ IN}^2 PR_b \text{ JECTED AREA}$ $F = O_{bd} \cdot A_b = \left(26000 \frac{\text{eV}}{\text{IN}^2}\right) \left(0.375 \text{ IN}^2\right) = 9750 \text{ U}$ SHEAR STRESS GOVERNS! FALLOW = 3736 UL

3-181

DATA FROM PROBLEM 3-180; USE FIGURE P3-181

- a) <u>SHEAR OF RIVERS</u> $T_d = 9500 M/_{IN} = F/AS$ $A_S = 3(IT-(0.375)^2/4) = 0.3313 IN^2$ $F = T_d \cdot A_S = (9500 M/_{IN}^2)(0.3313 IN^2) = 3148 M$
- b) TENSILE STRESS IN BLATE! OF=13333 ps; = F/A

 A = [3.0-3(0.375)] (0.375) = 0.703 IN2

 F = Os.A = (13,333 ll/,N2) (0.703 IN2) = 9375 ll
- C) BEARING & OLD = 26 000 M/m ON PLATE

 Ab = 3[Dit] = 3[(0,275)(01375)] = 0,422 IN2

 F = Obd. Ab = (26000 M/IN2)(0.422 IN2) = 10,969 M

 SHEAR STRESS GOVERNS: FALLOW = 3148 M

3-102 DATA FROM PROBLEM 3-180

a) SHEAR OF RIVETS!
$$T_d = 9500 \, ll/_{IN^2} = F/A_S$$

 $A_S = 4[H(0.375)^2/4] = 0.44/8 IN^2$
 $F = T_d \cdot A_S = (9500 \, ll/_{IN^2})(0.44/8 IN^2) = 4197 \, ll$

$$\begin{array}{l} \underline{ON\ PLATES}:\ O_{bd} = 0.65(40 \text{KS}I) = 26 \text{KS}I \\ A_b = 2(0.25)(0.375)(2) = 0.375 \text{IN}^2 \\ F_b = O_{bd}\cdot A_b = (26000 \text{M/N}_2)(0.375 \text{IN}^2) = 9750 \text{M} \\ \underline{ON\ RIVETS}:\ O_{bd} = 0.65(42 \text{KS}I) = 27.3 \text{KS}I \\ A_b = 2(0.375)(0.375) = 0.28 \text{IN}^2 \\ F_b = (27300 \text{M/IN}_2)(0.28 \text{II}) = 7678 \text{M} \\ \underline{SHEAR\ OF\ RIVETS}\ GOVERNS:\ FALLOW = 4197 \text{M} \end{array}$$

$$\frac{3-183}{FENSION} REPEATED FORCE.$$

$$\frac{FENSION}{FENSION} IN LINKA! OJ = \frac{SM_{8}}{8} = \frac{147 \text{KS}i/9}{9} = \frac{18.375 \text{KS}i}{100}$$

$$\frac{O = \frac{K+F}{A}}{A} : F = \frac{OB}{A} \frac{ANET}{K+C} = \frac{(18375 \text{M}/N^{2})}{2.60} (1.5-0.76)(1.25) N^{2}}{100}$$

$$\frac{APP}{A} \frac{A22-4}{4}, \text{ curves}; \frac{d}{N} = \frac{0.79}{1.5} = 0.50 ... K+C = 2.60}{(AISI III/4) OQT 1100}$$

$$\frac{FALLON = 6626 \text{ LL}}{SHEMS} \frac{STRESS}{INPM} INFINITY T_{3} = \frac{54}{8} = \frac{97 \text{KS}i/8}{9} = \frac{12.125 \text{KS}i}{100}$$

$$\frac{F}{A} : F = \frac{7}{6} \cdot \frac{A_{5}}{A_{5}} = \frac{(12125 \frac{M}{A})}{100} \left(\frac{2}{1100.150^{2}/4} \right) = \frac{10.713 \text{ LL}}{100}$$

$$\frac{BEARING}{A} STRESS AT PIN' : OLD = 0.90 SV = \frac{10.90}{20.90} (97 \text{KS}i) = 97.3 \text{KS}i}$$

$$A_{6} = \frac{(1.25 \text{ M})}{(0.75 \text{ IN})} = 0.9375 \text{ IN}^{2}$$

$$O_{6} = \frac{F}{A} = F = O_{60} \cdot A_{6} = \frac{(97300 \text{ M}/N^{2})}{(0.9375 \text{ IN}^{2})} = \frac{81843 \text{ M}}{100}$$
TENSION IN LINK GOVERNS! FALLON = 6626 LL

FORCES IN MEMBERS: AB = ZY65 LB(+), AC = 1925 LB(C)

BC = 1375 LB (T), BD = 1200 LB(T), CE = 650 LB(C),

CD = 750 LB (C), DE = 961 LB(T).

SUPPORT FORCES! AY = 1540LB + , BY = 2690LB + , BX = 100LB

MATERIAL! ASTM ASG STRUCTURAL STEEL, SY=36KS; ASSUME STATIC LOAD. OJ = 51/2 = 18KS;

KE	OD AREA!	AMIN = F/ON			SQUARE	ROUM	THREAD
	MEMBER	F(U)	Od (ksi)	Amin (142)	ban	DMA	
	AB	2465	18	0.137	-374	,418	1/2-13
	BC	1375	18	0.0764	1276	,3/2	3/8-16
	BO	1200	18	0.0667	.258	.291	3/8-16
	DE	94	18	0.0534	,231	,261	3/8-16

ALTERNATIVE DESIGNS:

SOUND ROD : A = TO 3/4; DMIN = VA

THREADED ROD! LET AMIN L TENSILE STRESS AREA OF THREAD
FROM APP A-3, COARSE THREADS

FOR THRETTOED ROO, ATTACH TO CLEVIS AT EACH END, DESIGN PIN FOR CLEVIS FOR SAFE SHEAR STRESS.

AT BI PIN JOINT ATTACKED TO FRAME

AT A: PROVIDE ROLLER ON BIN THAT BEARS ON FRAME.

AT C AND E', PROVIDE AN ADDITIONAL CLEVES FROM WHICH TO ATTACH LOADS.

NOTE: COMPRESSION MEMBERS MUST BE DESIGNED WITH COLUMN BUCKLING ANALYSIS. SEE CHAPTER 11.

3-185 FORCES INMEMBERS!

AB= 4687 N (T) BE=0 BF= 2241 N (T) CB= 1097 N(T)

AD = 1400 N (T) DE= Z300N(C) CF= 800 N (C) FG = SON(C)

BD = 2597N (C) BC = 750N(T) EF= 2300N (C)

SUPPORT FORCES! AY= 1400N + , Ax= 4683N -, Dx= 4488N

DESIGNS COULD BE SIMILAR TO PROBLEM 3-184

FORCES ARE GENERALLY SHALLER. SMALL WIRES MAY BE USED FOR TENSION MEMBERS. COMPRESSION MEMBERS MUST BE DESIGNED FOR BICKLING. SEE CHAPTER 11.

3-186

FORCE ANALYSIS;

USING FBO OF ENTIRE STRUCTURE!

ABIS A TWO FORCE MEMBER

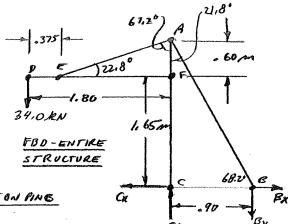
FBD OF BOOM ;

PIN A:

SUMMARY OF RESULTS:

a) FORCES IN WIRES: A E= 110.8 hN; AB= 13.2 kN

C) SHEARING FORCE IN EACH PIN:



AEY AE 1.80m FX 34.0 AN

FBD OF BOOM



AY= 48=73.2/2W

Ax=74.9 A

Fx = Fy = 8.95 kN

lozizkn

FBD OF VERTICAL SUPPORT

Cx=272

Cy = 102 kN

3-186 (CONTINUED) b) DESIGN DE ROOS! AE = 110.8 KN, AB= 73.2 KN, MODERATE SHOCK. 02 = 5M/12. SPECIFY AISI 4140 OQT 900. Sn= 1289Mla, 151/00006. HIGH STRENG DA, GOOD DUCTILITY. Od = 1289 MPa/12 = 107.4 MPa = 107.4 N/mm LET O = OMAX = F/A . THEN REODA = OF FOR AE: A = F = 110.8 × 103N = 1031 mm2 = 1702/4 REQ'D D = J4A/1 = J4(1031 mm2)/1 = 36.2 mm SPECIFY D= 40 mm - PREFERRED BASIC SIZE. APP. 2 FOR AB: A = F = 73.2 × 103 N = 681.6 mm2 = 1717/4 REOD D= [4A/H = /4(681.6 mm2)/+ = 29.5 mm SPECIFY D= 30.0 mm - PREFERRED BARN SIZE d) DESIGN OF PINS: ALL PINS TO BE IN DOUBLE SHEAR USING A CLEVIS -TYPE CONNECTION. [SEE FIG. 3-17] FROM TABLE 3-8; To = 5 ys/6 = 51/12 SPECIFY AIST 4140 OOT 900. Sy= 1193 MPA, 1540 EL ONG. To= 51/12 = 1193 MBa/12 = 99.4 MBa = 99.3 N/MM2 LET TO = TMAX = F/As . THEN REOD AS = F/TH $\frac{PINA!}{As} = \frac{134 \text{ kN} \cdot REGD. As}{FA} = \frac{F}{T_{3}} = \frac{1348 \text{ mm}^{2}}{99.3 \text{ N/mm}^{2}} = \frac{1348 \text{ mm}^{2}}{99.3 \text{ N/mm}^{2}}$ $As = \frac{2A}{T_{3}} = \frac{2 \text{ HD}^{2}/2}{T_{3}} \cdot REGDDD_{A} = \sqrt{\frac{2(1348 \text{ mm}^{2})}{17}} = \frac{29.3 \text{ mm}}{T_{3}} \cdot \frac{SPECIFYD}{T_{3}} = \frac{30.0 \text{ mm}}{T_{3}}$ $\frac{PIN F!}{Dmin} = \frac{102.6 \text{ MN.}}{Z As/H} = \frac{102.6 \times 10^{3}}{Z (1032 \text{ mm}^{2})} = \frac{1032 \text{ mm}^{2}}{T (1032 \text{ mm}^{2})} = \frac{1032 \text{ mm}^{2}}{Z (1032$ PIN C: F = 105.6 MN. As = 105.6×103 = 1062 mm2 DMIN = \(\frac{12(1062)}{7} = 26.0 mm. SPECIFY De=28.0 mm PIN E: F= 110.8 KN. As= 110.8 X103 = 1115 mm PMIN = [2 (1115)] = 26.6 mm. SPECIFY DE=28.00000 PIND: F= 34.0 kN, As = 34×103 = 342.4 mm DAN = \(\frac{2(342.4)}{7} = 14.8 mm. SPECIFY D= 16 mm

[NEXT PAGE FOR BEARING STRESS.]

3-186 (CONTINUED)

BEARING STRESS ON PINS: [SEE FIR3-17 FOR DESIGN OF SOINT]

$$O_b = \frac{F}{A_b} = \frac{F}{D \cdot t_1} \quad AND \quad t_2 \ge \frac{t_1/2}{2}$$

$$RE@D, \quad t_1 = \frac{F}{D \cdot O_{bd}}$$

That = 0.90 SY FQ. 3-22 FAR STEEL.

Sy = 1/93 MPa - AISI 4140 OQT 900 FOR PINS

MATERIAL FOR MATING PARTS MUST BE ATLEAST AS STRONG.

Obd = 0,90 (1193MPa) = 1074MPa = 1074N/mm2

THE REQ'D THICKNESS IS QUITE SMALL. IT IS HIGHLY WAY
THAT ACTUAL DIMENSIONS FOR to AND to ARE MULH
LARGER FOR OTHER STRESS CONDITIONS.

THIS IS ALSO WERY SMALL. PINS F AND CHAVE SUGATLY LOWER FORCES, SO RED'D & 15 SIMILAR.

NOTE! IF BOOM OR COLUMN ARE MADE FROM A MATERIAL WITH LOWER STRENGTH (SUCH AS STRUCTURAL STREEL),
BEARING STREES CALCULATINS MUST BE REDONE.

CHAPTER 4 Torsional Shear Stress and Torsional Deflection

$$\frac{4-1}{3} T = \frac{(BONNM)(10000)}{\pi(20)^{3} 12 \text{ mm}^{3}} \times \frac{10^{2} \text{mm}}{10} = \frac{178 \text{ Mfa}}{18000}$$

$$\frac{4-2}{32} J = \frac{\Pi}{32} (00^{4} - 0.1^{4}) = \frac{\Pi}{32} (35^{4} - 25^{4}) = 109 \times 10^{3} \text{ mm}^{4}$$

$$T = \frac{TC}{3} = \frac{(S60 N \text{ m})(35/2) \text{ mm}}{10^{9} \times 10^{3} \text{ mm}^{4}} = \frac{89.9 \text{ Mfa}}{10^{9} \times 10^{3} \text{ mm}^{4}} = \frac{89.9 \text{ Mfa}}{10^{9} \times 10^{3} \text{ mm}^{4}}$$

$$\frac{4-3}{3} T = \frac{(S500 L8 \cdot 10)(1.25/2) \text{ in}}{J} = \frac{4092 \text{ es}}{10^{9} \times 10^{3}}$$

$$\frac{4-4}{3} Di = 0.0 - 2t = 1.75 - 2(0.725) = 1.50 \text{ in}}{10^{9} \times 10^{9}} = \frac{176008i}{32}$$

$$T_{0} = \frac{TC}{J} = \frac{(5500 L8 \cdot 10)(1.25/2) \text{ in}}{32} = \frac{173608i}{32}$$

$$T_{0} = \frac{TC}{J} = \frac{(5500 L8 \cdot 10)(1.25/2) \text{ in}}{0.924 \text{ in}^{4}} = \frac{173608i}{32}$$

$$T_{1} = \frac{T\Lambda_{1}}{J} = \frac{(5500 L8 \cdot 10)(1.50 L2) \text{ in}}{10^{9} \times 10^{9}} = \frac{9734 \text{ es}}{10^{9} \times 10^{9}}$$

$$\frac{4-5}{J} = \frac{P}{M} = \frac{0.08 \times 10^{3} \text{ N/m}}{10^{9} \times 10^{9}} = 0.494 \text{ N/m}$$

$$T = \frac{P}{M} = \frac{35 \times 10^{3} \text{ N/m}}{10^{3} \times 10^{9}} = \frac{10^{3} \text{ mm}}{10^{9}} = \frac{833 \text{ N/m}}{10^{9}} = \frac{833 \text{ N/m}}{10^{9}}$$

$$T = \frac{P}{M} = \frac{35 \times 10^{3} \text{ N/m}}{273 \times 10^{9} \text{ m/m}^{4}} = \frac{78.3 \text{ Mfa}}{10^{9} \times 10^{9}}$$

$$T = \frac{17}{M} = \frac{63000(P)}{270 \times 10^{9}} = \frac{(63000)(15.01e)}{10^{9} \times 10^{9}} = \frac{3938 \text{ L6.1N}}{10^{9} \times 10^{9}}$$

$$T_{0} = \frac{59}{2N} = \frac{101000 \text{ es}}{10^{9}} = \frac{841765i}{0} \text{ OK}$$

```
4-8

FROM PROBLEM 4-7, T = 3938 LB·IN, Tg = 84/7 PSS

C = 1.44 m./2 ° 0.72 m.

f = π 0 4

32 = π (1.44 m.) = 0.422 m

FOR PROPILE KEYSENT, Ke ° 2.0

T = KeTC (2.0 ¥3938 LB·IN)(0.72 IV) = /3 433 PSi

BECAUSE T >T , DESIGN IS NOT SAFE.
```

$$T = 63000 (7.5KP) = 2/5 LB.IN$$

$$AT FILLET: h/d = 0.85/0.75 = 0.066; 0/d = 1.25/0.75 = 1.61; k = 1.55$$

$$AT KEYSEAT: k = 2.0$$

$$T_{MAY} = \frac{K}{2P} = \frac{(2.0 \times 2/5 LB.IN)}{10.055} = 5/90 PSI$$

$$BLAGE WWID SEE STACL: Td = \frac{5}{2} \frac{1}{2} \frac{1}{$$

6061-T6 HAS SV = 276 MPa

```
MASS = (VOL)(DENS.) = A.L. DENS = II (SO) & 600 mm x 7680 kg, 1 mm 3
                  M=9.05 kg
               HOLLOW: J= TT (50 4-404) = 362.3 XA3 mm
                  7 = (850)(25)(03) = 58.7 MPa (1.69 TIMES TSU.10)
                  0 = (850)(606)(109) = 0.0176 had [1.69 TIMES OSINO]
                 M = #(502-40) x(600) (7680) = 3.26 kg [San 15 2.78 TIMES HIGHER]
\frac{473}{76} \quad R = 00. \quad Z_{\rho} = \frac{T}{76} = \frac{1200 \text{ N/m}}{45 \text{ N/mm}^2} \frac{10^3 \text{ m/m}}{m} = 26667 \text{ m/m}^3
\frac{Z_{\rho} = \frac{17}{16} \frac{D_{\nu}^4 - D_{\nu}^4}{p_0} = \frac{17}{16} \frac{(J_{\nu} + D_{\nu})^4 - D_{\nu}^4}{J_{\nu}^2 + D_{\nu}^2} = 0.226 D_{\nu}^3
R = \frac{17}{16} \frac{D_{\nu}^4 - D_{\nu}^4}{p_0} = \frac{17}{16} \frac{(J_{\nu} + D_{\nu})^4 - D_{\nu}^4}{J_{\nu}^2 + D_{\nu}^2} = 0.226 D_{\nu}^3
R = \frac{17}{16} \frac{D_{\nu}^4 - D_{\nu}^4}{p_0} = \frac{17}{16} \frac{(J_{\nu} + D_{\nu})^4}{J_{\nu}^2 + D_{\nu}^2} = 0.226 D_{\nu}^3
                                    Do = 1.25 Di = 61.3 mm
               T = 63000(7.5)/241 = 1969LB.1H
T = \frac{T}{20} = \frac{1969LB.1H}{11(6.26)^3/16.1H^3} = 15764.051
                T = 63000 (7.5) / 1140 = 414 LB.JA
                REOD. 20 T = 414 LB.IN = 0.0263 IN = 11 D3/16
                 REO'D. D= 1620/11 = $1610.0263/17 = 0.5/2 IN
              T = F-d = (BOLe)(1811) = 1440 LB-14; Zo= 0.6524 113 (APP.A-12)
                  T= T/20= 1440 LB.14/D.6524 14 = 2207 15i
477 M= (180/55EC) (6050/MW) = 120 RAM3 T=BOLB. AT XIZW/AT)=36018.1N
               \rho = \frac{Tm}{63000} = \frac{(360)(12)}{63000} = 0.0686 \, \text{LP}
                T = T/20 = 360 La.IN/11(0.60)3/16 N3 = 8488 PSi = S1/2N = SY/8
               REO'D Sy = 8 T = 8 (8488) = 67 900 PSi
                POSSIBLE STEEL: AISI 1040 WOF 1100, Sy=80KS; 24% ERONG.
```

```
J,=11(20)/32=15 708 mm & & J2=11(40)/3 =257 300 mm
               0=0.067 + 0.0119 = 0.0756 RAD (4.83 056.)
4-28 0-(10.0 DER) (TRAO/HODER) = 0.1745 A
               REOD f = \frac{TL}{66} = \frac{(6.0 \text{ N/m})((50 \text{ m/m}))}{(26 \times 10^4 \text{ N/m}^2)(0.1745)} \times \frac{10^9 \text{ mm}^3}{(26 \times 10^4 \text{ N/m}^2)(0.1745)} = 165.3 \text{ m/m}^4
               REOD D=1327/11 = 640 mm
                T = \frac{Tc}{t} = \frac{(5.000 \, N \cdot man)(3.20 \, mm)}{165.3 \, mm} = \frac{96.8 \, MPa}{2.000 \, mm}
N = \frac{Sy}{2.(7)} = \frac{276 \, MPa}{2.(96.8 \, MPa)} = 1.43 \, Low
                 COULD USE STRONGER ALUMINIM OR LONGER BAR
4-29 T=T-20= 250N x #(150) man = 165.7 Himm
               0 = TL = (65.7 Noman) (40mm) -106mm2 - 0278 RAD (15.9 066)
4 130 += TT (184-164) = 3872 mm 4: 0 = 40 DE6 x TTMO/180 DE6 = 0.698 RAD
              T = \frac{663}{L} = \frac{6.698 \text{ RAD}(43 \times 10^{9} \text{ N/ara})(3872 \text{ man}^{4})}{1650 \text{ m/m}} \frac{\text{Im}^{2}}{105 \text{ m/m}} = 704 \times 10 \text{ N·mm}
T = \frac{T_{c}}{3} = \frac{60.42 \times 10^{3} \text{ N·mm}(4 \text{ m/m})}{3872 \text{ m/m}^{4}} = \frac{164 \text{ M/a}}{2.069 \text{ m/m}} = \frac{3.27}{2.069 \text{ m/m}}
               J= TT (35) 4/32 = 147.3 x 10 3 mm 4
               TAC = 73 = 500 Nom = 500 XIO Nomm : TA = TE +T2 = 1500 Nom = 15x1 Nomm
                G= 806Pa= (80×109 N/m2) (102/106 mm2) = 80×103 N/mm2
                 BAC = DAB + DBC = TAO LO + TEC LZ

BAC = (55x106 Nema (500 mm)) + (500108) (800)

(80x103 NAMOR) (147.3x103 mm) + (80x103) (147.3x103)
                  OAC = 0.0636 + 0.0339 = 0.0976 RAO (5-59 PEG) (3.64 DEG.)
                 \theta = (2.2 \text{ DEG}) ( // RAG / RG \text{ DEG}) = 0.0384 \text{ RAO}
REG 0 \ \ J = \frac{TL}{60} = \frac{(360 \text{ M·m})(810 \text{ M/m})}{(80 \text{ M/m}^2)(810364)} \times \frac{(10^3 \text{ m/m})^3}{40^3} = 363 \times 10^3 \text{ m/m}^4 = \frac{\pi D^4}{32}
                 REDD D= (32 + 11 = 43.9 mm

T= TC = U360 N·m)(21.95 mm), 18 mm = 82.1 M/a
```

4-33 TEP = 120 x103 NIM/S = 539 Nim $J = \frac{II}{32} (754 - 55^4) = 2.208 \times 10^6 \text{ m/m}^4$ $T = \frac{TC}{3} = \frac{(533 \text{ N/m})(32.5 \text{ m/m})}{2.208 \times 10^6 \text{ m/m}^4} = \frac{9.06 \text{ Mfa}}{\text{N}}$ $\theta = \frac{TL}{6} = \frac{(533 \text{ N/m})(1.525 \text{ m/m})}{(80 \times 10^6 \text{ N/m}^2)(2.208 \times 10^6 \text{ m/m}^4)} \times \frac{(603 \text{ m/m})^3}{(6.264 \text{ DEG})}$ $\frac{4.34}{200} T = \frac{p}{100} = \frac{60 \times 10^3 \, \text{N·m} / \text{S}}{700 \, \text{RAD/S}} = 857 \, \text{N·m}$ $2p = 17 \, \text{d}^3 / \text{b} = 17 \, \text{(35)}^3 / \text{b} = 2418 \, \text{m·m}^3$ 1/4=4/35=0.114 : 0/3=50/20=1.435 Kg=1.35 FROM APP. A-22-7 7= TK+ 657 Nim (635), 10mm = 137/1/a $\frac{4-35}{T} = \frac{P}{M} = \frac{105 \times 10^3 \, \text{N·m/s}}{220 \, \text{RAO/s}} = 477 \, \text{N·m}$ $\frac{7}{M} = \frac{105 \times 10^3 \, \text{N·m/s}}{1000 \, \text{RAO/s}} = 12.566 \, \text{m/m}^3$ 1/4= 6/40 = 0.150 ; 0/8 = 70/40 =1.75 ; Ke = 1.29 PROM APP. A-22-7 T= TK= HTINIM)(1.29) 103mm = 49.0 MPa FOR PROBLEMS 4-36 THROVAN 4-39: To = 5x = 669 MPA = 83.6 MPA OR 7, = 97000 PS/ = /2/25/5/ T = TK+ /20 ; ALLOW. T = (Ta)(20)/K+ 4-36 LEFT ENQ: 20 = TT (12) 3/16 = 339.3 mm3 N/a = 2/12 = 0.167; 0/4 = 21/2 = 2.0; k= =1.21 (A-22-T = (B3.6 N/mm²)(339.3 mm³) = 22.3 N/m CRITICAL VALUE RIGHT ENO: 20= 15 (1653/16 = 804-2 mm 1/4=1/16 = 0.063; 0/4 = 24/16 = 1.50; Kt=1.53 (A-22-7) T = (83.6 N/mm²)(801.2 mm²) = 43.9 x/03 N/mm = 43.9 N/m GROOVE Zp= TT(1.20)3/16=0.339 183 LEFT GROOVE: N/J = 0.008/1.20 = 0.0067; D/J = 1.50/,20=1.25; K=3.0 EIT. (A-22-1) RIGHT GROVE: $N_{H} = 0.08/120 = 0.061$; % = 1.25; $K_{t} = 1.63$ (A-21-6) LEFT GROWE CRITICAL! $T = \frac{(2.125 \text{ LB}/M^{2})(0.339 \text{ M}^{2})}{3.0} = \frac{1370 \text{ LB}/M}{2}$

Note concerning Problems 4-40 to 4-57: Torsion of Noncircular sections

These problems involve the analysis of torsional shear stress and torsional deformation of load-carrying members having noncircular cross sections. Data for the factors J and Z_p are computed from the equations in Figure 4-27.

```
4-40 T=T/2,8 T=TZp=(50N/mm2)/168/mm2)=83.2x3N/mm=832N/m
             2= 0.208 a3= 0.208 (20)3 = 1664 mon3
4-41 5=0.14/ a = 0.14/ (20) = 22.56 X10 mm
            442 Zp= 0.208 03 = 0.208(125)3 = 0406 IN3
            T = 7-20= (7500 LB/M-) (0.406 IN3) = 3047 LB.IN
4-43 J=0.14/ A4 = 0.14/ (1.25)4 = 0.344 IN4

6 = TZ (3047 LB/IN)(48/IN)

6 = (3.75 XN LB/IN)(0.344/IN4) = 0.112 RAO (6.42 OF6)
4-44 Zp= 6/2 [3+18(4/6)] = (3.0)(1.25)2 = 1.25 1013
             T= TZ = (3500LB/IN-)(1.25/N3) = 9375 LBIN
           J= (3.01/25) [ + - 021 125 (1- (1.25/20)4)]= 1.44 144
            \theta = \frac{TL}{G + 72.5210^{3}(1.44)} = 0.0367 \text{ RAO} (3.20.006.)
           J= 0.02/7a"=0.02/2(30)"= 17.58×103 mm
             0=(0.80 DES) ITRAD/180 DEG.) = 0-0140 RAD
            T= 060 _ (0.0140 RAO) (26000 N/mm) (1250 Nomm) = 246 Nomm
            Z= 0.050 a3 = 0.050(30)3 = 1350 mm3
             1 = T = 2961 Nimm = 1.82 Ma
\frac{4.48}{1.02} \frac{\text{ORLULAR PART: } E_{\theta} = 170^{3}/16 = 17(1.75)^{3}/16 = 1.052/N^{3}}{16 = \frac{1}{1000} = \frac{250 \text{ LBUA}}{1.000 \text{ LBUA}} = \frac{608151}{1000 \text{ LBUA}}
            SHAPT WITH FLAT: h=1.50-0.875=0.6200 ; h= 1/25=0.875/N
                1/2 = 0.625/0,875 = 0.714 & C = 1.089 (INTERPLATION-FIG. 4-27)
                Zp= (2 13=(4.069)(0.875)3= 0.716.143
                7 = 1/25 850LB-IN/0.716 IN3 =1187:055

\frac{4-49}{J_{c}} = \pi(1.75)^{4}/32 = 0.9208 \text{ in}^{4}; C_{1} = 1.24 \text{ (INTERPRATION -FIG 4-27)}

J_{c} = C_{1} D_{1}^{4} = 1.24 \text{ (0.815)}^{4} = 0.727 \text{ in}^{4}

\theta = \frac{TL}{GJ_{c}} + \frac{TL}{GJ_{c}} = \frac{(850)(20)}{(1.5210^{5})(7.727)} = 0.0010 + 0.00203

\theta = 0.00364 RAD = 0.209 DEE.

J_{c} = J_{c} = 0.209 DEE.

              JE = I FOR SHAFT WITH FLAT
```

```
h = 1.25/2-0.628 M: A/h = 0.625/0.875 = 0.7/4: C= 0.839
4-50
           Zr = Cv /L<sup>3</sup> = 0.839 (0.875) = 0.562 /N<sup>3</sup>
            T'= T 850 LB / IN SAMET WITH FLATS
4-51
           C3 = 0.966 FOR M/h=0.714 IN FIR 4-27 BY INTERPOLATION
            J=C3 124 = 0.966 (0875)4 = 0.566 104
            \Theta = \frac{TL}{G\frac{1}{2}} = \frac{(850)(20)}{(1/374/0^{4})(0.566)} = 0.0026 RAO IN SNAFT WITH FLATS
            OTOT = 0.60/6 + 0.0826 = 0.0042 RAD (0.24/0 66.)
(ROUND) (FLATS)
           E_p = 0.208 \, a^3 = 0.208(8)^3 = 106.5 \, mm^3 \left\{ (F16.4-27) \right\} = 0.141 \, a^4 = 0.141 \, (8)^4 = 577.5 \, mm^4 \right\}
             T = Sys = 0,5 Sy = 0,5(1070) = 535 MPa
             T = TZP = (5.35 N/mm²) (106,5 mm²) = 57.0 K10 N/mm = 51.0 N/m

0 = TL = (57.0 × 10² N/mm × 200) m/m

G = (43000 N/mm²) (577.5 m/m²) = 0.459 RAO (26.3 DEG)
            0= 3.0 DER (TRAD/RODER) = 0.0524RAD.; USE t= tdes = 0.233in
             f = \frac{2t(a-t)^2(b-t)^2}{(a+b-2t)} = \frac{2(a-233)(3.767)^2(3.767)^2}{(4+4-2(0.733))} = 12.45 IN^4
             T= 061 = (0.0524) (11.5×106 LB /14) (12.45/44) = 78 150 LB ·14
             Z=2+(a-t)(b-t)= 2(0.283)(3.767)(3.767) = 6.6/3/183
             T=T= 78150 LB./N = 1/8/8 PSi
              FOR ASTM ASOI STEEL, Sy = 36000PSi
               T_d = \frac{S_V}{Z(t)} = \frac{36000 PSI}{4} = \frac{9000 PSI}{4} NOT SAFE
            J= 2(.237)(3.767)2(5.767) = 23.07/N4
            T = 06+ = 6.0524 X 11.5 x/0 (23.07) = 144 860 LB-IN
4-58 &= 2(0.233) (3.767)(5.767) = 10.12 IN3
            T= T/Z= 144800/10/12 = 14300 PSi NOT SAFE
4-57 TUBE: 20 = 2(0:233) (57167) 2 = 15,50 IN3 PIRE: 20 = 16.99 IN3
            J=21,233 (5,767) (5,767) 2 44,69 M4
                                                         J=JI=2(28N)=5628 MY
                                                        To= T/20= 0.0589 T
           7- T/2= 0.0648 T
            \frac{1}{GT} = \frac{16}{GT} = 0.0224(71/6)
                                                        OP= Th= 0.017(12/4)
           \frac{T_{\tau}}{\tau_0} = \frac{0.0648}{0.0589} = 1.10
\frac{\theta_{\tau}}{\theta_{\theta}} = \frac{0.0224}{0.0177} = 1.266
```

P=T·M T=P/M D= 25MM M= 1150 rev . 2 11 rod . /min = 120.4 rod/s $T = \frac{P}{M} = \frac{125 \times 10^3 \text{ N·m/s}}{120.4 \text{ Ned/s}} = 1038 \text{ N·m}$ $\frac{T_{MAx}^{2}}{f} \frac{Tc}{f} = \frac{T}{2P} = \frac{1038N \cdot m}{97(36mm)^{3}/16} \frac{10^{3}mm}{m} = 123N = 123MPa$ 4-59 SMOOTH POWER. To = SYS/N = SY/2N . LETN = 2 Td = SY/4. LET TMAX = Td = SY/4 REQ'D Sy = 4(Ta) = 4(123MPa) = 493 MPa POSSIBLE STED: AISI 1040 CD, SY = 565 MPa 4-60 REPEATED POWER LET N=4, Td=5y/2N=5y/8=TMAY REOD SY = 8 TMAX = 8(123 MPa) = 986 MPa POSSIBLE STEEL: AISI 4140 OQT 900. Sy= 1193MPa 15% RUNGATION. GOOD PACTILITY. 4-61 SHOCK LOADING KET N=6, Td=5V/12=5V/12=TMAX REGO Sy=12 TMAX = 12 (123 MPa) = 1480 MPa. POSSIBLE STEEL: A1SI 4140 DOT 700, Sy= 1462 MPa 12% ELONGATION, MARGINAL STRENGTH, SATISFACTORY DUCTLITY. 4-62 P= 12.0 HP STEADY. M= 1150 Mpm - SY= 80KS/ T = 63 000 (P)/m = 63 000 (12)/1/50 = 657 IN.CB TMAX = T/20. REOD 20 = T = 657 IN.LB = 0.0329 IN3 = 1103 LETTMAX = To = SY/4 = 80 hsi /4 = 20 Ksi = 2000 Rl/me D= 1/6 ZP = \$16(0.0329/N3) = 0.551 IN; SPECIFY D = 0.60 IN 4-63 P=20.0 HP STEADY. M= 3450 Npm, Sy=10/KS/ T = 63000(P)/m = 63000(20)/3450 = 365 IN.LB TMAX = 12p. REQD Zp = T = 365 INLE = 0.01451N3 = 1103 TMAX = 25250 LB/IN2 = 0.01451N3 = 1103 LET TMAX = Ta = 58/4 = 101 KSi/4 = 25.25KSi = 25 250PSi

DMIN = 3/1620 = 3/16(6.0HS) IN3 = 6.419IN; SPECIFY D=0.50IN

4-64 Do=100 mm; Di=60 mm; ALLOY STEEL ZPs = 97 0.3/16= 17 (100 mm) 3/16 = 196350 mm3 T=T.Zp= (200 N/mm2) (196350 mm3)=3,927×107N.mm $T_{HOLBOW} = \frac{T}{Z_P} = \frac{3.927 \times 10^7 \, \text{N/mm}}{1.709 \, \text{M/o}^3} = 230 \, \text{N/mm}^2 = 230 \, \text{M/o} = T_H$ $Z_P = \frac{T}{16} \frac{D_0^4 - D_1^4}{D_0} = \frac{T1 \left[100^4 - 60^4\right]}{16 \left(100\right)} \, \text{mm}^3 = 170900 \, \text{mm}^3$ 4-65 FIND ANGLE OF TWIST FOR SHAFT OF PROB. 5-64. T= 3.927 X107 N.mm $\frac{SOLIO SEGNENT!}{\Theta_{S}} = \frac{17D_{0}^{4}}{32} = \frac{17(100 \text{ m/m})^{4}}{32} = 9.817 \times 10^{6} \text{ m/m}^{4}$ $\frac{1}{100} = \frac{1}{100} = \frac{1}{1$ HOLLUN S'EGMENT: J= 17 (1004-604) mm = 8.545 × 106 mm4 OH = TL = (3.927 × 107) (300) = 0.0172 red TOTAL OF = 05 + 04 = 0.0/50+0.0172 = 0.0322 Rad (1.850EA) 4-66 FIND T IN EACH PART OF SHAFT. M = 1750 New 218 RAD , 1 min = 183 rod/s TA = PA = 15×103 N·m/s = 81.85 N·m $T_c = \frac{P_c}{m} = \frac{20 \times 10^3}{183} = 109.1 \text{ N·m}; T_B = \frac{P_B}{m} = \frac{35 \times 10^3}{183} = 191.0 \text{ N·m}$ TAB= TA = 81.85 Nom TBC = TE = 109.1-Nom 1 AB 1 A = 01.80 Norm 180 - 18 TAT BEARING TORIGHT OF PULLEY: STEPPED SHAFT. D=10 mm D/d= 15/10= 1.50; 1/d= 0.5mm/10 mm = 0.05; Kt=1.60 T = TAB : Kt/20 = (81.85)(1.60) (103) = 667 MPa (CONTINUED NEXT PAGE) 4-66 (CONTINUED)

TO LEFT OF BO RETAINING RING GROUVE; D=14 MM ATGROOME

I AT KEYSEAT AT B: D= 15 mm, K= 2.0 FORKEYSEAT

T=Ta= = 69.1 Nim

TTO RIGHT OF B AT SHOULDER FILLET! P=15mm, D==Zomm

T AT RIGHT BEARING AT SHOULDER FILLET! D=15 mm, Pr=20mm

SAME CONDITIONS AS AT PULLEY! T= 288 MPa

TAT CAT RETAINING RING GROOVE! KE=3.0; Dg=14.0 mm

TATE AT SLED RUNNER REY SEAT! D=15mm Kt=1.60

SUMMARY SEVERAL STRESSES ARE QUITE HIGH. LARGER SHAFT DIAMETERS RECOMMENDED.

4-67 FIND Y IN EACH PART OF SHAFT.

$$T_{A} = \frac{P_{A}}{m} = \frac{20 \times 10^{3} \, \text{N/m/s}}{120.4 \, \text{rod/s}} = 166 \, \text{N, m} \times \frac{10^{3} \, \text{m/m}}{m} = 1.66 \times 10^{5} \, \text{N. m/m}$$

$$T_{C} = \frac{P_{C}}{m} = \frac{12 \times 10^{3} \, \text{N. m/s}}{120.4 \, \text{rod/s}} = 99.6 \, \text{N. m} \times \frac{10^{3} \, \text{m/m}}{m} = 9.96 \times 10^{4} \, \text{N. m/m}$$

$$T_{B} = \frac{P_{B}}{m} = \frac{32 \times 10^{3} \, \text{N. m/s}}{120.4 \, \text{rod/s}} = 266 \, \text{N. m} \times \frac{10^{3} \, \text{m/m}}{m} = 2.66 \times 10^{5} \, \text{N. m/m}$$

$$T_{AB} = T_{A} = 1.66 \times 10^{5} \, \text{N. m/m}$$

$$T_{C} = T_{C} = 9.96 \times 10^{4} \, \text{N. m/m}$$

(CONTINUED NEXT PAGE)

4-67 (CONTINUED)

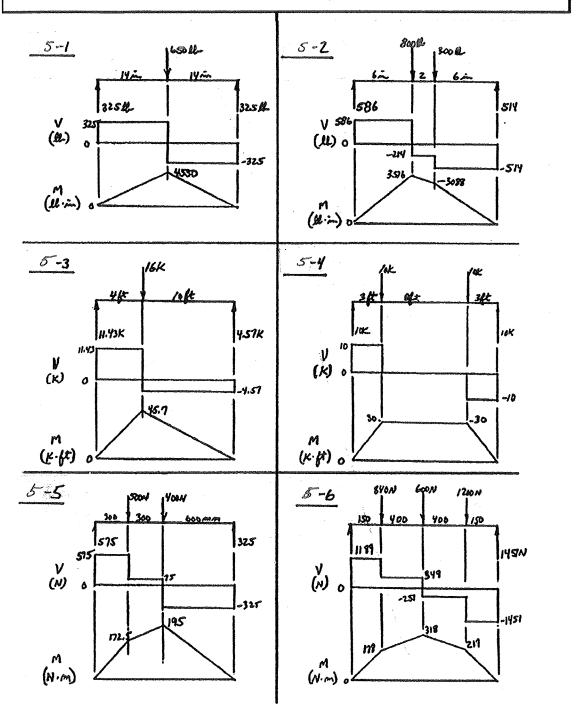
V, AT A ATKEYSEAT: D=20.0 mm; Kt= 2.0 -PROFILE KEYSEAT T, = TAB ET = 1.66 × 165 N/mm (2.0) = 211 N/mm² = 211 MPa TO mm³ 3/16 = 211 N/mm² = TMAX TEAT SHOULDER TO RIGHT OFA: D=20.0mm; 1/d= 30=1.50 A/d= 1.0/20 = 0.05; Kt = 1.62 Tr = TAR Kt (1.66 ×105)(1.62) = 171 MPa T3 AT RIGHT OF BEARING SEAT! D= 30mm; 0/= 40 = 1.33 h/1 = 1.0/3 = 0.033; Kt = 1.78 T3= TAB Kt = (1.66×105)(1.78) = 55.7 MPa TYAT RETAINING RING TO LEFT OFB: D= 40,0 mm; Kt=3,0 $T_{y} = \frac{T_{AB} K_{E}}{Z_{P}} = \frac{(1.66 \times 10^{5})(3.0)}{\pi (40)^{3}/16} = 39.6 MPa$ TSAT KEY SEAT ATB: KE=ZO, D=40mm 75 = TAB KE = Ty. KOS = 39.6MPa = 26,4MPa TO AT STEP TO RIGHT OF B! D=40 mm, %= 58.0 =1.25 M/1 = 10/40 = 0.025; Kt=1.85 76 = TBC Kt = (9.96 ×10) (1.85) = 14.7 MPa TTAT STEP FLOM 50 1030 MM DIA, D=30.0 mm, D/J=5/30=1.67 1/1 = 18/30 = 0.033; Kt= 1. Tr = TBC KC = (9.96 ×104)(1.82) = 10.7 MPa TO AT LEFT OF BEARING: D= 20.0 mm; 0 = 30/20 = 1.50 1/d = 1.0/20 = 0.05; Ke= 1.62 TBEKE = (9.96 X/04)(1.62) = 10.3 MPa TGAT STEP TO LEFT OF C: 0 = 15.0 mm; P/d = 20/15 = 1.33; 1/8=1/15=0.067 Kt=1.50: Tq= TBC Kt (9.96 X104)(1.50) = 22.5 MPa TIO AT KEYSEAT AT C! To = TECKT = 79 Ktio = (225) 2.0 = 30.1MPa

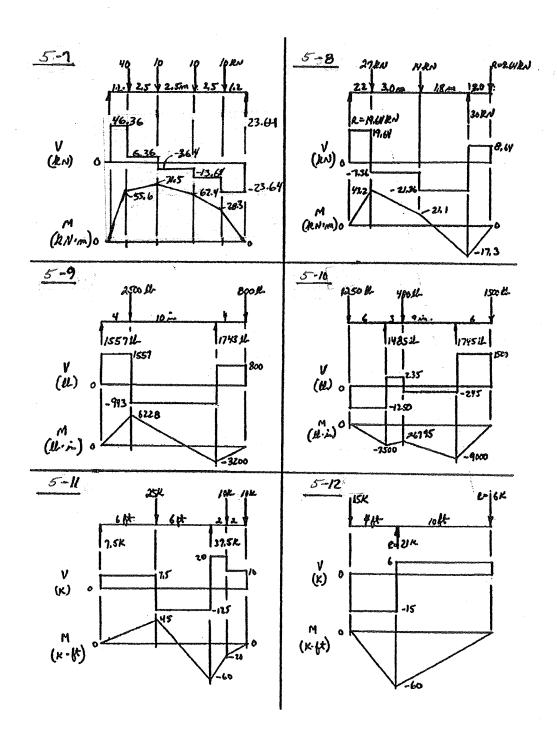
```
DESIGN SHAFT P=225kW', n=80 pm; To=60 MPa; Kt=1.0
 T = \frac{P}{m} = \frac{725 \times 10^3 N \cdot m/s}{8.38 \text{ rea/s}} = 26857 N \cdot m
M= 80 REV . ZITRAD . IMIN = BIBB RADIS
T = \frac{T}{2\rho} i REOD_{2\rho} = \frac{T}{T_d} = \frac{26857 N \cdot m}{60N / mm^2} \frac{10^3 mm}{m}
\frac{T}{T_d} = \frac{T}{60N / mm^2} \frac{10^3 mm}{m}
\frac{T}{T_d} = \frac{T}{60N / mm^2} \frac{D_0 V - D_0 V}{D_0}
BUT = \frac{T}{(6)} \frac{(1.25 D i)^4 - D_0 V}{(6)} = \frac{T(1.44 D i)^4}{(16)(1.25 D i)} = 0.226 D i^3
 THEN RED'D DA = 121 = 13 4.476 × 105 mm = 125.5 mm
                   Do $ 1.25 Di = 1,25(125.5) = 157 mm
  LET Do = 160 mm 3 Pi # Do - 160 = 128 mm; USE Di = 125 mm
    CHECK 20= IT DO4-Di4 = TI((1604-1/26)) = 5.05 x 105 mm 3
  TRY Do=160mm, Di=130 mm

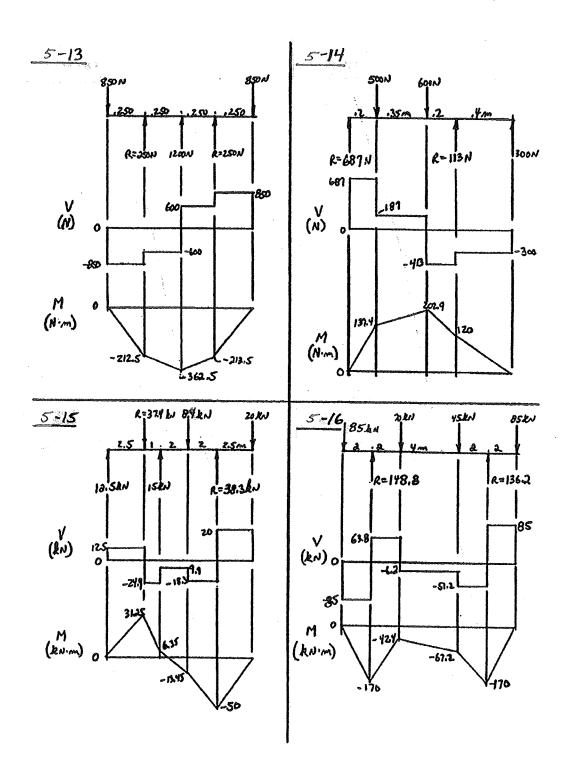
ZP= M (U60)4-130)4] = 4.54 X165 mm OK
    OR: LET DO=160 mm, SOLVE FOR RED'O. DI FORZO= 4.476×105 mm
        2P= T[(160)4-Di4] 1 (6)(160) 2p= 1 [1604-Di4]
      16(160) ZP = 1604 - Diy; Di = 1604 - 16(160)(4.476 x/5)
       Di MAX = 130.6 mm; USE Do =160 mm; Di=130 mm
   CHECK FOR WALL THICKNESS: t = 00-DA 160-130 = 15 mm
           MEAN RADIUS = Dotoi) = 72,5 mm
               MEAN/ = 72.5/ = 4.83 LIO . SHAFT IS NOT THIN WALLED
               BUCKLING NOT LIKELY.
```

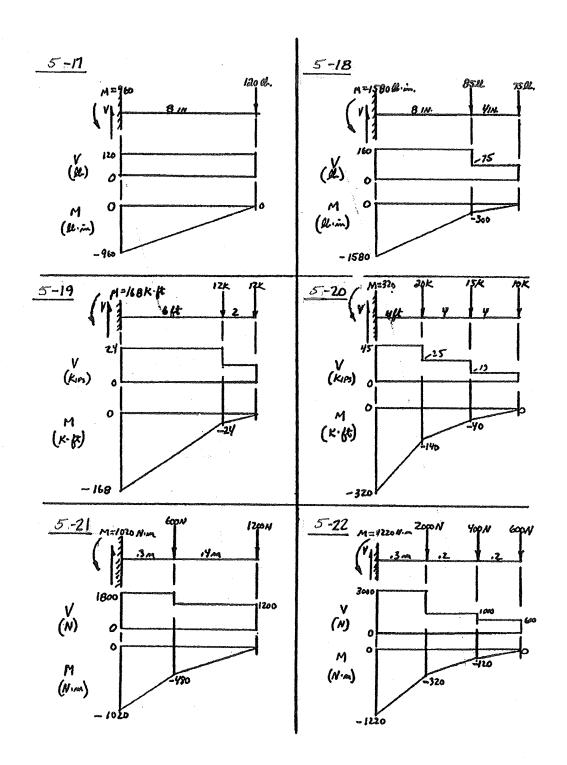
```
4-69 D= 4,0 mm; B= 180 DEG X TRAD = TTRAD; TAX= 150 MPa = TC
     J = 10 / 27 = 17 (400 mm) 4 = 25.1 mm 4
      TMAX = TMAX + (50 N/mm²)(25.1 mm4) = 1885 N.mm
       D= TL : LAIN = DGT
       G = 26 GPa = \frac{26 \times 10^9 N}{M^2} \times \frac{1 m^2}{(10^3 mm)^2} = \frac{26.0 \times 18^3 N}{m^2}
       Lnin = (17 RADX 26 × 103 N/mm²)(25.1 mm4) = 1088 mm = 1.088 mm
4-70 TORSION BAR! L= 200 mm = 0.200 m. Do/01 21.50
       TURSIONAL STIFFNESS = = = 0.015 DEG X TRAD = 0.26 18 X/0 RAD
          \theta = \frac{TL}{G+}, RED'D f = \frac{TL}{RG}
          G= 43 GPa= (43×109 N/m2) (1.0m2/106mm2) = 43 ×163 N/mm2
          J = (1.0 kinha) (200 mm) x 103 mm = 17766 mm4
           Do = 1,50(Di) = 1,50(14.53 mm) = 21.79 mm = 00
       ALTERNATE DESIGN: PREFERRED SIZE FOR Do = 22.0 mm
             f = H(Do4-Di4); Do4-Di4 = 32+; Di4 = Do4-32+
              Di = \ 00 - 32 + = \ \ \frac{4}{17} = \ \ \ \frac{122.04 - 32(17766)}{17} = \ \frac{15.19 mm = Di}{17}
         USE FIRST DESIGN FROM 4-70. Do = 21,79 mm, D1 = 14.53 mm
     T = \frac{TC}{t} = \frac{TDo}{+2} \theta = \frac{TL}{Gt} OR T = \frac{\theta GJ}{L}
      THEN T = BGY, Do = OGPO - 6.174 SRAD Y 43 X103 N/mm (01.79 mm)
       B = 10 ° x Tr RAO = 0.1745 RAO
       r= 408.BN/mm2= 408.8 MPa
```

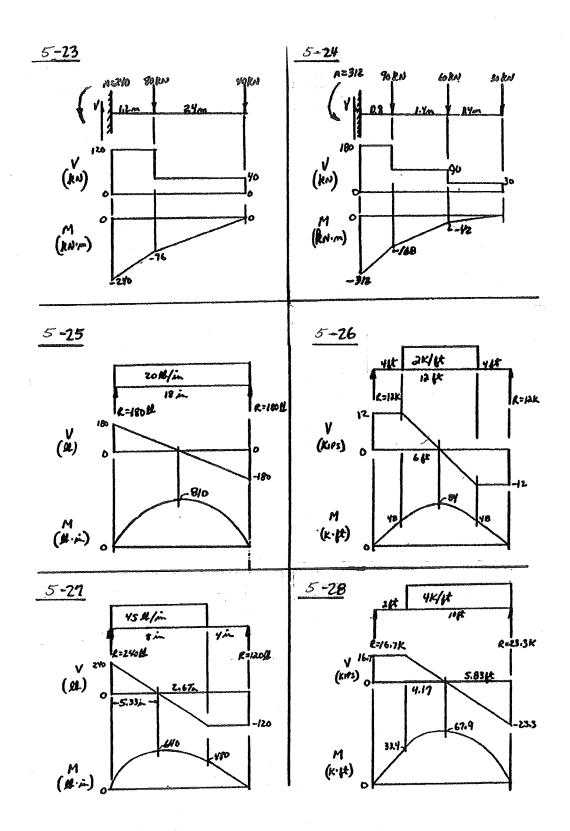
CHAPTER 5 Shearing Forces and Bending Moments in Beams

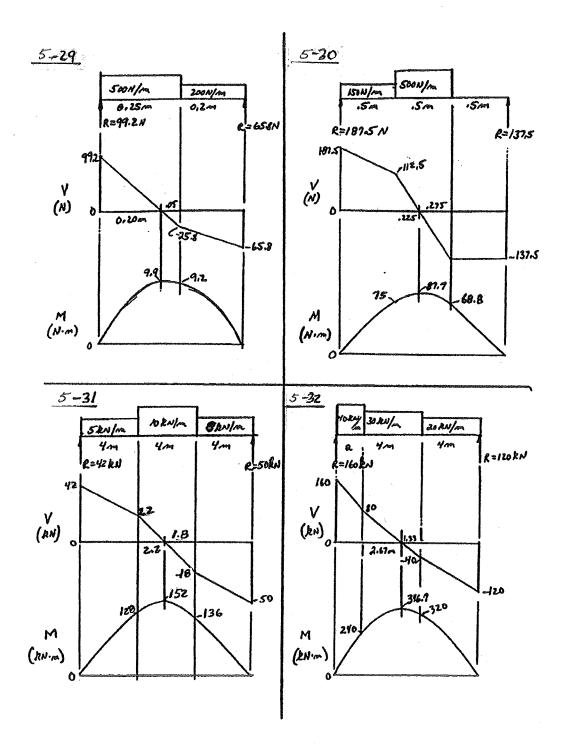


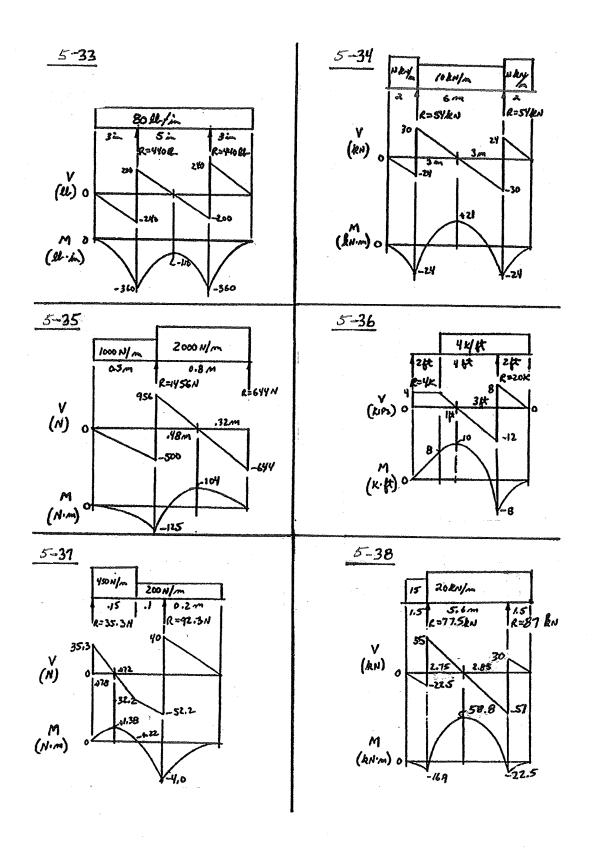


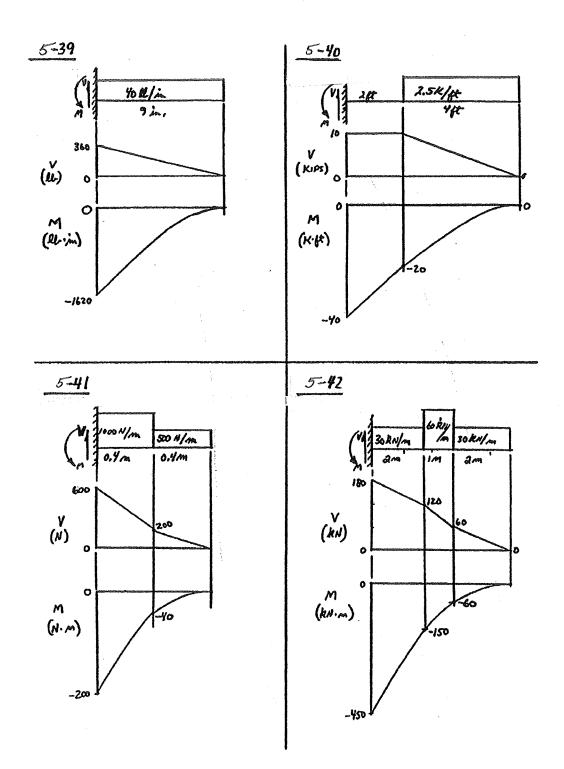


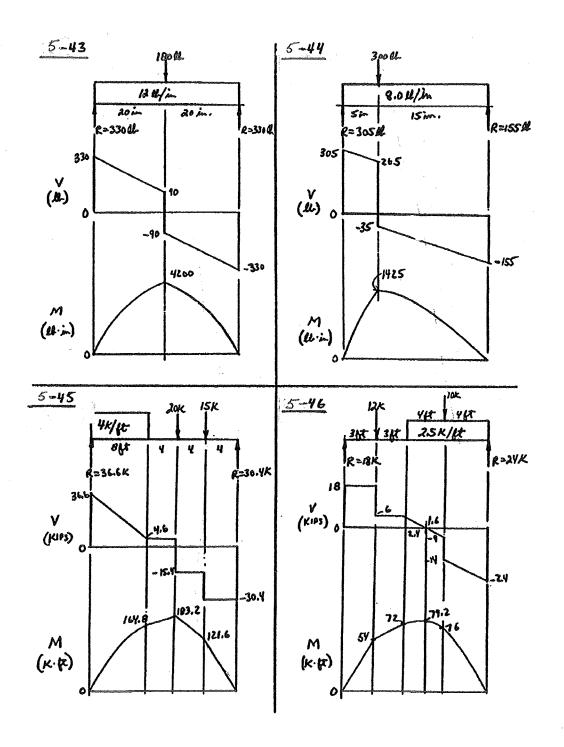


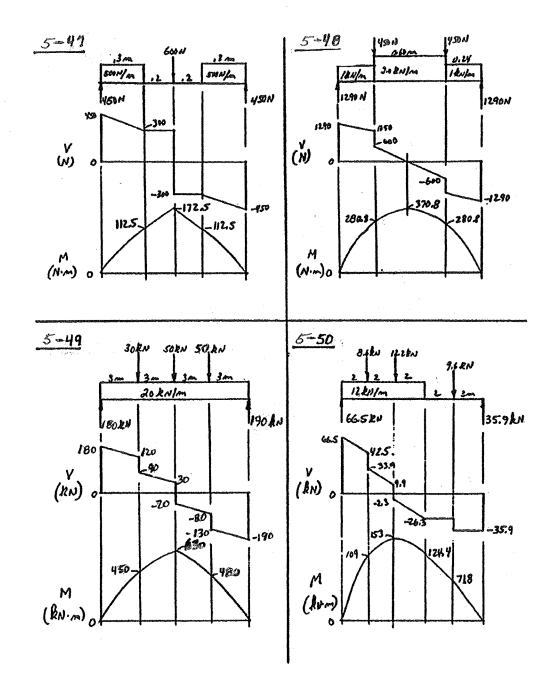


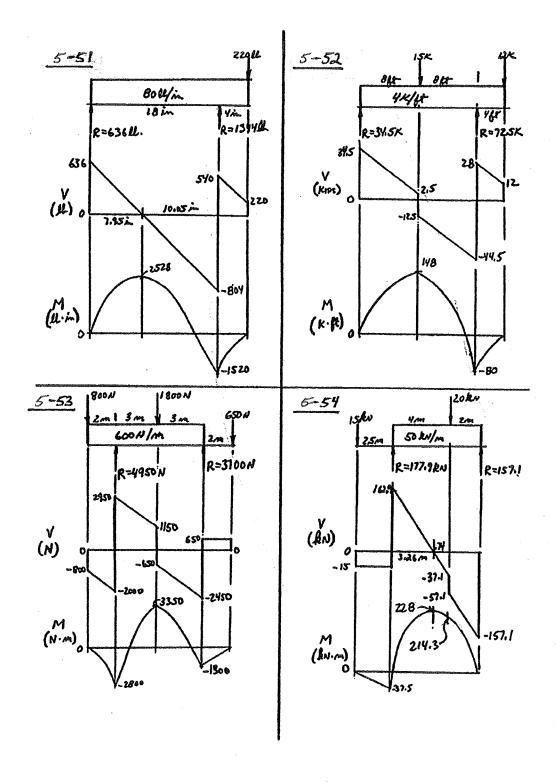


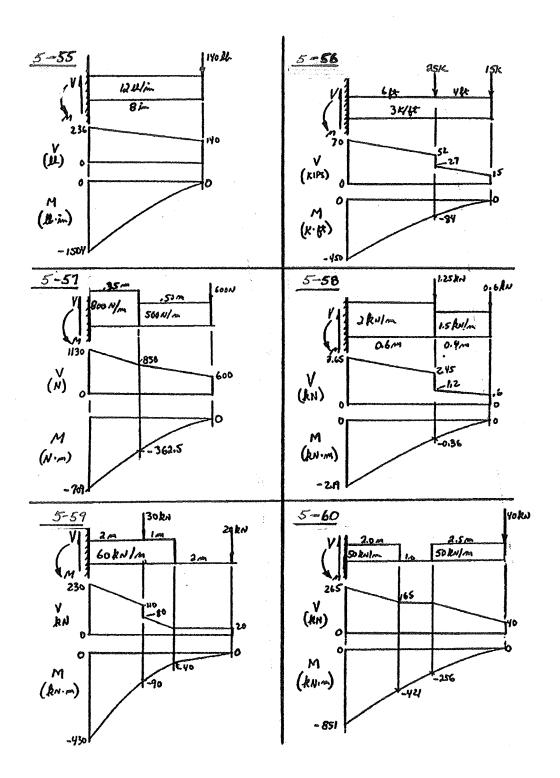


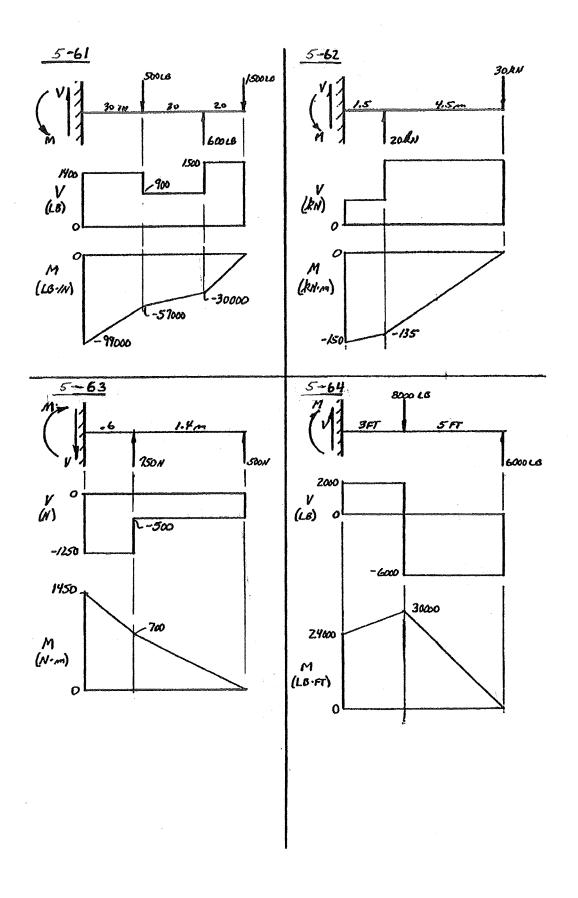


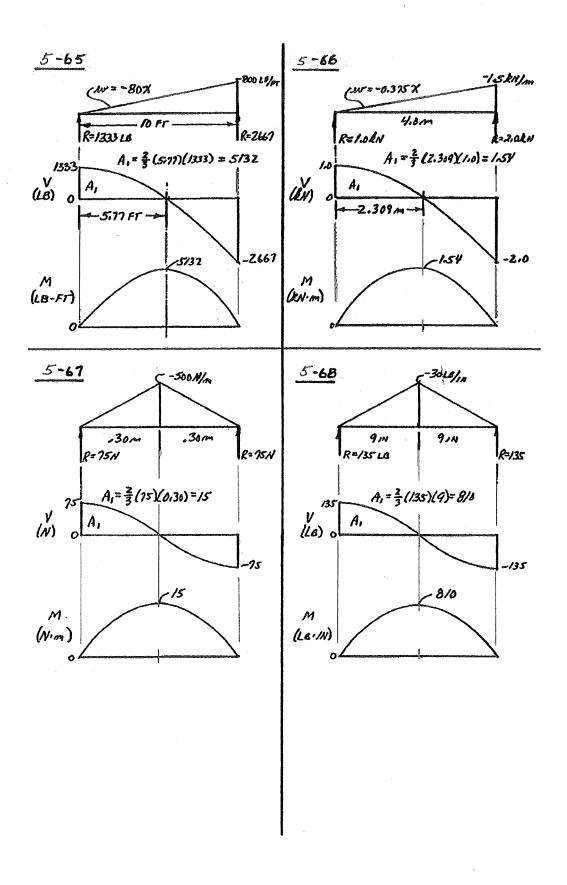


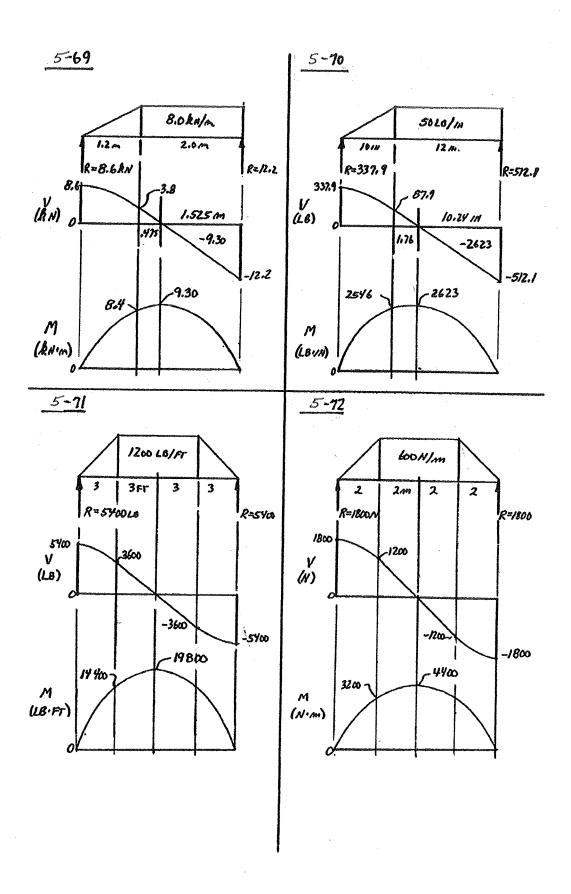


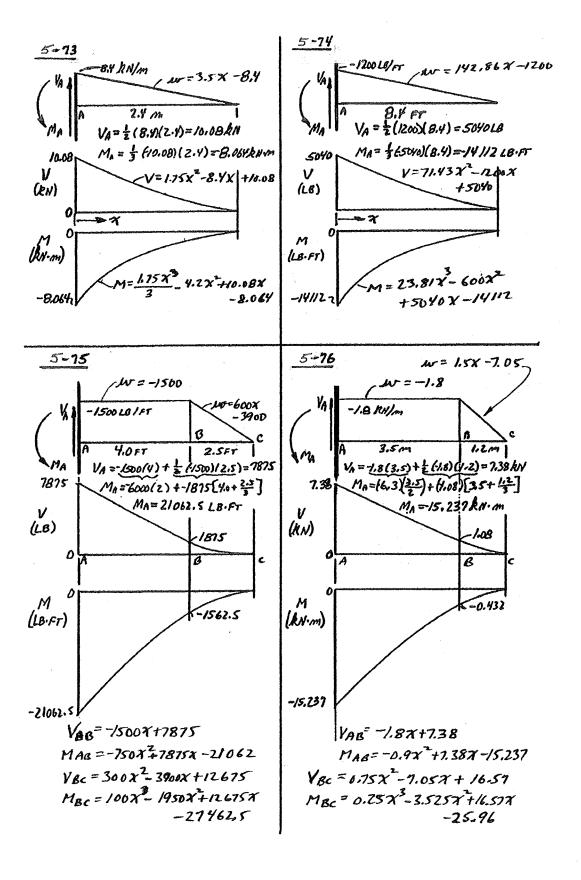


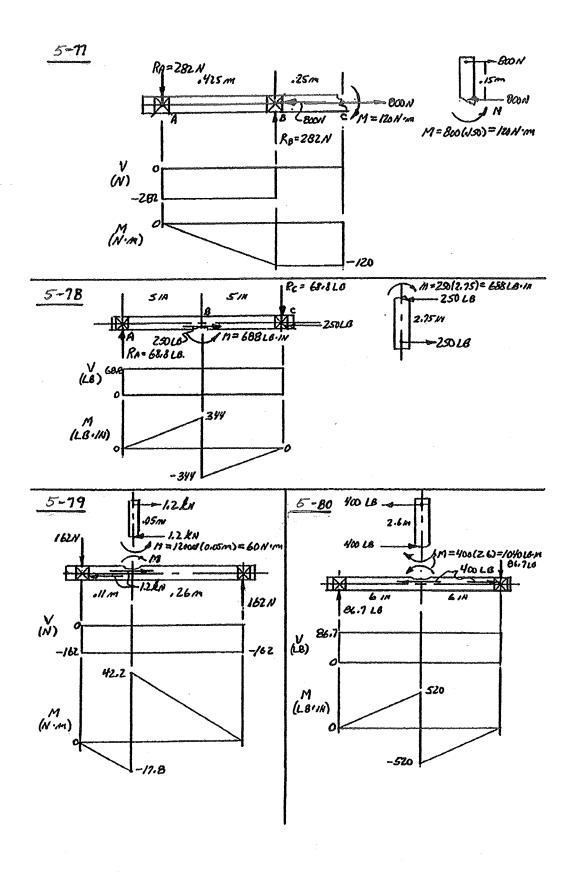


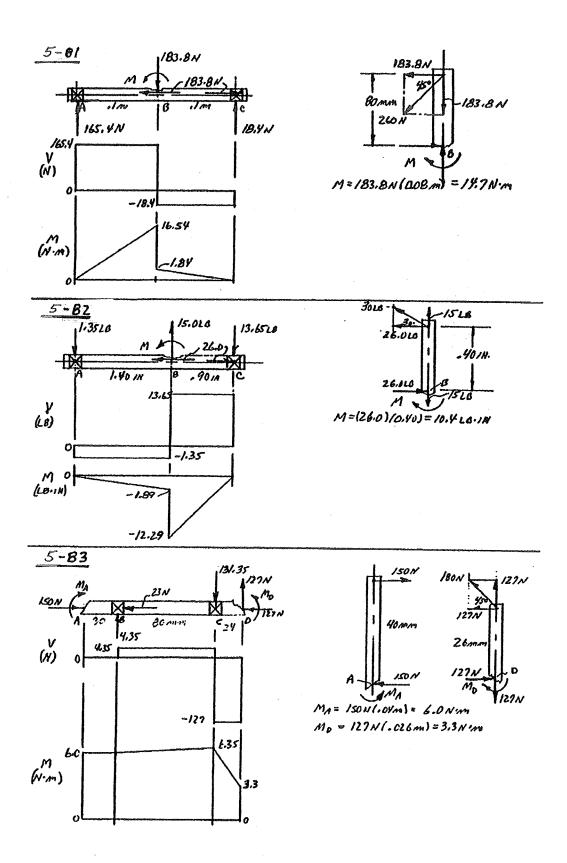


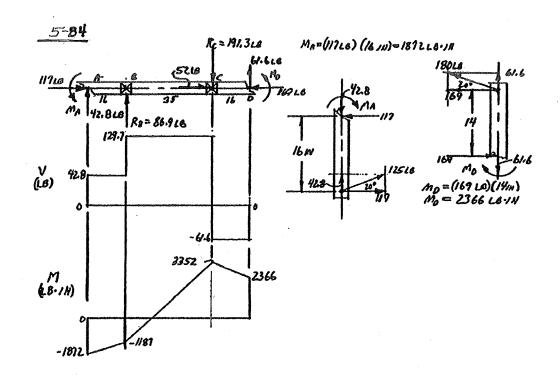




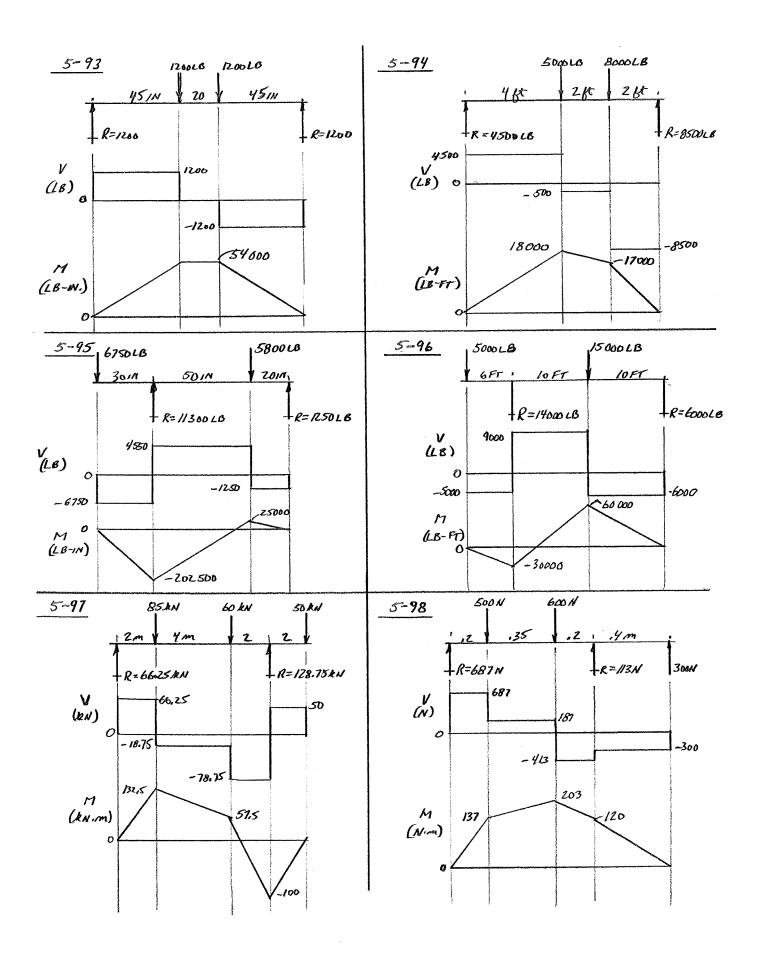


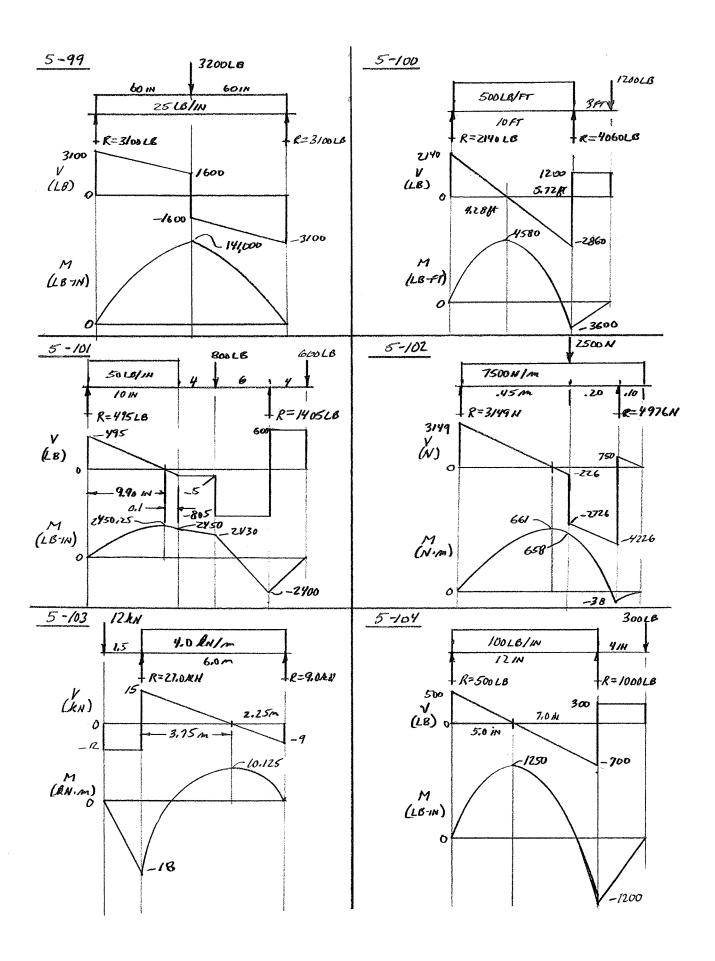


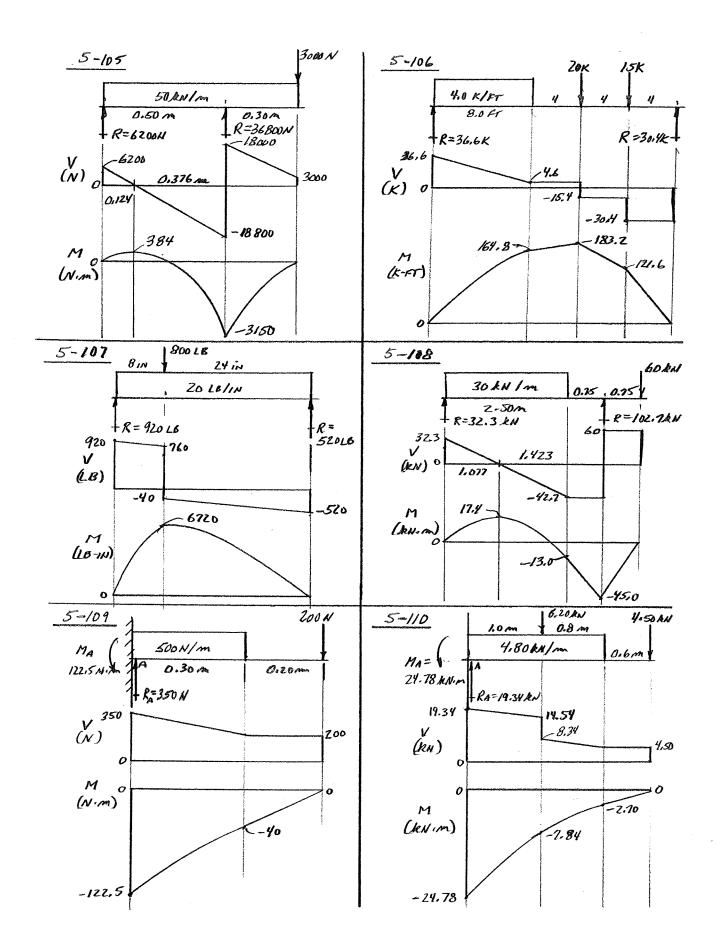


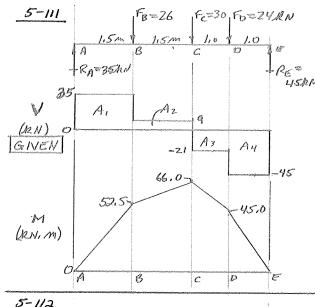


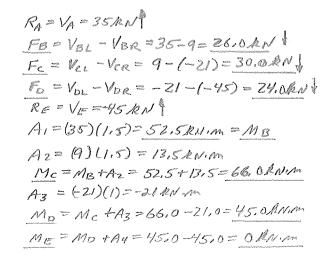
```
5-85
       FIGURE 5-B.
                         V= 19.64-27.0 =-7.36 AN
             27.RN
                             -M = (19.64.20) (4.6m) - (27.0AW) (1.8m)
                               M = 29.96 KN.M
   R=19.64 KN
5-86 FIGURE 5-15.
                        USE PART OF BEAM TO RIGHT OF CUT SECTION.
                 20 KN
                         M = (-20AN) (1.50m) = -30KN·M
5-87 FIGURE 5-22, R=3000N; M=/220 Nim
                                 V= 3000N-2006N = 1006N
                                 M = -1220 N.m + 3000 N (0.45m) - 2006 N (0.15m)
5-88
         FIGURE 5-35.
                        2 8004
                                      V= 1456 N - 500N - 800N = 56N
             W1=500 N
                                         M=(1456N)(O.4M)-(500N)(.65m)-BOON)(02A)
           1000 Nifm
                       R=1456N
5-89
                                 W= (600 N/m) (6.0 m) = 3600 N
         FIGURE 5-53.
           8004
                 W
                                   V = 4950 - 860 - 3600 - 1800 = -12 50 N
                                  M = (4950)(4)-800(6)-1800(1)-3600(3)
                                   M = 2400 N.m
                R=4950N
 5-90
         FIGURE 5-58.
                                  W1=2kN/m (.6m) = 1.2kN
                                  Wz = 1.5 Rd/m(0,2 m) = 0,30 kN
                                   RA= 3.65 RN, MA= -2.19 RN-M
                                    V=3.65-1.2-1.25-0.30=0.90 KW
                                     M = -2./9 + 3.65(0.8) - 1.2(0.5) - 0.3(0.1) - 1.25(0.2)
                                    M=-0.15/2N.M
5-91
         FIGURE 5-69.
                             W, = (,5)(8 ku/m)(1,2m) = 4.8kN; Wz=(8)(1) = 8kN
            W. 41 515
                              V = 8.6 - 4.8 - 8.0 = -4.2 km
                              M = 8.6(2,2) - 4.8(1.4) - 8.0(0.5) = 8.2 kN.m
P6-92 FIGURE 5-76, USE RIGHT PART FOR FBD.
                          W = (0.5)(1.05kN/m)(0.7m) = 0.327 kN
             1,05
     1.80-1
                          AT CUT: V= W= 0,377 km
                             M=-W(0,7-0,467)=(0,377 NN)(.233)=-0.0858KN. AM
```

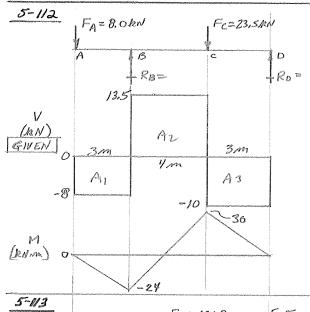












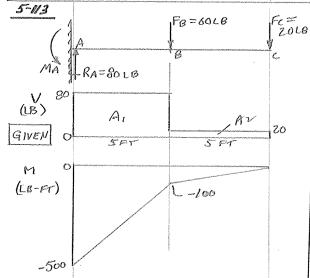
FA=VA=8.0 kN \\
RB=VBL-VBR=-8-13.5=21.5 kN \\
FC=VCL-VCR=13.5-(-10)=23.5 kN \\
RD=VD=-10.0 kN \\
A1=-8(3)=-24 kN.m=MB

A2=13.5(4)=54.0 kN.m

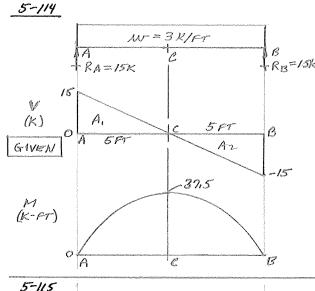
MC=MB+A2=-24+54=30.0 kN.m

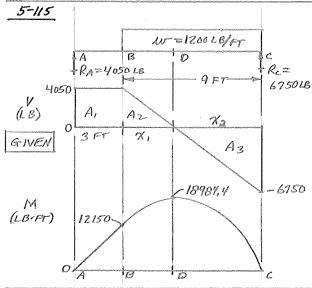
MD=MC+A3=30-30=0 kN.m

A3=-10(3)=-30 kN.m

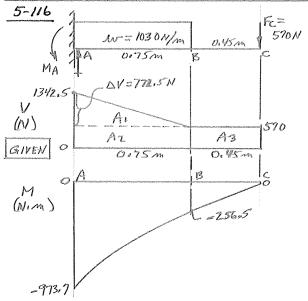


CANTILEVER $R_A = V_A = 80LB^{\dagger}$ $F_B = V_{BL} - V_{BR} = 80 - 20 = 60LB^{\dagger}$ $F_C = V_C = 20LB^{\dagger}$ FORCES PRODUCE A NET CLOCKWISE MOMENT THAT MUST BE RESISTED AT A. $M_A = (60)(5) + (20)(10) = 500LB - FT^{\dagger}$ NEG. $A_1 = (80)(5) = 400LB - FT$ $A_2 = (20)(5) = 100LB - FT$ $M_B = MA + A_1 = -500 + 100 = -100LB - FT$ $M_C = MBTA_2 = -100 + 100 = 0LB - FT$

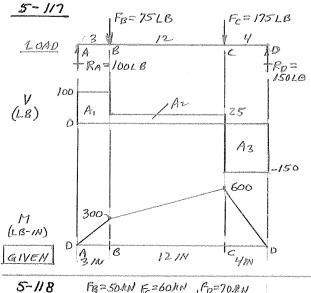


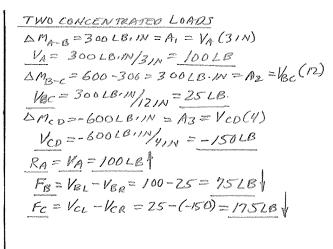


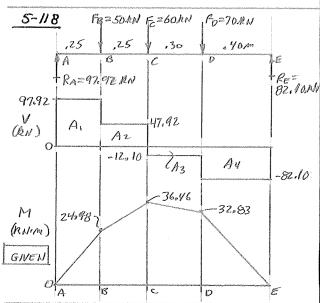
 $R_A = V_A = 4050 LB^{\dagger}$ NO LOND FROM A -B $R_C = V_C = 6750 LB^{\dagger}$ V DROPS: 4050 + 6750 = 10800 LB IN 9 FT $LV = \frac{\Delta V}{\Delta X} = \frac{10800 LB}{9.0 FT} = 1260 LB/FT$ X_1 WHERE V - C URVE CROSSES AXIS $X_1 = \frac{\Delta V}{L} = \frac{4050 LB}{1200 LB/FT} = \frac{3.375}{5.625}$ FT $X_2 = 9.0$ FT $-X_1 = 9.0 - 3.375 = 5.625$ FT $A_1 = (4050 LB)(3FT) = 12.150 LB - FT = MB$ $A_2 = \frac{1}{2}(4050)(3.375) = 6834.4 LB - FT$ $A_3 = \frac{1}{2}(-6750)(5.625) = 18984.4 LB - FT$ $M_D = MB + A_2 = 12.150 + 6834.4 = 18984.4 LB - FT$ $M_C = MD + A_3 = 18984.4 - 18984.4 = 0 LB - FT$

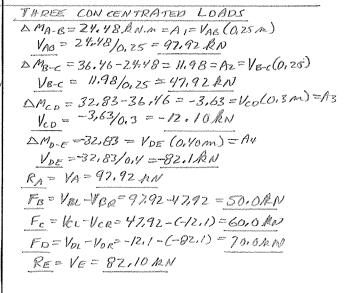


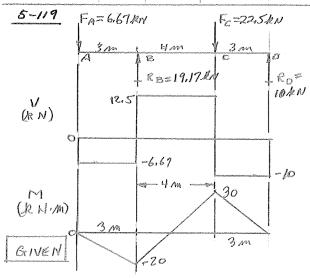
 $BA = V_A = 1342.5 N$ $Fe = V_C = 570 N$ No LOAD FROM B-C. V DROPS! 1342.5 - 570 = 772.5 N IN 0.75 M $W = \frac{\Delta V}{\Delta X} = \frac{772.5 N}{0.75 m} = 1030 N/m$ REACTION MOMENT MA REQUIRED MA = (1030 N/m)(0.75 m)(0.75 m) + (570 N)(12 m) MA = (1030 N/m)(0.75 m)(0.75 m) + (570 N)(12 m) MA = 973.7 N I M = 10 $A_1 = \frac{1}{2}(172.5)(0.75) = 289.7 N I M$ $A_2 = (570)(0.75) = 427.5 N I M$ $A_3 = (570)(0.75) = 256.5 N I M$ $M_3 = M_4 + A_1 + A_2 = -973.7 + 289.7 + 427.5$ $M_4 = -256.5 N I M$ $M_5 = M_6 + A_3 = -256.5 + 256.5 = 0 N I M$





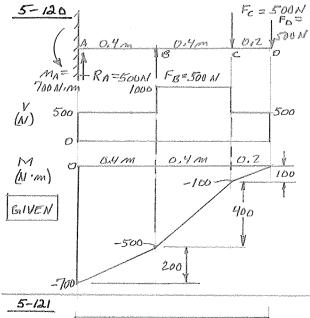


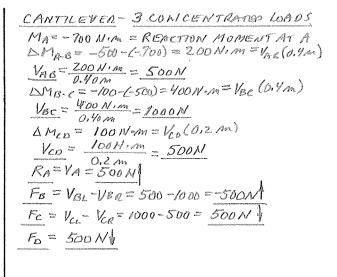


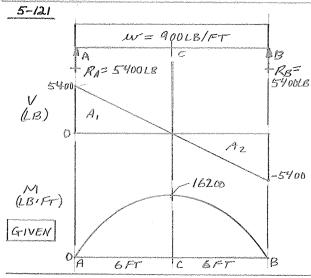


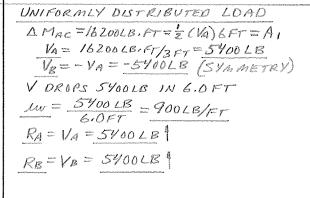
 $\Delta M_{AB} = -20kN \cdot m = V_{AB}(3m)$ $V_{AB} = 20kN \cdot m/3m = -6.66kN$ $\Delta M_{BC} = 30 - (-20) = 50kN \cdot m = V_{BC}(4m)$ $V_{BC} = 50/y = 12.5kN$ $\Delta M_{CD} = -30/kN \cdot m = V_{CO}(3m)$ $V_{CD} = -30/3 = -10.0kN$ $F_{A} = V_{A} = -6.67kN + \frac{1}{2}$ $R_{B} = V_{BC} = V_{BC} = 12.5 - (-6.67) = 19.17kN$ $F_{C} = V_{CR} - V_{CL} = 12.5 - (-10) = 22.5kN$ $R_{D} = V_{D} = 10kN$

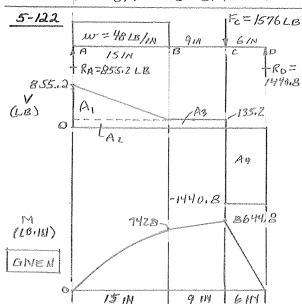
TINO CONCENTRATED LOADS - OVERHANG











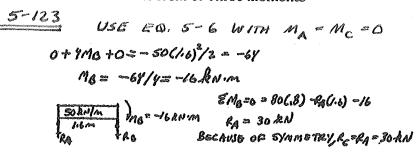
PARTIAL UNIFORMY DISTOC, LOAD + CONC, LOAD

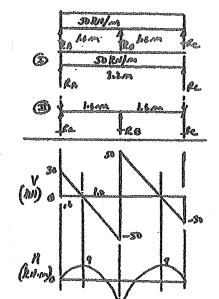
FROM D TO LEFT:

\[
\Delta M_{20} = 8644.8 \text{LB.IN} = V_{c0}(61N) = A4
\]
\[
V_{c0} = \frac{-8644.8 \text{LB.IN}}{61N} = -1440.8 \text{LB}
\]
\[
\Delta M_{BC} = 8644.8 \text{-7428.0} = 12/6.8 = A3 = \text{V_c}(\text{Ain})
\]
\[
V_{BC} = \frac{12/6.8 \text{LB.IN}}{91N} = \frac{135.2 \text{LB}}{135.2 \text{LB}}
\]
\[
\Delta M_{AB} = \frac{7428 \text{LB.IN}}{91N} = \frac{A1 + A2}{2028 \text{LB.IN}}
\]
\[
\Delta = \frac{7428 \text{LB.IN}}{91N} = \frac{7428 - 2028 = 5400 \text{LB.IN}}{91N}
\]
\[
\Delta = \frac{5400 + 1014}{2500} = \frac{855.2 \text{LB}}{1500}
\]
\[
V DROPS \text{BS5.12} - \frac{135.2}{135.2} = \frac{720 \text{LB.IN}}{1500}
\]
\[
\Delta = \frac{72018/5}{150} = \frac{4818/1N}{810}
\]
\[
\Delta = \frac{72018/5}{150} = \frac{7816/5}{150} = \frac{7490.815}{150} = 1576 \text{LB}}
\]
\[
\Delta = \frac{72018/5}{150} = \frac{72018}{150} = \fra

Continuous Beams - Theorem of Three Moments

R6= 50 (3,2) - 2(30) = 100 AN





5-124

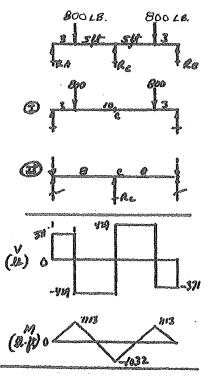
USE EQ(5-7) WITH MA=ME=0

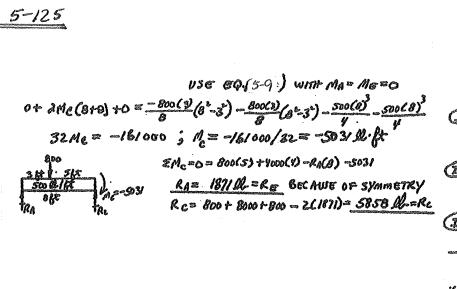
or
$$2M_{\rm C}$$
 (8+0) +0 = $-\frac{800(3)}{8}(8^2-3^2) - \frac{800(3)}{8}(8^2-3^2)$

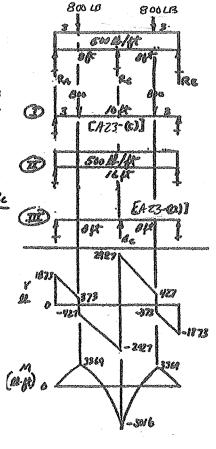
32 Mg = -33000 3 Mg = -33000/32= -103/ lb-ft Note: Mc IS THE MOMENT AT THE MIDGE SUPPORT, SUBSCRIPT IN EQ.(5-7) WERE ADJUSTED TO MATCH FIG. P5-124.

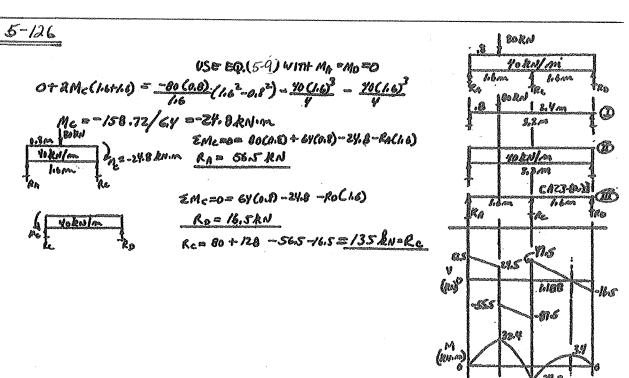
FOR REACTIONS:

800 $EM_{c}=0=800(s)-R_{A}(8)=1031$ $R_{A}=(8000-1031)/8=37188=R_{A}$ $R_{C}=0=800(s)-R_{0}(0)-1031$ $R_{C}=37188$ $R_{C}=37188$ $R_{C}=1600-2(371)=85888=R_{C}$

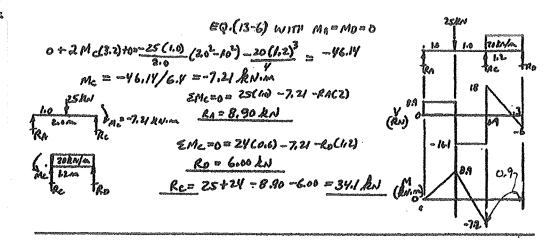




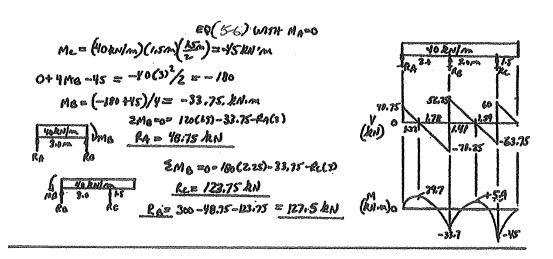




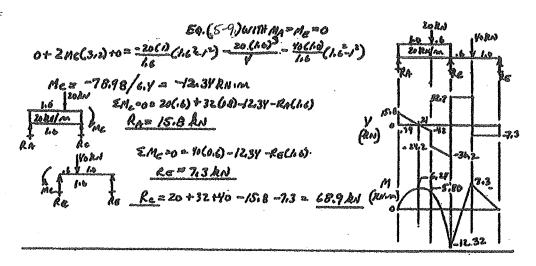
5-127

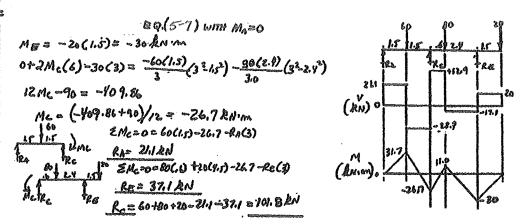


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5-129





CHAPTER 6 Centroids and Moments of Inertia of Areas

Notes concerning the format of solutions for Chapter 6 problems:

- Problem solutions for the moments of inertia of the shapes shown in Figures p₆₋₁ through p₆₋₄₈ are shown in the tabular format recommended in Section ₆₋₆,
- Calculations were completed using a spreadsheet.
- The requested result includes the vertical Y distance to the centroidal axis from the reference axis and the moment of inertia I of the composite shape relative to the horizontal centroidal axis.
- In most problems, the reference axis for computing the location of the horizontal centroidal axis was taken as the base of the section. Exceptions are noted on the top or bottom lines of the solution. For example, in Figure P6-17 the reference axis is at the axis of symmetry at the mid-height of the shape, found by inspection.
- The left-most column of the solution gives a brief description of the part of the composite shape being analyzed.
- For some shapes, internal parts removed from the outer shape are shown to be negative.
- For composite shapes having parts that are commercially available structural shapes, pipes, or tubes, or wood beams, reference should be made to the Appendix tables for pertinent data.

FIGURE DA 4		la abaa	NOTE: D-4					
FIGURE P6-1	Units:	Inches	NOTE: Refere				1 . 4 140	
Part	Area	у	Ay	lc	d	Ad^2	lc+Ad^2	
1-Vertical	0.5000	1.0000	0.5000	0.16670	0.3365	0.0566	0.2233	
2-Horizontal	0.3125	0.1250		0.00163	0.5384	0.0906	0.0922	
Total area =		Sum Ay=	0.5391			Total I =	0.3156	in^4
Υ=	0.6635	in						
FIGURE P6-2	Units:	Inches	NOTE: 6x8 re	ectangle with 5	ix6 rectan	ale removed		
Part	Area	у	Ау	lc	d	Ad^2	lc+Ad^2	
1-Total 6x8	48.00	4.00	192.00	256.00	0.00	0.00	256.00	
2-Void 5x6	-30.00	4.00	-120.00	-90.00	0.00	0.00	-90.00	
Total area =		Sum Ay=	72.00	00.00	0.00	Total I =	166.00	in^4
Y=		•	NOTE: Refere	ence axis is ha	se of the		100.00	,
,_						опаро		
FIGURE P6-3	Units:	Inches	NOTE: 6x8 re	ectangle with 4	x6 rectan	gle removed		
Part	Area	у	Ау	lc	d	Ad^2	lc+Ad^2	
1-Total 6x8	48.00	4.00	192.00	256.00	0.00	0.00	256.00	
2-Void 4x6	-24.00	4.00	-96.00	-72.00	0.00	0.00	-72.00	
Total area =	24.00	Sum Ay=	96.00			Total I =	184.00	in^4
Y=	4.00	in	NOTE: Refere	ence axis is ba	se of the	shape		
FIGURE P6-4	Units:	mm	NOTE: Refere	ence axis is ba	se of the	shape		
Part	Area	у	Ау	lc	d	Ad^2	lc+Ad^2	
1-Vertical	5000	100	5.000E+05	1.667E+07	52.50	1.38E+07	3.04E+07	
2-Horizontal	4375	213	9.297E+05	2.279E+05	60.00	1.58E+07	1.60E+07	
Total area =	9375	Sum Ay=	1.430E+06			Total I =	4.64E+07	mm^4
Υ=	152.50	mm						
FIGURE DO E								
FIGURE P6-5	Units:		NOTE: Refere			•		
Part	Area	у	Ay	lc = coo=.o.	d	Ad^2	lc+Ad^2	
1-Vertical	250	30.0	7.500E+03	5.208E+04	5.00		5.83E+04	
2-Horiz-bot	100	2.5	2.500E+02	2.080E+02	32.50		1.06E+05	
3-Horiz-top	200	57.5	1.150E+04	4.170E+02	22.50	1.01E+05	1.02E+05	
Total area =		Sum Ay=	1.925E+04		•	Total I =	2.66E+05	mm^4
Y≕	35.00	mm						

FIGURE P6-6	Units:	mm	NOTE: Both	vertical rectang	gles (10x3	30) combined		
Part	Area	у	Ау	lc	d	Ad^2	lc+Ad^2	
1-Ver-20X30	600	15	9.000E+03	4.500E+04	2.50	3.75E+03	4.88E+04	
2-Hor-20X10	200	5	1.000E+03	1.667E+03	7.50	1.12E+04	1.29E+04	
Total area =	800	Sum Ay=	1.000E+04			Total I =	6.17E+04	mm^4
Y=	12.50	-		ence axis is ba	se of the	shape		
FIGURE P6-7	Units:	mm	NOTE: Entire	vertical stem;	2 horiz.	flanges each	1 5x15	
Part	Area	у	Ay	lc	d	Ad^2	lc+Ad^2	
1-Ver-5X40	200	20.0	•	2.667E+04	0.00	0E+00	2.67E+04	
2-Horiz-bot	75	2.5	1.875E+02	1.562E+02	17.50	2.30E+04	2.31E+04	
3-Horiz-top	75	37.5	2.812E+03	1.562E+02	17.50	2.30E+04		
Total area =	350	Sum Ay=				Total I =	7.29E+04	mm^4
Y=	20.00	•		ence axis is ba				
FIGURE P6-8	Units:	mm	NOTE: Refere	ence axis is ba	se of the	shape		
Part	Area	у	Ay	lc	d	Ad^2	lc+Ad^2	
1-Ver-5X40	200	20.0	4.000E+03	2.667E+04	0.00	0E+00		
2-Ver-5x40	200	20.0		2.667E+04	0.00	0E+00		
3-Hor-30x5	150	20.0		3.125E+02	0.00	0E+00	3.12E+02	
Total area =		Sum Ay=	1.100E+04			Total I =	5.36E+04	mm^4
Y=	20.00	-	77.7002		-	rotur i	5.00L · 04	11011 4
			•					
FIGURE P6-9	Units:	mm	NOTE: Refere	ence axis is bas	se of the s	shape		
Part	Area	у	Ау	lc	d	Ad^2	lc+Ad^2	
1-Ver-5X30	150	20.0	3.000E+03	1.125E+04	0.00	0E+00	1.12E+04	
2-Horiz-bot	200	2.5	5.000E+02	4.167E+02	17.50	6.12E+04	6.17E+04	
3-Horiz-top	200	37.5	7.500E+03	4.167E+02	17.50	6.12E+04	6.17E+04	
Total area =	550	Sum Ay=	1.100E+04		-	Total I =	1.35E+05	mm^4
Y≕	20.00	mm						
FIGURE P6-10	Units:	mm	NOTE: Refere	ence axis is bas	se of the s	shape		
Part	Area	у	Ау	lc	đ	Ad^2	lc+Ad^2	
1-Ver-5X50	250	30.0	7.500E+03	5.208E+04	0.00	0E+00	5.21E+04	
2-Horiz-bot	140	2.5	3.500E+02	2.917E+02	27.50	1.06E+05	1.06E+05	
3-Horiz-top	140	57.5	8.050E+03	2.917E+02	27.50	1.06E+05	1.06E+05	
Total area =	530	Sum Ay=	1.590E+04		-	Total I =	2.64E+05	mm^4
Y=	30.00	mm						

	FIGURE P6-11	Units:	mm	NOTE: Bott	n vert. combine	d 10v45.	hariz flanca	a aambinad	Ev.20
	Part	Area		Ay	lc	d d	Ad^2		5X30
	1-Ver-10X45	450	у 22.5	•				Ic+Ad^2	
	2-Hor-5x30	150	2.5			0.69		7.62E+04	
						19.31			
	3-Hor-5x25	125				20.69			
	Total area =		Sum Ay=				Total I =	1.86E+05	mm^4
	Y=	21.81	mm	NOTE: Here	rence axis is ba	ase of the	shape		
	FIGURE P6-1:	2 Units:	mm	NOTE: All v	erticals massed	l toaether			
٠.	Part	Area	у	Ay	lc	d	Ad^2	lc+Ad^2	
	1-Ver-16X16	256	. 8	•		4.39	4.92E+03	1.04E+04	
	2-Hor-4X50	200	18			5.61	6.30E+03	6.57E+03	
	Total area =		Sum Ay=			2.0.	Total I =	1.70E+04	mm^4
	Υ=	12.39	•		rence axis is ba	se of the			
	FIGURE P6-13	Units:	mm	NOTE: Refe	rence axis is ba	se of the	shape		
	Part	Area	у	Ау	lc	d	Ad^2	lc+Ad^2	
	1-Hor-5x10	50	2.5	1.250E+02	1.045E+02	20.83	2.17E+04	2.18E+04	
	2-Ver-5X55	275	27.5	7.562E+03	6.932E+04	4.17	4.77E+03	7.41E+04	
	3-Hor-5x20	100	27.5	2.750E+03	2.083E+02	4.17	1.74E+03	1.94E+03	
	4-Ver-5x30	150	15.0	2.250E+03	1.125E+04	8.33	1.04E+04	2.17E+04	
	5-Hor-5x5	25	52.5	1.312E+03	5.208E+01	29.17	2.13E+04	2.13E+04	
	Total area =	600	Sum Ay=	1.400E+04			Total I =	1.41E+05	mm^4
	Y=.	23.33	mm						
	FIGURE P6-14	12-2-	1 1	NOTE D.		•			
		Units:			rence axis is ba		-	1	
	Part	Area	у .	Ay	lc 0.00170	d	Ad^2	lc+Ad^2	
	1-Bot plate	0.5200	0.1000	0.0520		0.4330	0.0975	0.0992	
	2-Bot flanges	0.1200	0.2500	0.0300		0.2830	0.0096	0.0097	
	3-2 Vert webs	0.3000	0.9500	0.2850		0.4169	0.0522	0.1084	
	4-Horiz-top	0.12	1.65	0.1980	0.0001	1.1170	0.1497	0.1498	
	Total area =	1.06	Sum Ay=	0.5650			Total I =	0.3672	in^4
	Y=	0.5330	in						
	FIGURE P6-15	Units:	Inches	NOTE: Refer	ence axis is ba	se of the	shape		
	Part	Area	у	Ay	lc	d	Ad^2	lc+Ad^2	
	1-Bot flange	0.1000	0.0500	0.0050	0.00008	1.0176	0.1036	0.1036	
	2-2 Verticals	0.4800	1.2000	0.5760	0.23040	0.1323	0.0084	0.2388	
	3-Mid-Horiz.	0.1	1.4500	0.1450	0.0000833	0.3823	0.0146	0.0147	
	Total area =	0.68	Sum Ay=	0.7260			Total I =	0.3572	in^4
	Y =	1.0676	in						

FIGURE P6-1	6 Units:	Inches	NOTE: Refere	ence axis is ba	se of the	shape		
Part	Area	у	Ау	lc	d	Ad^2	Ic+Ad^2	
1-Rectangle	1.1250	0.7500	0.8438	0.21094	0.1491	0.0250	0.2360	
2-Semicircle	0.2209	1.6590	0.3665	0.0022148	0.7598	0.1275	0.1297	
Total area =	1.34589	Sum Ay=	1.2102			Total I =	0.3657	in^4
Y=	0.8992	in						
					·			
FIGURE P6-17	7 Units:	mm	NOTE: Refere	nce axis taker	at y=125			
Part	Area	у	Ау	lc	d	Ad^2	lc+Ad^2	
1-Rectangle	11400	0.0	0E+00	3.430E+07	0.00	0E+00	3.43E+07	
2-Semic-bot	1414	-107.7	-1.52E+05	9.072E+04	107.72	1.64E+07	1.65E+07	
3-Semic-top	1414	107.7	1.52E+05	9.072E+04	107.72	1.64E+07	1.65E+07	
Total area =	14227	Sum Ay=	0E+00			Total I =	6.73E+07	mm^4
Y=	0.00	mm						
FIGURE P6-1	8 Units:	mm	NOTE: Refere	ence axis is ba	ise of the s	shape		
Part	Area	у	Ау	lc	d	Ad^2	Ic+Ad^2	
1-Rectangle	1200	20.0	2.400E+04	1.60E+05	7.27	6.35E+04	2.23E+05	
2-Rect rem.	-400	20.0	-8.00E+03	-1.33E+04	7.27	-2.1E+04	-3.4E+04	
3-Triangle	300	46.7	1.40E+04	6.67E+03	19.39	1.13E+05	1.20E+05	
Total area =	1100	Sum Ay=	3.000E+04			Total I =	3.08E+05	mm^4
Y=	27.27	mm						
FIGURE P6-1		Inches	NOTE: Refere			•		
Part	Area	у	Ау	lc	d	Ad^2	ic+Ad^2	
1-Hor5x1.4	0.700	0.250	0.1750	0.0146	0.681	0.3242	0.3388	
2-Ver6x2.5	1.500	1.250	1.8750	0.7813	0.319	0.1531	0.9343	
3-2 Tr7x1.5	0.910	0.933	0.8493	0.0854	0.003	0.0000	0.0854	
4-Tri-rem	-0.460	0.807	-0.3711	-0.0216	0.124	-0.0071	-0.0287	
5-Hole-rem	-0.049	2.200	-0.1080	-0.0002	1.269	-0.0791	-0.0793	
Total area =		Sum Ay=	2.4202			Total I =	1.2506	in^4
Υ=	0.9305	in						
FIGURE P6-2	O Haisas	laches	NOTE: Defeue	ann auin in ba				
1	*	Inches	NOTE: Refere			•	las AdAO	
Part	Area	y 1,0000	Ay	lc 0.4000	d 0.2700	Ad^2	lc+Ad^2	
1-2 Vert rect	1.2000	1.0000	1.2000	0.4000	0.2798	0.0940	0.4940	
2-2 Triangles	0.5100	1.1333	0.5780	0.0819	0.1465	0.0109	0.0928	
3-Top3x2.4	0.7200	1.8500	1.3320	0.0054	0.5701	0.2341	0.2395	in A 4
Total area =	2.4300	Sum Ay=	3.1100			Total I =	0.8263	#1"4
Υ=	1.2798	Ħ.J						

FIGURE P6-21	Units:	Inches	NOTE: Referen	ice axis is bas	se of the si	nape		
Part	Area	у	Ay	lc	đ	Ad^2	Ic+Ad^2	
1-Vert rect	8.2500	4.2500	35.0625	20.7969	0	0.0000	20.7969	
2-Bot flange	5.2500	0.7500	3.9375	0.9844	3,5	64.3125	65.2969	
3-Top flange	5.2500	7.7500	40.6875	0.9844	3.5	64.3125	65.2969	
Total area =	18.7500	Sum Ay=	79.6875			Total I =	151.3906	in^4
Y=	4.2500	in						

,	FIGURE P6-22	Units:	Inches	NOTE: 7.25x7	rectangle v	with 4.25x5.5	rectangle	removed
	Part	Area	у	Ау	lc	d	Ad^2	Ic+Ad^2
	1-Tot 7.25x7	50.75	3.50	177.63	207.23	0.00	0.00	207.23
	2-4.25x5.5 r€	-23.38	3.50	-81.81	-58.92	0.00	0.00	-58.92
	Total area =	27.38	Sum Ay=	95.81			Total I =	148.30 in^4
	Y ==	3.50	in	NOTE: Referen	ce axis is ba	ase of the sha	ape	

FIGURE P6-23	Units:	Inches	NOTE: 24x4.5	rectangle wi	th 21x3.5	rectangle re	emoved	
Part	Area	у	Ay	Iç	d	Ad^2	Ic+Ad^2	
1-Tot 24x4.5	108.00	2.25	243.00	182.25	0.00	0.00	182.25	
2-21x3.5 rem	-73.50	2.25	-165.38	-75.03	0.00	0.00	-75.03	
Total area =	34.50	Sum Ay=	77.63			Total I =	107.22	in^4
Y==	2.25	in	NOTE: Referen	ce axis is bas	se of the s	hape		

FIGURE P6-24	Units:	Inches	NOTE: Referen	ce axis is bas	xis is base of the shape			
Part	Area	у	Ау	lc	d	Ad^2	Ic+Ad^2	
1-2 Verticals	33.75	5.63	189.84	355.96	2.13	152.40	508.36	
2-Top flange	16.88	12.00	202.50	3.16	4.25	304.80	307.97	
Total area =	50.63	Sum Ay=	392.34			Total ! =	816.33	in^4
Y==	7.75	in						

FIGURE P6-25	Units	: Inches	NOTE: Beam depth = 13.7 in;Ref axis=centroid;7.35 in from bot						
Part	Area	у	Ay	Ic	d	Ad²	$I_c + Ad^2$		
1-W14x43	12.60	0.00	0.00	428.00	0.00	0.00	428.00	- Carlotte Comment of the Comment of	
2-bot plate	4.00	-7.10	-28.40	0.0833	7.10	201.64	201.72		
3-top plate	4.00	7.10	28.40	0.0833	7.10	201.64	201.72		
Total area =	20.60	Sum Ay =	0.00			Total I =	831.45	in ⁴	
Y	0.00	Inches							

FIC	SURE P6-26	Units:	Inches	NOTE: Reference axis is base of the shape						
	Part	Area	У	Ау	I _c	d	Ad²	$l_c + Ad^2$		
Patroposia	1-S12x50	14.600	6.000	87.600	303.00	1.913	53.43	356.43	og 1994 of the second s	
**************	2-C12x25	7.350	11.713	86.091	4.45	3.800	106.13	110.58		
	Total area =	21.950	Sum Ay =	173.691			Total I =	467.01	in ⁴	
	Y =	7.913	Inches	NOTE: Web f	or C is 0.387	thick: Y-Y	axis down 0.6	74 from ton		

NOTE: Web for C is 0.387 thick; Y-Y axis down 0.674 from top NOTE: For Channel; y = 12.0 + 0.387 - 0.674 = 11.713 in

FIGURE P6-27	Units:	Inches	NOTE: Reference axis is base of the shape					
Part	Area	у	Ау	Ic	d	Ad^2	lc+Ad^2	
1-l12x14.292	12.15	6.00	72.92	317.33	1.40	23.73	341.06	
2-Top plate	3.50	12.25	42.88	0.07	4.85	82.41	82.49	
Total area =	15.65	Sum Ay=	115.79			Total I =	423.55	in^4
Y= -	7.40	in						

1	FIGURE P6-2	8 Units:	Inches	NOTE: Depth	of C12 is12.0	; Ref. axis	at centroic	t;y=6.50 from	bot
	Part	Area	У	Ау	lc	d	Ad^2	lc+Ad^2	
	1-Two C12	14.07	0.00	0.00	319.520	0.00	0.00	319.52	
	2-Bot plate	5.00	-6.25	-31.25	0.104	6.25	195.31	195.42	
	3-Top plate	5.00	6.25	31.25	0.104	6.25	195.31	195,42	
	Total area =	19.07	Sum Ay=	0.00			Total I =	710.35 ir	1^4
	Y=	0.00	in						•

FIGURE P6-29	Units	: Inches	in from bot					
Part	Area	у	Ау	I _c	d	Ad²	$I_c + Ad^2$	
1 Vert plate	3.00	0.000	0.00	9.00	0.000	0.000	9.000	
2-Bot angles (2)	2.74	-2.368	-6.49	0.9520	2.368	15.364	16.316	
3-Top angles (2)	2.74	2.368	6.49	0.9520	2.368	15.364	16.316	
4-Top plate	2.25	3.250	7.31	0.0469	3.250	23.766	23.813	
5-Bot plate	2.25	-3.250	-7.31	0.0469	3.250	23.766	23.813	
Total area =	12.980	Sum Ay =	0.00		The second se	Total I =	89.258	in⁴
Y = 0.00 Inches NOTE: For Angle; y = 3.50 - 0.50 - 0.632 = 2.638 in								

FIGURE P6-30	Units	: Inches	NOTE: Overall depth = 6.0 in; Ref axis=centroid; 3.0 in from bot						
Part	Area	у	Ay	I _c	d	Ad²	$I_c + Ad^2$	The second secon	
1-Vert plates (2)	3.000	0.000	0.000	9.000	0.000	0.000	9.000	THE PERSON NAMED IN COLUMN	
2-bot channel	1.760	-2.545	-4.479	0.300	2.545	11.3996	11.6996		
3-top channel	1.760	2.545	4.479	0.300	2.545	11.3996	11.6996		
Total area =	6.520	Sum Ay =	0.000			Total I =	32.3991	in ⁴	
Y	0.00	Inches							

FIGURE P6-31	Units	: Inches	NOTE: Ref axis=centroid; 3.0 in from center of either pipe						
Part	Area	у	Ay	l _c	d	Ad ²	I _c + Ad ²		
1-Vert plate	2.050	0.000	0.000	2.8717	0.000	0.000	2.872	MONOTON COMMENTS OF THE PARTY O	
2-bot pipe	0.799	-3.000	-2.397	0.3099	3.000	7.1910	7.5009		
3-top pipe	0.799	3.000	2.397	0.3099	3.000	7.1910	7.5009		
Total area =	3.648	Sum Ay =	0.000			Total I ≡	17.8735	in ⁴	
ΥΞ	0.00	Inches	NOTE: Length	n of plate = 6	.00 - pipe d	dia = 6.00 - 1.9	90 = 4.10 in		

FIGURE P6-32	Units	Inches	NOTE: Refer	NOTE: Reference axis=centroid= 12 in from CL of pipes					
Part	Area	У	Ay	I _c	d	Ad²	$I_c + Ad^2$	Committee of the Commit	
1-Top pipes (2)	4.4560	12.0000	53.4720	6.0340	12.00	641.66	647.70		
2-Bot pipes (2)	4.4560	-12.0000	-53.4720	6.0340	12.00	641.66	647.70		
Total area =	8.9120	Sum Ay =	0.0000			Total I =	1295.40	in⁴	
Υ=	0.0000	Inches							

FIGURE P	3-33	Units:	Inches	NOTE: Ref a	xis at base of	shape			
Part		Area	у	Ау	I _c	d	Ad²	$I_c + Ad^2$	Oxyderation and an authorized participation of the control of the
1-Base pl	late	2.500	0.125	0.313	0.0130	2.592	16.800	16.813	
2-Angles	(2)	3.380	1.470	4.969	5.5000	1.247	5.2582	10.7582	
3-top pla	ate	6.000	4.500	27.000	0.1250	1.783	19.0689	19.1939	
Total a	rea =	11.880	Sum Ay =	32.281			Total I =	46.7646	in ⁴
	γ =	2.717	Inches						•••

FIGURE P6-34	Units	Inches	NOTE: Reference axis=centroid= 3.00 in from bottom						
Part	Area	у	Ау	l_{c}	d	Ad²	$I_c + Ad^2$	W. M. Company of the	
1-Channel	3.830	0.000	0.000	17.300	0.000	0.000	17.300	**************************************	
2-Channel	2.830	0.000	0.000	17.300	0.000	0.000	17.300		
Total area =	6.660	Sum Ay =	0.000			Total =	34,600	in ⁴	
Y =	0.0000	Inches					000	•••	

FIGURE P6-35	Units	Inches	NOTE: Ref a	xis at base of	shape			
Part	Area	у	Ау	I _c	d	Ad²	$I_c + Ad^2$	ANTO-OCT SEALON SERVICE SERVIC
1-Angles (2)	1.888	0.586	1.106	0.6920	2.023	7.730	8.422	the state of the s
2-Bot channel	2.640	0.478	1.262	0.6240	2.131	11.9931	12.6171	
3-Vert webs (2)	4.500	3.000	13.500	13.5000	0.391	0.6866	14.1866	
4-Top channel	2.640	5.522	14.578	0.6240	2.913	22.3959	23.0199	
Total area =	11.668	Sum Ay =	30.446	Control of the Contro	THE PARTY OF THE P	Total I =	58.2452	in ⁴
Y	2.609	Inches					oo.m.tob	21 8

FIGURE P6-36	Units	Inches	NOTE: Reference axis is bases of shape						
Part	Area	у	Ау	l _c	d	Ad²	$I_c + Ad^2$	Постанова по предостава и постанова предостава и постанова предостава и постанова постанова и постанова и пост Постанова постанова и пост	
1-W6x15	4.430	2.995	13.268	29.100	0.642	1.827	30.927		
Angles (2)	1.888	0.846	1.597	0.692	1.507	4.287	4.979		
Total area =	6.318	Sum Ay =	14.865			Total I =	35.906	in ⁴	
Ϋ́Ξ	2.3528	Inches					00.000	•••	

FIGURE P6-37	Units	Inches	NOTE: Reference axis is bases of shape						
Part	Area	у	Ау	I _c	d	Ad²	$I_c + Ad^2$	and the second second second	
1-Bot tube	2.440	2.000	4.880	4.490	1.500	5.490	9.980	William barbones to organiza	
2-Top tube	2.440	5.000	12.200	1.480	1.500	5.490	6.970		
Total area =	4.880	Sum Ay =	17.080			Total I =	16.950	in ⁴	
Y =	3.5000	Inches					.0.000		

FIGURE P6-38	Units	: Inches	NOTE: Ref a	axis at base of	shape			
Part	Area	у	Ay	l _c	d	Ad²	$I_c + Ad^2$	
1-6x6x1/2	9.740	3.000	29.220	48.3000	0.051	0.025	48.325	Principle of the challenge of the control of the co
2-4x2x1/4	2.440	1.465	3.575	1.4800	1.484	5.3736	6.8536	
3-3x2x1/4	1.970	4.535	8.934	1.1100	1.586	4.9552	6.0652	
Total area =	14.150	Sum Ay =	41.729			Total =	61.2442	in ⁴
Y	2.949	Inches	NOTE: Use	design wall thic	kness for	$6x6x1/2$; $t_w =$	0.465 in	

FIGURE P6-39	Water Commence of the Commence	: Inches	NOTE: Ref a:	Carried Control of Carried Control of Contro	Contraction of the Contraction o	A 22		
Part	Area	У	Ay	l _c	d	Ad²	$I_c + Ad^2$	VVIII TABORAL QUORNOQUI
1-Bot channel	1.590	0.457	0.727	0.3120	2.904	13.411	13.723	
2-6x2x1/4	3.370	3.184	10.730	13.1000	0.177	0.1058	13.2058	
3-Toop channel	1.590	6.641	10.559	0.3120	3.280	17.1037	17.4157	- A
Total area = Y =	6.550 3.361	Sum Ay =	22.016			Total I =	44.3442	in ⁴
¥ moon	3.301	Inches						
FIGURE P6-40	Units	: Inches	NOTE: Refer	ence axis is b	ases of sl	nane		
Part	Area	y	Ay	I _c	d	Ad²	$I_c + Ad^2$	
1-Bot channel	1.881	0.730	1.373	0.980	0.321	0.193	1.173	in minamone.
2-Top I-beam	1.726	1.400	2.416	0.680	0.349	0.211	0.891	
Total area =	3.607	Sum Ay =	3.790	THE PROPERTY OF THE PROPERTY O		Total I =	2.064	in ⁴
Υ=	1.0506	Inches					22.00-4	***
PIOUP PA 11								
FIGURE P6-41 Part	engaggianus an anna taga de describer.	Inches	NOTE: Refer	The space of the first section of the state		nape Ad ^z	1 . ^ 12	
	Area	y 2.450	Ay	l _c	d		$I_c + Ad^2$	managa da
1-W12x30 2-C6x13	8.790	6.150	54.059	238.000	2.022	35.953	273.953	
THE PARTY OF THE P	3.830	12.814	49.078	1.050	4.642	82.514	83.564	- 1
Total area =	12.620	Sum Ay =	103,136			Totalle	267 647	in ⁴
Y=	8.1724	Inches	NOTE: depth	of W-beam =	: 12,3 in	Total I =	357.517	***
FIGURE P6-42	Units	Inches	NOTE: depth	kis=centroid o	of W-shape	e		okanika enorana wazana
FIGURE P6-42 Part	Units: Area	Inches	NOTE: depth NOTE: Ref ax	xis=centroid c	of W-shape	e Ad²	I _c + Ad ²	olanio miero cararez sez sez s
FIGURE P6-42 Part 1-W4x13	Units: Area 3.830	Inches y 0.000	NOTE: depth NOTE: Ref av Ay 0.000	kis=centroid c	of W-shape d 0.000	e Ad² 0.000	l _c + Ad ² 11.300	
Part 1-W4x13 2-bot tube	Units: Area 3.830 2,440	y 0.000 -3.080	NOTE: depth NOTE: Ref av Ay 0.000 -7.515	kis=centroid c I _c 11.3000 1.4800	of W-shape d 0.000 3.080	Ad ² 0.000 23.1468	I _c + Ad ² 11.300 24.6268	milijanismi e essaman escressor. Samus del signa ginnepsus, induses
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube	Units: Area 3.830 2.440 2.440	y 0.000 -3.080 3.080	NOTE: depth NOTE: Ref av Ay 0.000 -7.515 7.515	kis=centroid c	of W-shape d 0.000	Ad ² 0.000 23.1468 23.1468	I _c + Ad ² 11.300 24.6268 24.6268	artikalar sekencense sette samen sette
Part 1-W4x13 2-bot tube 3-top tube Total area =	Units: Area 3.830 2.440 2.440 8.710	y 0.000 -3.080 3.080 Sum Ay =	NOTE: depth NOTE: Ref av Ay 0.000 -7.515 7.515 0.000	kis=centroid o I _c 11.3000 1.4800 1.4800	of W-shape d 0.000 3.080 3.080	Ad ² 0.000 23.1468	I _c + Ad ² 11.300 24.6268	in ⁴
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube	Units: Area 3.830 2.440 2.440	y 0.000 -3.080 3.080	NOTE: depth NOTE: Ref av Ay 0.000 -7.515 7.515	kis=centroid o I _c 11.3000 1.4800 1.4800	of W-shape d 0.000 3.080 3.080	Ad ² 0.000 23.1468 23.1468	I _c + Ad ² 11.300 24.6268 24.6268	and a description of the contract of the contr
Part 1-W4x13 2-bot tube 3-top tube Total area =	Units: Area 3.830 2.440 2.440 8.710 0.00	y 0.000 -3.080 3.080 Sum Ay =	NOTE: depth NOTE: Ref av Ay 0.000 -7.515 7.515 0.000	kis=centroid o I _c 11.3000 1.4800 1.4800 of W-beam =	of W-shape d 0.000 3.080 3.080 4.16 in	Ad ² 0.000 23.1468 23.1468 Total I =	I _c + Ad ² 11.300 24.6268 24.6268 60.5536	and a description of the contract of the contr
Part 1-W4x13 2-bot tube 3-top tube Total area = Y =	Units: Area 3.830 2.440 2.440 8.710 0.00	y 0.000 -3.080 3.080 Sum Ay = Inches	NOTE: depth NOTE: Ref a) Ay 0.000 -7.515 7.515 0.000 NOTE: depth	kis=centroid o I _c 11.3000 1.4800 1.4800 of W-beam =	of W-shape d 0.000 3.080 3.080 4.16 in	Ad ² 0.000 23.1468 23.1468	I _c + Ad ² 11.300 24.6268 24.6268 60.5536	artikalar sekencense sette samen sette
Part 1-W4x13 2-bot tube 3-top tube Total area = Y =	Units: Area 3.830 2.440 2.440 8.710 0.00 Units:	y 0.000 -3.080 3.080 Sum Ay = Inches	NOTE: depth NOTE: Ref av Ay 0.000 -7.515 7.515 0.000 NOTE: depth	cis=centroid of I _c 11.3000 1.4800 1.4800 of W-beam =	of W-shape d 0.000 3.080 3.080 4.16 in	Ad ² 0.000 23.1468 23.1468 Total I =	I _c + Ad ² 11.300 24.6268 24.6268 60.5536	and a description of the contract of the contr
Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part	Units: Area 3.830 2.440 2.440 8.710 0.00 Units: Area	y 0.000 -3.080 3.080 Sum Ay = Inches	NOTE: depth NOTE: Ref av Ay 0.000 -7.515 7.515 0.000 NOTE: depth	kis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam =	of W-shape d 0.000 3.080 3.080 4.16 in of shape d	Ad ² 0.000 23.1468 23.1468 Total I =	I _c + Ad ² 11.300 24.6268 24.6268 60.5536	and a description of the contract of the contr
Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30	Units: Area 3.830 2.440 2.440 8.710 0.00 Units: Area 8.790	y 0.000 -3.080 3.080 Sum Ay = Inches y 6.150	NOTE: depth NOTE: Ref av Ay 0.000 -7.515 7.515 0.000 NOTE: depth NOTE: Ref av Ay 54.059	dis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam = dis is bottom of l _c 238.0	d 0.000 3.080 3.080 4.16 in of shape d 2.047	Ad ² 0.000 23.1468 23.1468 Total I = Ad ² 36.828	I _c + Ad ² 11.300 24.6268 24.6268 60.5536	
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30 2-L4x3x1/4 3-L4X3X1/4 Total area =	Units: Area 3.830 2.440 2.440 8.710 0.00 Units: Area 8.790 1.690 1.690 12.170	y 0.000 -3.080 3.080 Sum Ay = Inches Inches y 6.150 13.520 13.520 Sum Ay =	NOTE: depth NOTE: Ref av	dis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam = dis is bottom of l _c 238.0 2.750 2.750	of W-shape d 0.000 3.080 3.080 4.16 in of shape d 2.047 5.323 5.323	Ad ² 0.000 23.1468 23.1468 Total I = Ad ² 36.828 47.8871	I _c + Ad ² 11.300 24.6268 24.6268 60.5536 I _c + Ad ² 274.828 50.6371	
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30 2-L4x3x1/4 3-L4X3X1/4	Units: Area 3.830 2.440 2.440 8.710 0.00 Units: Area 8.790 1.690 1.690	y 0.000 -3.080 3.080 Sum Ay = Inches Inches y 6.150 13.520 13.520	NOTE: depth NOTE: Ref a) Ay 0.000 -7.515 7.515 0.000 NOTE: depth NOTE: Ref a) Ay 54.059 22.849 22.849	dis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam = dis is bottom of l _c 238.0 2.750 2.750	of W-shape d 0.000 3.080 3.080 4.16 in of shape d 2.047 5.323 5.323	Ad ² 0.000 23.1468 23.1468 Total I = Ad ² 36.828 47.8871 47.8871	I _c + Ad ² 11.300 24.6268 24.6268 60.5536 I _c + Ad ² 274.828 50.6371 50.6371	in ⁴
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30 2-L4x3x1/4 3-L4X3X1/4 Total area = Y =	Units: Area 3.830 2.440 2.440 8.710 0.00 Units: Area 8.790 1.690 1.690 12.170 8.20	y 0.000 -3.080 3.080 Sum Ay = Inches y 6.150 13.520 13.520 Sum Ay = Inches	NOTE: depth NOTE: Ref a) Ay 0.000 -7.515 7.515 0.000 NOTE: depth NOTE: Ref a) Ay 54.059 22.849 22.849 99.756 NOTE: depth	dis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam = dis is bottom of l _c 238.0 2.750 2.750 of W-beam =	of W-shape 0.000 3.080 3.080 4.16 in of shape d 2.047 5.323 5.323	Ad ² 0.000 23.1468 23.1468 Total I = Ad ² 36.828 47.8871 47.8871	I _c + Ad ² 11.300 24.6268 24.6268 60.5536 I _c + Ad ² 274.828 50.6371 50.6371	in ⁴
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30 2-L4x3x1/4 3-L4X3X1/4 Total area = Y =	Units: Area 3.830 2.440 2.440 8.710 0.00 Units: Area 8.790 1.690 1.690 12.170 8.20 Units:	Inches y 0.000 -3.080 3.080 Sum Ay = Inches y 6.150 13.520 13.520 Sum Ay = Inches I	NOTE: depth NOTE: Ref a) Ay 0.000 -7.515 7.515 0.000 NOTE: depth NOTE: Ref a) Ay 54.059 22.849 22.849 99.756 NOTE: depth	dis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam = dis is bottom of l _c 238.0 2.750 2.750 of W-beam =	of W-shape d 0.000 3.080 3.080 4.16 in of shape d 2.047 5.323 5.323	Ad ² 0.000 23.1468 23.1468 Total I = Ad ² 36.828 47.8871 47.8871 Total I =	I _c + Ad ² 11.300 24.6268 24.6268 60.5536 I _c + Ad ² 274.828 50.6371 50.6371 376.1020	in ⁴
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30 2-L4x3x1/4 3-L4X3X1/4 Total area = Y = FIGURE P6-44 Part	Units: Area 3.830 2.440 2.440 8.710 0.00 Units: Area 8.790 1.690 12.170 8.20 Units: Area	Inches y 0.000 -3.080 3.080 Sum Ay = Inches y 6.150 13.520 13.520 Sum Ay = Inches	NOTE: depth NOTE: Ref a) Ay 0.000 -7.515 7.515 0.000 NOTE: depth NOTE: Ref a) Ay 54.059 22.849 22.849 99.756 NOTE: depth	xis=centroid of I _c 11.3000 1.4800 1.4800 of W-beam = xis is bottom of I _c 238.0 2.750 2.750 of W-beam =	of W-shape d 0.000 3.080 3.080 4.16 in of shape d 2.047 5.323 5.323 12.3 in	Ad ² 0.000 23.1468 23.1468 Total I = Ad ² 36.828 47.8871 47.8871 Total I =	I _c + Ad ² 11.300 24.6268 24.6268 60.5536 I _c + Ad ² 274.828 50.6371 50.6371 376.1020	in ⁴
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30 2-L4x3x1/4 3-L4X3X1/4 Total area = Y = FIGURE P6-44 Part 1-6x2x1/4	Units: Area 3.830 2.440 8.710 0.00 Units: Area 8.790 1.690 1.690 12.170 8.20 Units: Area 3.370	Inches y 0.000 -3.080 3.080 Sum Ay = Inches y 6.150 13.520 13.520 Sum Ay = Inches y 0.000	NOTE: depth NOTE: Ref a) Ay 0.000 -7.515 7.515 0.000 NOTE: depth NOTE: Ref a) Ay 54.059 22.849 22.849 99.756 NOTE: depth NOTE: depth	dis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam = dis is bottom of l _c 238.0 2.750 2.750 of W-beam = dis=centroid of l _c 13.1000	of W-shape d 0.000 3.080 3.080 4.16 in of shape d 2.047 5.323 5.323 12.3 in f tube d 0.000	Ad ² 0.000 23.1468 23.1468 23.1468 Total I = Ad ² 36.828 47.8871 47.8871 Total I =	I _c + Ad ² 11.300 24.6268 24.6268 60.5536 I _c + Ad ² 274.828 50.6371 50.6371 376.1020	in ⁴
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30 2-L4x3x1/4 3-L4X3X1/4 Total area = Y = FIGURE P6-44 Part 1-6x2x1/4 2-bot plate	Units: Area 3.830 2.440 2.440 8.710 0.00 Units: Area 8.790 1.690 12.170 8.20 Units: Area 3.370 1.000	Inches y 0.000 -3.080 3.080 Sum Ay = Inches y 6.150 13.520 13.520 Sum Ay = Inches y 0.000 -3.250	NOTE: depth NOTE: Ref av	dis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam = dis is bottom of l _c 2.750 2.750 of W-beam = dis=centroid of l _c 13.1000 0.0208	of W-shape d 0.000 3.080 3.080 4.16 in of shape d 2.047 5.323 5.323 12.3 in f tube d 0.000 3.250	Ad ² 0.000 23.1468 23.1468 Total I = Ad ² 36.828 47.8871 47.8871 Total I = Ad ² 0.000 10.5625	I _c + Ad ² 11.300 24.6268 24.6268 60.5536 I _c + Ad ² 274.828 50.6371 50.6371 376.1020 I _c + Ad ² 13.100 10.5833	in ⁴
FIGURE P6-42 Part 1-W4x13 2-bot tube 3-top tube Total area = Y = FIGURE P6-43 Part 1-W12x30 2-L4x3x1/4 3-L4X3X1/4 Total area = Y = FIGURE P6-44 Part 1-6x2x1/4	Units: Area 3.830 2.440 8.710 0.00 Units: Area 8.790 1.690 1.690 12.170 8.20 Units: Area 3.370	Inches y 0.000 -3.080 3.080 Sum Ay = Inches y 6.150 13.520 13.520 Sum Ay = Inches y 0.000	NOTE: depth NOTE: Ref a) Ay 0.000 -7.515 7.515 0.000 NOTE: depth NOTE: Ref a) Ay 54.059 22.849 22.849 99.756 NOTE: depth NOTE: depth	dis=centroid of l _c 11.3000 1.4800 1.4800 of W-beam = dis is bottom of l _c 238.0 2.750 2.750 of W-beam = dis=centroid of l _c 13.1000	of W-shape d 0.000 3.080 3.080 4.16 in of shape d 2.047 5.323 5.323 12.3 in f tube d 0.000	Ad ² 0.000 23.1468 23.1468 23.1468 Total I = Ad ² 36.828 47.8871 47.8871 Total I =	I _c + Ad ² 11.300 24.6268 24.6268 60.5536 I _c + Ad ² 274.828 50.6371 50.6371 376.1020	in ⁴

FIGURE P6-45	Units	Inches	NOTE: Ref ax	dis is bottom	of shape			
Part	Area	у	Ау	I _c	d	Ad²	$I_c + Ad^2$	
1-C8x4.147	3.526	4.000	14.104	37.40	1.023	3.692	41.092	DOCK COMMUNICATION CONTRACTOR CON
2-C8x4.147	3.526	4.000	14.104	37.40	1.023	3.692	41.092	
3-C8x4.147-Top	3.526	7.070	24.929	3.250	2.047	14.770	18.020	
Total area =	10.578	Sum Ay =	53.137			Total I =	100.205	in ⁴
Υ=	5.023	Inches					100.200	***

FIGURE P6-46	Units	: Inches	NOTE: Ref ax	xis at base of	shape			
Part	Area	у	Ау	I _c	d	Ad²	$I_c + Ad^2$	Name and the Control of the Control
1-1/2x18 plate	9.000	0.250	2.250	0.1875	1.857	31.036	31.223	THE PERSON NAMED AND ADDRESS OF THE PERSON NAMED AND ADDRESS O
2-3/4x10 plate	7.500	5.500	41.250	62.500	3.393	86.344	148.844	
3-L8x4x1/2	5.800	1.354	7.853	6.750	0.753	3.289	10.039	
4-L8x4x1/2	5.800	1.354	7.853	6.750	0.753	3.289	10.039	
Total area =	28.100	Sum Ay =	59.206			Total =	200.144	in ⁴
YES	2.107	Inches						•••

FIGURE P6-47		Units: r	nm	NOTE: Refe	rence ax	is is botton	of the shape
Part	Area, A,	\mathbf{y}_i	$A_i y_i$	10	d_i	$A_i d_i^2$	$I_c + Ad^2$
1-Flanges(2)	72.000	1.500	108.0	54.0	13.1	12434.2	12488.2
2-Vert. webs(2)	150.000	12.500	1875.0	7812.5	2.1	687.9	8500.4
3-Semicircle(+)	157.080	29.240	4593.0	1120.0	14.6	33476.6	34596.6
4-Semicircle(-)	-76.970	27.968	-2152.7	-268.9	13.3	-13669.7	-13938.6
Total area =	302.110 mm ²	Sum Ay =	4423.3	mm ³	٦	$fotal I_c =$	41646.6 mm ⁴
	Y=	14.641 n	nm				

FIGURE P6-48		Units: I	nches	NOTE: Refe	erence ax	is is base o	of the shape
Part	Area, A,	\mathbf{y}_i	$A_i y_i$	10	d,	$A_i d_i^2$	$I_c + Ad^2$
1-Rect. (2)	1.250	0.625	0.781	0.163	0.391	0.191	0.353
2-Semicircle	0.884	1.568	1.385	0.035	0.552	0.270	0.305
Total area =	2.134 in ²	Sum $Ay =$	2.167	in ³	٦	Γ otal $I_c =$	0.659 in⁴
	Y=	: 1.016 iı	n				

SOLUTIONS FOR PROBLEMS 7-49 THROUGH 7-66

Each problem requires the computation of the radius of gyration

 $r_{\rm X}$ = (I $_{\rm X}$ /A)^1/2 with respect to the horizontal centroidal axis.

Data for I and A are taken from the solution for the given figure number.

Prob. No.	Fig. No.	l _×	Α	r_{χ}
6-49	P6-2	166.0 in^4	18.00 in^2	3.04 in
6-50	P6-3	184.0 in^4	24.00 in^2	2.77 in
6-51	P6-4	4.64E+07 mm^4	9375 mm^2	70.35 mm
6-52	P6-5	2.66E+05 mm^4	550 mm^2	21.99 mm
6-53	P6-6	6.17E+04 mm^4	800 mm^2	8.78 mm
6-54	P6-8	5.36E+04 mm^4	550 mm^2	9.87 mm
6-55	P6-9	1.35E+05 mm^4	550 mm^2	15.67 mm
6-56	P6-11	1.86E+05 mm^4	725 mm^2	16.02 mm
6-57	P6-12	1.70E+04 mm^4	456. mm^2	6.11 mm
6-58	P6-14	0.3672 in^4	1.06 in^2	0.59 in
6-59	P6-15	0.3572 in^4	0.68 in^2	0.72 in
6-60	P6-16	0.3657 in^4	1.35 in^2	0.52 in
6-61	P6-17	6.73E+07 mm^4	14227 mm^2	68.78 mm
6-62	P6-21	151.4 in^4	18.75 in^2	2.84 in
6-63	P6-22	148.3 in^4	27.38 in^2	2.33 in
6-64	P6-23	107.2 in^4	34.50 in^2	1.76 in
6-65	P6-24	816.3 in^4	50.63 in^2	4.02 in
6-66	P6-25	831.45 in⁴	20.6 in ²	6.35 in

SOLUTIONS FOR PROBLEMS 6-67 THROUGH 6-81

Each problem requires computation of the radius of gyration: $r_y = (I/A)^0.5$ with respect to the vertical *Y-Y centroidal* axis Data for *A* are taken from the solutions for I_x for the given figure number. All sections have a vertical axis of symmetry and they can be broken into parts that all have their centroidal axis on the axis of symmetry. Therefore, the total I is the algebraic sum of the I values for all parts.

		I ₁	12	. 13	Total I _y	A	$r_{_{V}}$
6-67	P6-2	18.00	0.50	18.00	36.500	18.00	1.424
6-68	P6-3 [*]	144.00	-32.00	0.00	112.000	24.00	2.160
6-69M	P6-4	2.60E+05	1.12E+07	0.00	1.14E+07	9375	34.911
6-70M	P6-5	3333	521	26667	3.05E+04	550	7.449
6-71	P6-16	0.0527	0.00775	0.00	0.0605	1.35	0.212
6-72M	P6-17	3.42E+06	3.18E+05	3.18E+05	4.06E+06	14227	16.883
6-73	P6-21	5.359	1.547	5.359	12.266	18.75	0.809
6-74	P6-22 [*]	222.30	-35.18	0.00	187.11	27.38	2.614
6-75	P6-23 [*]	5184.00	-2701.13	0.00	2482.88	34.50	8.483
6-76	P6-24	25.31	177.98	0.00	203.29	50.63	2.004
6-77	P6-25	45.20	21.33	21.33	87.867	20.60	2.065
6-78	P6-26	15.60	144.00	0.00	159.60	21.95	2.696
6-79	P6-27	35.48	14.29	0.00	49.772	15.65	1.783
6-80	P6-42	3.860	4.490	4.490	12.840	8.71	1.214
6-81	P6-44	2.210	0.333	0.333	2.877	5.37	0.732

 $^{^*}I_1$ is for the large outside rectangle; I_2 is for the internal rectangle and is negative For Problems 6-69M, 6-70M, and 6-72M: I in mm⁴, A in mm², r in mm For all other problems: I in in⁴, A in in², r in inches

SOLUTIONS TO PROBLEMS 6-21M TO 6-46M METRIC VERSIONS OF FIGURES P6-21 TO P6-46

FIGURE P6-21M	Unit	s: mm	NOTE: Refe	rence axis is b	pase of the	shape		
Part	Area	у	Ay	I _c	d	Ad²	$I_c + Ad^2$	***************************************
1-Bot 2x4	3382	19	64258	4.070E+05	89	2.679E+07	2.72E+07	~
2-Web-2x6	5320	108	574560	8.689E+06	0	0.0000	8.69E+06	
3-Top 2x4	3382	197	666254	4.070E+05	89	2.679E+07	2.72E+07	
Total area =	12084	Sum Ay =				Total I =		mm ⁴
Υ ==	108	mm	Used 2x4 = :	38 mm x 89 m	m; 2x6 = 3	38 mm x 140 m	m	
FIGURE P6-22M	l Inite	s: mm	MOTE: Doso	ranaa ayia ia b		-1.		
Part	Area	***************************************		rence axis is b		snape Ad²	1 . 1 . 2	
1-Outside rect.	32752	у 89.0	Ay 2.915E+06	I _c 8.648E+07	<u>d</u>		$I_c + Ad^2$	
2-Inside rect.	-15120	89.0	-1.346E+06		0.00	0.000E+00	8.648E+07	
3-	0	0.0	0.000E+00	0.000E+00	0.00 0.00	0.000E+00 0.000E+00	-2.470E+07	
Total area =	17632	Sum Ay =		0.0001.00	0.00	Total I =	0.000E+00	4
Υ =	89.00	mm		19 mm v 184 r	nm: 2v6 =	38 mm x 140 n		mm ⁴
				angle - Inside		00 11111 X 140 11	11111	
				J				
FIGURE P6-23M		s: mm	NOTE: Refe	rence axis is b	ase of the			
Part	Area	у	Ay	l _c	d	Ad²	$I_c + Ad^2$	
1-Outside rect.	69784	57.2	3.992E+06	7.611E+07	0.00	0.000E+00	7.611E+07	
2-Inside rect.	-47526	57.2		-3.137E+07	0.00	0.000E+00	-3.137E+07	
3-	0	0.0	0.000E+00	0.000E+00	0.00	0.000E+00	0.000E+00	
Total area = Y =	22258	Sum Ay =				Total I =	4.47E+07	mm ⁴
Y 234	57.20	mm	Outside rest	38 mm x 89 mi	m; 1/2x24	= 12.7 mm x 6°	10 mm	
			Outside recta	angle - Inside i	rectangle			
FIGURE P6-24M	Units	: mm	NOTE: Refer	ence axis is b	ase of the	shane		
Part	Area	У	Ау	I _c	d	Ad²	I _c + Ad ²	
1-Verticals (2)	21736	143.0	3.108E+06	1.482E+08	54.00	6.338E+07	2.115E+08	
2-Top flange	10868	305.0	3.315E+06	1.308E+06	108.00	1.268E+08	1.281E+08	
3-	0	0.0	0.000E+00	0.000E+00	0.00	0.000E+00	0.000E+00	
Total area =	32604	Sum Ay =	6.423E+06			Total I =	3.40E+08	mm ⁴
Y ****	197.00	mm	Used 2x12 =	38 mm x 286	mm			,,,,,,
FIGURE P6-25M	مؤنما		NOTE: D		-			
Part	Units					dis = centroid;18		oot
1-W360x64	Area 8130	у 0.00	Ay	l _c	d	Ad ²	$I_c + Ad^2$	
2-bot plate	2400	-186	0.00 -446400	1.780E+08	0.00	0.00	1.780E+08	
3-top plate	2400	186	446400	2.880E+04 2.880E+04	186 186	8.303E+07	8.306E+07	
Total area =	12930	Sum Ay =	0.00	2.000L104	100	8.303E+07	8.306E+07	
γ =	0.00	Inches	0.00			Total I =	3.44E+08	mm⁴
•	2.00							
FIGURE P6-26M	Units	mm	NOTE: Refer	ence axis is ba	ase of the	shape; Depth o	of S = 305 mn	า
Part	Area	у	Ау	I _c	d	Ad²	I _c + Ad ²	
1-S300x74	9420	152.500	1.437E+06	1.260E+08	48.615	2.226E+07	1.483E+08	**************************************
2-C300x37	4740	297.730	1.411E+06	1.850E+06	96.615	4.425E+07	4.610E+07	
Total area =	14160		2.848E+06			Total I =	1.94E+08	mm ⁴
Υ =	201.12	mm	NOTE: Web f	or C is 9.83 m	m thick; Y	-Y axis down 1	7.1 mm from	top
			NOTE: For C	hannel; y = 30	5+9.83-17	.1 = 297.73 mn	n	-

FIGURE P6-27M	Units	Jnits: mm NOTE: Reference axis is base of the shape; Depth of S = 305 mm						
Part	Area	у	Ay	I _c	d	Ad²	I _c + Ad ²	
1-I305x23.80 AI	7841	152.5	1.196E+06	1.320E+08	34.233	9.189E+06	1.412E+08	******************
2-12x180 Plate	2160	311.0	6.718E+05	2.592E+04	124.267	3.336E+07	3.338E+07	
Total area =	10001	Sum Ay =	1.868E+06			Total I =	1.75E+08	mm ⁴
γ =	186.73	mm						

FIGURE P6-28M	Units	: mm	NOTE: Char	nnel depth=305	mm;Ref	xis = centroid;	164.5 mm fro	m bot
Part	Area	у	Ау	I _c	d	Ad²	$I_c + Ad^2$	***************************************
1-C305x12.31 (2)	9080	0.00	0.00	1.330E+08	0.00	0.00	1.330E+08	
2-bot plate	3000	-158.5	-475500	3.600E+04	158.5	7.537E+07	7.540E+07	
3-top plate	3000	158.5	475500	3.600E+04	158.5	7.537E+07	7.540E+07	
Total area = V ≡	15080 0.00	Sum Ay =		ID-#I-		Total I =		mm ⁴
γ =	0.00	Inches	NOTE: TOP	and Bottom pla	tes are 12	mm x 250 mm		

Figure P6-29M	Units	s: mm	NOTE: Refe	rence axis = ce	entroid = 8	7 mm from bott	tom	
Part	Area	у	Ay	I _c	d	Ad²	I _c + Ad ²	
1 Vert plate	1800	0.0	0.00	3.375E+06	0.0	0.000E+00	3.375E+06	*************
2-Bot angles (2)	1768	-58.9	-104135	3.960E+05	58.9	6.134E+06	6.530E+06	
3-Top angles (2)	1768	58.9	104135	3.960E+05	58.9	6.134E+06	6.530E+06	
4-Top plate	1320	81.0	106920	1.584E+04	81.0	8.661E+06	8.676E+06	
5-Bot plate	1320	-81.0	-106920	1.584E+04	81.0	8.661E+06	8.676E+06	
Total area =	7976	Sum Ay =	0.00			Total I =	3.38E+07	mm ⁴
Υ =	0.00	mm	NOTE: For A	Angle; y = 87 - 1	12 - 16.1 =	= 58.9 mm from	centroid	

FIGURE P6-30M	Units	s: mm	NOTE: Overall depth = 150 mm; Ref axis=centroid; 75 mm from bot						
Part	Area	У	Ау	I _c	d	Ad²	$I_c + Ad^2$		
1-Vert plates (2)	3600	0.00	0.00	3.375E+06	0.000	0.00	3.375E+06		
2-bot channel	1140	-63.4	-72276	1.250E+05	63.4	4.582E+06	4.707E+06		
3-top channel	1140	63.4	72276	1.250E+05	63.4	4.582E+06	4.707E+06		
Total area =	5880	Sum Ay =	0.00			Total I =	1.28E+07	mm ⁴	
Υ =	0.00	mm							

FIGURE P6-31M	Units	: mm	NOTE: Ref axis=centroid; 75 mm from center of either pipe					
Part	Area	у	Ау	l _c	d	Ad²	$I_c + Ad^2$	······
1-Vert plate	1220.88	0.00	0.000	1.053E+06	0.00	0.000E+00	1.053E+06	Oranda Waller Commence
2-bot pipe	515.80	-75.00	-38685	1.290E+05	75.00	2.901E+06	3.030E+06	
3-top pipe	515.80	75.00	38685	1.290E+05	75.00	2.901E+06	3.030E+06	
Total area =	2252.48	Sum Ay =	0.000			Total I =	7.11E+06	mm ⁴
Υ =	0.00	mm	NOTE: Web	length: 150 mr	n - pipe O	D = 150 mm - 4	8.26 = 101.7	'4 mm

FIGURE P6-32M	Units	ts: mm NOTE: Reference axis=centroid= 300 mm from CL of pipes						
Part	Area	У	Ау	l _c	d	Ad ²	I _c + Ad ²	
1-Top pipes (2)	2876	300	8.628E+05	2.520E+06	300	2.588E+08	2.614E+08	
2-Bot pipes (2)	2876	-300	-8.628E+05	2.520E+06	300	2.588E+08	2.614E+08	
Total area = Y ≃	5752 0.00	Sum Ay = mm	0.0000			Total I =	5.23E+08	mm ⁴

FIGURE P6-33M	Units	: mm	NOTE: Ref a	axis at base of	shape; Ov	erall height = 1	20 mm	
Part	Area	у	Ау	I _c	d	Ad²	$I_c + Ad^2$	
1-Base plate	1500	3.0	4500	4.500E+03	65.071	6.351E+06	6.356E+06	
2-Angles (2)	2180	37.0	80660	2.280E+06	31.071	2.105E+06	4.385E+06	
3-top plate	3600	114.0	410400	4.320E+04	45.929	7.594E+06	7.637E+06	*****
Total area = Y =	7280 68.071	Sum Ay =	495560			Total I =	1.84E+07	mm⁴
1 ~	00.071	(1111)						
FIGURE P6-34M	Units	: mm	NOTE: Reference axis = centroid = 76 mm from bottom					
Part	Area	у	Ay	I _c	d	Ad²	$I_c + Ad^2$	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
1-Channel	2470	0.00	0.00	7.200E+06	0.00	0.00	7.200E+06	······································
2-Channel	2470	0.00	0.00	7.200E+06	0.00	0.00	7.200E+06	
Total area =	4940	Sum Ay =				Total I =	1.44E+07	mm ⁴
Υ=	0.00	mm	NOTE: Dept	h of channel =	152 mm			
FIGURE P6-35M	Units	: mm	NOTE: Ref a	xis at base of	shape			
Part	Area	у	Ау	l _c	d	Ad²	$I_c + Ad^2$	
1-Angles (2)	1218	14.9	18148	2.880E+05	50.491	3.105E+06	3.393E+06	***************************************
2-Bot channel	1700	12.1	20570	2.600E+05	53.291	4.828E+06	5.088E+06	
3-Vert webs (2)	3000	75.0	225000	5.625E+06	9.609	2.770E+05	5.902E+06	
4-Top channel	1700	137.9	234430	2.600E+05	72.509	8.938E+06	9.198E+06	
Total area = Y =	7618	Sum Ay =	498148			Total I =	2.36E+07	mm⁴
γ	65.391	mm						
FIGURE P6-36M	Units	: mm	NOTE: Refer	ence axis is b	ases of sha	ape; Overall he	iaht = 152 m	m
Part	Area	У	Ау	I _c	d	Ad²	$I_c + Ad^2$	***************************************
1-W150x22.5	2860	76.000	217360	1.210E+07	16.278	7.578E+05	1.286E+07	
2-Angles (2)	1218	21.500	26187	2.880E+05	38.222	1.779E+06	2.067E+06	
Total area =	4078	Sum Ay =				Total I =	1.49E+07	mm ⁴
Υ=	59.722	mm	NOTE: y for	angles = 14.9	+ 6.60 = 21	1.50 mm; $t_f = 6$.60 mm	
FIGURE P6-37M	Units	: mm	NOTE: Refer	ence axis is ba	ases of sha	ana		
Part	Area	У	Ay	I _c	d	Ad ²	I _c + Ad ²	
1-Bot tube	1570	51.00	80070	1.870E+06	38.25	2.297E+06	4.167E+06	
2-Top tube	1570	127.50	200175	6.160E+05	38.25	2.297E+06	2.913E+06	
Total area =	3140	Sum Ay =	280245	,		Total I =	7.08E+06	mm ⁴
Υ=	89.25	mm						
FIGURE P6-38M	Units:	mm	NOTE: Ref a	xis at base of s	shane			
Part	Area	у	Ay	l _c	d	Ad²	I _c + Ad ²	
1-Outside tube	6280	76.00	477280	2.010E+07	1.269	1.011E+04	2.011E+07	
2-Bot inner tube	1570	37.30	58561	6.160E+05	37.431	2.200E+06	2.816E+06	
3-Top inner tube	1271	114.70	145784	4.620E+05	39.969	2.030E+06	2.492E+06	
Total area =	9121	Sum Ay =	681625			Total I =	2.542E+07	mm ⁴
Υ =	74.731	mm	NOTE: Use d	lesign wall thic	kness for H	HSS 152x152x	12.7; t _w = 11.	8 mm
EIGHDE DE 2088	Unite		MOTEL DEC.					
FIGURE P6-39M Part	Units:	***************************************		xis at base of s	***************************************	Ad²	1 . 4 .2	
1-Bot channel	Area 1020	y 11.60	Ay 11832.0	I _c 1.300E+05	72 550		I _c + Ad ²	~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~
2-152x51x6.4	2170	80.67	175053.9	5.450E+05	73.559 4.489	5.519E+06 4.374E+04	5.649E+06 5.494E+06	
3-Toop channel	1020	168.27	171635.4	1.300E+05	83.111	7.046E+06	7.176E+06	
Total area =	4210		358521.300			Total I =	1.83E+07	mm ⁴
Υ =	85.16	mm ´				·		

FIGURE P6-40M		s: mm	NOTE: Reference axis is bases of shape					
Part	Area	у	Ay	I _c	d	Ad ²	$I_c + Ad^2$	
1-Bot channel	1214	18.500	22459	4.080E+05	8.278	8.320E+04	4.912E+05	
2-Top I-beam	1114	35.800	39881	2.830E+05	9.022	9.067E+04	3.737E+05	
Total area =	2328	Sum Ay =	62340			Total I =	8.65E+05	mm ⁴
Y som	26.78	mm						
FIGURE P6-41M	1 Inite	s: mm	NOTE, Defe					
Part				erence axis is b	***************************************			
	Area	y 450,000	Ay	l _c	d	Ad²	$I_c + Ad^2$	
1-W310x44.5 2-C150x19.3	5670	156.000	884520	9.910E+07	51.312	1.493E+07	1.140E+08	
Total area =	2470 8140	325.100	802997	4.370E+05	117.788	3.427E+07	3.471E+07	
Y =	207.31	Sum Ay = mm		h of W-beam =	. 212	Total I =	1.49E+08	mm ⁴
1 ***	10,102	111111	NOTE. dept	n or vv-beam =	312 mm			
FIGURE P6-42M	Units	s: mm	NOTE: Ref	axis=centroid o	f W-shane			
Part	Area	у	Ау	I _c	d	Ad ²	I _c + Ad ²	
1-W100x19.3	2470	0.000	0	4.700E+06	0.0	0.000E+00	4.700E+06	····
2-bot tube	1570	-78.5	-123245	6.160E+05	78.5	9.675E+06	1.029E+07	
3-top tube	1570	78.5	123245	6.160E+05	78.5	9.675E+06	1.029E+07	
Total area =	5610	Sum Ay =	0.000			Total I =	2.53E+07	mm ⁴
Υ =	0.00	mm		h of W-beam =	106 mm	rotar r	Z.00L.07	*******
			•					
FIGURE P6-43M	Units	s: mm	NOTE: Ref	axis is bottom o	of shape			
Part	Area	У	Ay	I _c	d	Ad²	$I_c + Ad^2$	***************************************
1-W310x44.5	5670	156	884520	9.910E+07	51.931	1.529E+07	1.144E+08	
2-L4x3x1/4	1090	343	373870	1.140E+06	135.069	1.989E+07	2.103E+07	
3-L4X3X1/4	1090	343	373870	1.140E+06	135.069	1.989E+07	2.103E+07	
Total area =	7850	Sum Ay =	1632260			Total I =	1.56E+08	mm ⁴
Υ=	207.93	mm	NOTE: depti	h of W-beam =	312 mm			
FIGURE P6-44M	Unite	: mm	NOTE: Dof	axis=centroid o	f fh.a			
Part	Area	у у	Ay		·····	Ad²	1 . 4 . 2	·····
1-152x51x6.4	2170	0.000	0.000	I _c 5.450E+06	d		I _c + Ad ²	
2-bot plate	600	-82	-49200	7.200E+08	0.000 82	0.000E+00	5.450E+06	
3-top plate	600	82	49200	7.200E+03	82	4.034E+06 4.034E+06	4.042E+06	
Total area =	3370	Sum Ay =	0.000	7.2001.00	02	Total I =	4.042E+06	4
γ =	0.00			are 12 mm x 5	0 mm	i Otal I	1.35E+07	mm ⁴
				aro in min x o	O (11111)			
FIGURE P6-45M	Units	: mm	NOTE: Ref a	ixis is bottom o	f shape			
Part	Area	у	Ау	I _c	d	Ad ²	$I_c + Ad^2$	
1-C203x6.17	2275	101.5	230912.5	1.560E+07	25.967	1.534E+06	1.713E+07	
2-C203x6.17	2275	101.5	230912.5	1.560E+07	25.967	1.534E+06	1.713E+07	
3-C203x6.17-Top	2275	179.4	408135.0	1.350E+06	51.933	6.136E+06	7.486E+06	
Total area =	6825	Sum Ay =	869960.0			Total I ≃	4.18E+07	mm ⁴
γ =	127.47	mm						
ElCUDE DO 400*	£ 5 *4							
FIGURE P6-46M	Units:			xis at base of s				
Part	Area	у	Ау	l _c	d	Ad²	$I_c + Ad^2$	
1-12x450 plate	5400	6.0	32400	6.480E+04	48.221	1.256E+07	1.262E+07	***************************************
2-20x250 plate	5000	137.0	685000	2.604E+07	82.779	3.426E+07	6.030E+07	
3-L203x102x12.7	3740	33.7	126038	2.810E+06	20.521	1.575E+06	4.385E+06	
4-L203x102x12.7	3740	33.7	126038	2.810E+06	20.521	1.575E+06	4.385E+06	
Total area = Y =	17880	Sum Ay =	969476			Total I =	8.17E+07	mm ⁴
γ 💴	54.22	mm						

CHAPTER 7 Stress Due to Bending

ANALYSIS OF BENDING STRESSES

$$\frac{7-3}{\sigma} = \frac{(a)}{I} = \frac{5800 \text{ M} \cdot \text{in}}{(0.75 \text{ in})} = 0.211 \text{ in}^{4}$$

$$\sigma = \frac{Me}{I} = \frac{(5800 \text{ M} \cdot \text{in})(0.75 \text{ in})}{0.211 \text{ in}^{4}} = \frac{20620 \text{ pol}}{2000 \text{ pol}}$$
(b)
$$I = \frac{1.5(0.75)^{3}}{12} = 0.0527 \text{ in}^{4}$$

$$\sigma = \frac{(5800 \text{ M} \cdot \text{in})(0.375 \text{ in})}{0.0521 \text{ in}^{4}} = \frac{41240 \text{ pol}}{2000 \text{ pol}}$$

$$\frac{7-4}{J} = \frac{1.5(7.25)^{3}/2 = 47.63 \text{ in}^{4}; C = 7.25/2 = 3.625 \text{ in}}{J} = \frac{(15500 \text{ lb. in})(3.625) \text{ in}}{J} = \frac{1180 \text{ psi}}{47.63 \text{ in}^{4}}$$

$$\frac{7-5}{\sigma = \frac{20}{5} = \frac{30000 \text{ ft}}{17.1 \text{ m}^3} \times \frac{12 \text{ in}^3}{\text{ft}} = \frac{21050 \text{ psi}}{1}$$

$$\frac{7-7}{\text{ALUM. } C4 \times 2.33/; I = 1.02 \text{ m}^{4}; C_{\pm} = 0.78 \text{ m.; } C_{\delta} = 1.47 \text{ m}}$$

$$\text{BEAM IS IN NEGATIVE BENDING.}$$

$$\text{TENSILE - TOP}$$

$$\sigma = \frac{M \text{ CA}}{I} = \frac{(9000 \text{ M·m})(0.78 \text{ m})}{1.02 \text{ m}^{4}} = \frac{6882 \text{ psi}}{6882 \text{ psi}}$$

$$\text{Comp. - Bottom}$$

$$\sigma = \frac{M \text{ Cb}}{I} = \frac{(9000 \text{ M·m})(1.47 \text{ m})}{I} = 72 970 \text{ psi}$$

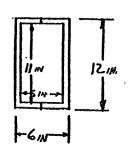
$$\frac{7-8}{S} = \frac{M}{5} = \frac{4550 \, \text{M} \cdot \text{m}}{0.3 \, \text{A} \cdot \text{m}^3} = \frac{13960 \, \text{psi}}{13960 \, \text{psi}}$$

$$\frac{7-9}{I} = \frac{71.5 \text{ kN·m}}{1.5 \text{ kN·m}} = \frac{715.00 \text{ N·m}}{1.5 \text{ kN·m}} \times \frac{8.851 \text{ ll·m}}{1.5 \text{ ll·m}} = \frac{6.33 \times 10^5 \text{ ll·m}}{1.5 \text{ ll·m}} = \frac{6.33 \times 10^5 \text{ ll·m}}{1.5 \text{ ll·m}} = \frac{5794 \text{ poi}}{1.5 \text{ ll·m}} = \frac{6.33 \times 10^5 \text{ ll·m}}{1.5 \text{ ll·m}} = \frac{5794 \text{ poi}}{1.5 \text{ ll·m}} = \frac{3.99 \text{ MPa}}{1.5 \text{ ll·m}} = \frac{7.10 \times 10^5 \text{ ll·m}}{1.5 \text{ ll·m}} = \frac{7.10 \times 10^5 \text{ ll·m}}{1.5 \times 10^5 \text{ ll·m}} = \frac{1.03 \text{ ll·m}}{1.5 \text{ ll·m}} = \frac{1.03 \text{ l$$

$$I = \frac{6(12)^3}{12} - \frac{5(11)^3}{12} = 309.4 \text{ in}^4$$

$$O = \frac{Mc}{I} = \frac{(6000 \text{ M} \cdot \text{ft}) (6 \text{ in})}{309.4 \text{ in}^4} \text{ ft}$$

$$O = 13963 \text{ psi}$$



DESIGN OF BEAMS

$$S = bh^{2}/6 = b(3b)^{2}/6 = 9b^{3}/6 = 1.5b^{3}$$

$$b = \sqrt{5/1.5} = \sqrt{2636 \text{ mm}^{3}/1.5} = 12.1 \text{ mm}$$

$$REQD S = \frac{M}{S1} = \frac{145N.m}{55N/mm^{2}} \times \frac{10^{3}mm}{m} = 2636mm^{3}$$

$$b = 12.1 \text{ mm} \text{ j. } h = 3b = 36.3 \text{ mm}$$

$$\frac{7-14}{C_b} = \frac{7}{7} = \frac{152.5 \, mm}{28.000 \, N \cdot m} \cdot \frac{C_c}{(152.5 \, mm)} \cdot \frac{10^3 \, mm}{M} = \frac{92.0 \, MBa}{M}$$
FOR AIST 1020 HR 5 = 231 Mgs.

$$T = \frac{1}{2.66 \times 10^{5} \text{ m/m}}; c_{b} = \overline{y} = 35.0 \text{ m/m}$$

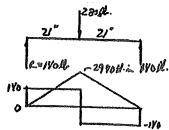
$$C = \frac{M c_{b}}{I} = \frac{675 \text{ N/m}}{2.66 \times 10^{5} \text{ m/m}}; \frac{10^{3} \text{ m/m}}{2.00 \times 10^{5} \text{ m/m}} = 36.2 \text{ MPa}$$

$$C = \frac{1}{I} = \frac{366 \times 10^{5} \text{ m/m}}{2.66 \times 10^{5} \text{ m/m}} = \frac{36.2 \text{ MPa}}{2.66 \times 10^{5} \text{ m/m}}$$

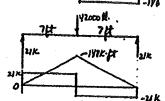
$$\frac{8-16}{ReQ'D}S = \frac{M}{\sigma_d} = \frac{2940 \, \text{l.m.}}{10000 \, \text{l.f.}} = 0.294 \, \text{in}^3$$

$$USE \frac{12 \, \text{H.} \, Sch. 40 \, \text{PIPE}}{V, M} = 0.3262 \, \text{i.s.}^3$$

$$V, M = 147000 \, \text{l.f.} + 12 \, \text{l.f.}$$



$$S = \frac{M}{\sigma_d} = \frac{147000 \, \text{d. ft}}{20000 \, \text{d. ft}} \frac{12 \, \text{d.}}{\text{ft}} = 88.2 \, \text{in}^3$$
USE A W 20 x 66 · S = 1/9 in 3

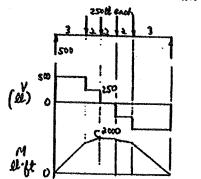


$$B + B$$
 $I = 107.2 \text{ in}^4$; $C = 4.50 \text{ in}/2 = 2.25 \text{ in}$

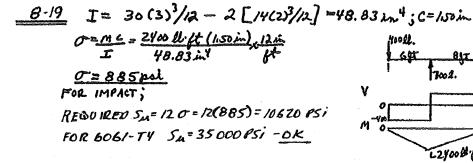
$$\sigma = MC = (2000 \text{ M} \cdot \text{pt}) (2.25 \text{ in}) (12 \text{ in})$$

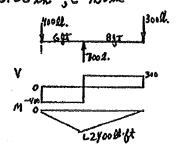
$$(107.2 \text{ in}^4) \text{ pt}$$

$$\sigma = 504 \text{ psi}$$



FROM. TABLE A-19, MINIMUM ALLOWABLE BENDING STRESS = 625 psi -OK





$$\frac{B-20}{I} = 1.86 \times 10^{5} \text{mm}^{\frac{1}{3}}; C_{1} = \overline{7} = 21.8 \text{ mm}; C_{2} = 45-21.8 = 23.3 \text{ mm}$$

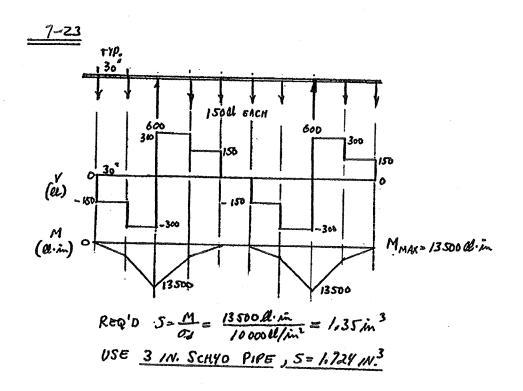
$$MAX STRESS AT TOP$$

$$\sigma = \frac{M C_{R}}{I} = \frac{(318 \text{ N·m})(23.2 \text{ mm})}{1.86 \times 10^{5} \text{mm}^{\frac{10}{3}}} \times \frac{10^{3} \text{mm}}{m} = 39.7 \text{ MPa. (comp.)}$$

$$REQ'D Sy = 2\sigma = 2(39.7 \text{ MPa.)} = 79.4 \text{ MPa. OK FOL 6061-TY}$$

$$Sy = 145 \text{ MPa.}$$

$$REQ'DS = \frac{M}{00} = \frac{11250N \text{ in }}{60N/mm^2} + \frac{N^2_{min}}{m} = 0.141 \times 0^{\frac{1}{2}} \times 0^{\frac{1}{$$



```
To = Sy/4 = 46 000 psi/4 = 11500 psi
               M = (4800LE)(14/N) = 67200 LE-1A
              RED'D. S = M/00 = 67200 LB.IN) (11500 LB/IN3) = 5.84 IN3
              USE EITHER 6x4x/4 OR 8x2x/4: EACH WEIGHS 156 LB/FT.
   7-25
              LET 0 = 54/4 = 40000851/4 = 10000851
              REOD, S= M/0= 67200/1000 = 672 IN3 = 6Ix 4.030
   7-26
              Od = 51/4 = 50 000 psi/4 = 12500 psi
              RESD. S= M/02 = 67200/12500 = 5.3812 = W8 4/0
             OT = 5 Y/y = 36000 PSI/Y = 9000 PSI
M/OT=S = 7.47 IN FOR Y-AXIS : NO SUITABLE CHANNEL
   7-27
   3-28

Sy = 36 Kei - THEN REOD. S= 7.47 IN 8 (PROST-27): 6-1N SCH40 PIPE

A = 5.581 IN - HEAVIER MAN OTHER STEEL DESIGNS
   T-29
DESIGN PROBLEM - MULTIPLE SOLUTIONS POSSIBLE - WT Z 4.030 LB/FT
FOR ALUM 6I X 4.030. USE ALUM 2014-T6, SY = 60KSI
ALLOWS USE OF 5I x 3.700.
7-30 FROM FIEP 6/5; I=0.3572 IN; Co=1.068/N.; Co=1.332 IN
         Smin = I = 0.3572 IN = 0.268 IN 3
         0= 1718. FT 121 5239 PS
         REOD OE = 4 0 = 20 960 PSi
        SEVERAL POSSIBLE CHOICES & APT. A-20 (LB)
        EXAMPLE: NYLON, POLYESTER
           HIGH MIDILUS OF ELASTICITY
           GOOD ELECTRICAL PROPERTIES (TABLE 2-12)
           MUST CHECK EXTRUDABILITY.
```

$$\frac{7-3!}{M_{MAX}} = 24 RN \cdot m \quad (SEE PROB P 5-34)$$

$$S = \frac{M}{G_{3}} = \frac{24000 \, N \cdot m}{150 \, N/mm^{2}} \frac{10^{3} \, mm}{m} = 160000 \, mm \times \frac{6.02 \times 16^{5} \, m^{2}}{mm^{3}}$$

$$S = 9.76 \, im^{3} : USE \, WD \times 12 : S = 10.9 \, im^{3} : W250 + 17.9 \, A-7(SS)$$

$$\frac{7-32}{7-32} \quad FROM PROB. PS=35 : M_{MAX} = 125 \, N \cdot m$$

$$G_{3} = \frac{SM}{8} = \frac{648 \, MPa}{8 \, MPa} = \frac{81 \, MPa}{8 \, mm^{3}} = \frac{170^{3}}{32}$$

$$S = \frac{M}{81 \, N/mm^{3}} \times \frac{10^{3} \, mm}{m} = \frac{1543 \, mm^{3}}{81 \, N/mm^{3}} = \frac{170^{3}}{32}$$

$$D = \sqrt[3]{325/\pi} = \frac{25.1 \, mm^{3}}{81 \, N/mm^{3}}$$

- 7-33 Specify the lightest wide-flange beam. ASTM A992 structural steel. Sy = 50 ksi Design stress: σ_d = 0.66 s_y = (0.66)(50 000 psi) = 33 000 psi From Figure P5-3: M_{max} = (45.7 K-ft)(1000 lb/K)(12 in/ft) = 548 400 lb-in Required section modulus: $S = M/\sigma_d$ = (548 400 lb-in)/(33 000 lb/in²) = 16.6 in³ Specify: W12x16 steel beam from Appendix A-7(US); S = 17.1 in³
- 7-34 Specify the lightest wide-flange beam. ASTM A992 structural steel. Sy = 345 MPa Design stress: σ_d = 0.66 s_y = (0.66)(345 MPa) = 227.7 MPa = 227.7 N/mm² From Figure P5-7: M_{max} = (71.5 kN-m)(1000 N/kN)(1000 mm/m) = 71.5x10⁶ N-mm Required section modulus: $S = M/\sigma_d$ = (71.5x10⁶ N-mm)/(227.7 N/mm²) = 3.14x10⁵ mm³ Specify: W360x39 steel beam from Appendix A-7(SI); US designation: W14x26 S = 5.79x10⁵ mm³

<u>Problems 7-35 to 7-42</u> are similar to 7-33 and 7-34 above with the same design stress. Maximum bending moment varies with the beam loading shown in the indicated figures from Chapter 5.

<u>Problems 7-43 to 7-52</u> use the same set of beam loadings as 7-33 and 7-34 but the objective is to specify the lightest American Standard S-beam. The required section modulus is the same.

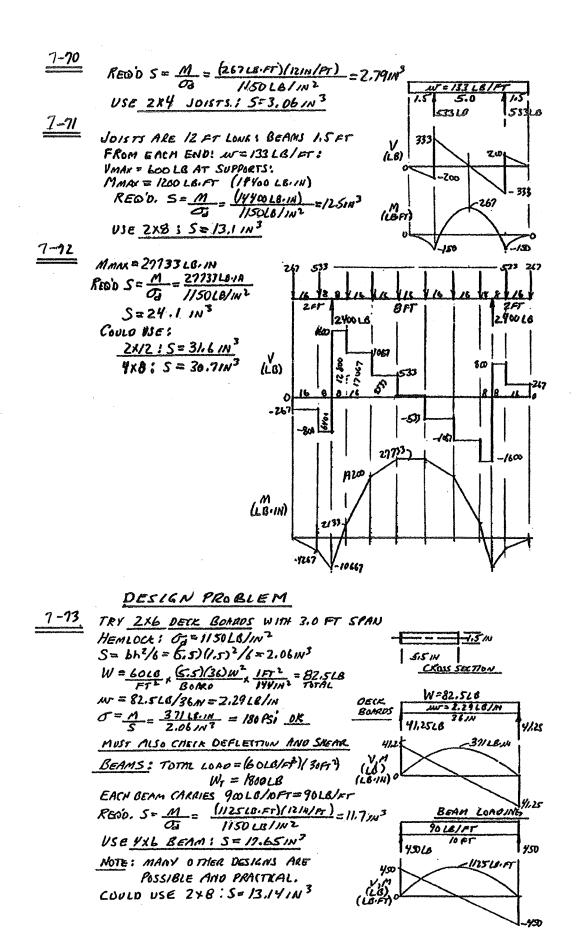
<u>Problems 7-53 to 7-62</u> use the same set of beam loadings as 7-33 and 7-42 but the material is ASTM A572 Grade 60 with $s_y = 60$ ksi (414 MPa). Then,

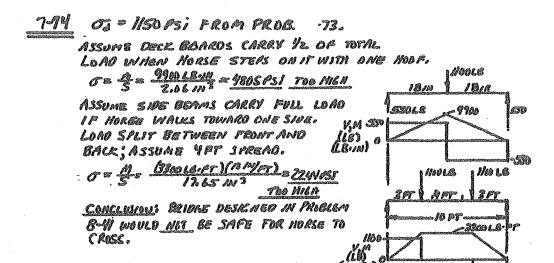
Design stress: σ_d = 0.66 s_y = (0.66)(60 000 psi) = 39 600 psi (273 MPa). The objective is to specify the lightest wide flange beam.

The results for these three sets of problems are summarized below.

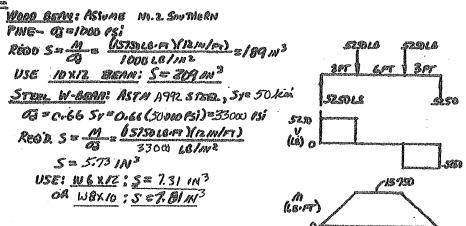
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THE PROPERTY OF THE PARTY OF TH	open component and a second	ASTM.		$s_y = 60 \text{ ksi } (41)$	4 MPa)				
Prob.	Fig.	M _{max}	Req'd.	Lightest	Prob.	Lightest	Prob.	Req'd.	Lightest
No.	No.		S	W-beam	No.	S-beam	No.	S	W-beam
7-33	P5-3	45.7 K-ft	16.6 in ³	W12x16	7-43	S10x25.4	7-53	13.8 in ³	W12x16
7-34	P5-7	71.5 kN-m			7-44	S250x37.8	7-54	2.62x10 ⁵ mm ³	W310x23.8
7-35	P5-8	43.2 kN-m	1.89x10 ⁵ mm ³	W310x23.8	7-45	S200x27.4	7-55	1.58x10 ⁵ mm ³	W250x17.9
7-36	P5-11	60.0 K-ft	21.8 in ³	W14x26	7-46	S10x25.4	7-56	18.2 in ³	W8x21
7-37	P5-16	170 kN-m	7.47x10 ⁵ mm ³	W460x60	7-47	S380x64	7-57	6.23x10 ⁵ mm ³	W310x44.5
7-38	P5-36	10.0 K-ft	3.64 in ³	W8x10	7-48	S5x10	7-58	3.03 in ³	W8x10
7-39	P5-40	40.0 K-ft	14.5 in ³	W12x16	7-49	S8x23	7-59	12.1 in ³	W12x16
7-40	P5-52	148 K-ft	53.8 in ³	W18x40	7-50	S15x42.9	7-60	44.8 in ³	W18x40
7-41	P5-63	1450 N-m	6.37x10 ³ mm ³	W200x15	7-51	S80x8.5	7-61	5.31x10 ³ mm ³	W200x15
7-42	P5-64	30.0 K-ft	10.9 in ³	W10x12	7-52	S8x18.4	7-62	9.08 in ³	W10x12

7-63	Od = 1000 Psi	TOTAL LOADS /ZDLB
	REOD. S= M = (ISESLE.FT)(1210/pg) = 18.81N3	Ser Ser
	USE Z x10 WOOD BEAM	625LB 625
	VM	
7-64	War and the second seco	O presenta anticonomina anticonomica anticonomica de la constantina del constantina de la constantina
,	Od = 1830 PS1	
1 5, 2 /6	4 m Am I J Ad ² I+Ad ² 25 1.75 9.188 5.36 1.907 19.085 24.445 287 4.25 71.698 3.184 5.53 5.939 9.103	: 200 LB/FF 2.F
	12 \$A _N = 80.886	1000
	$\overline{Y} = 3.66 \text{ IN} = C$ = MC(1875 L6.Fr\Y/2/W/Fr\X3.66/M) (L6)	
0	13.55WY	-500
7-65	UNSAPE	-1000
Communication of the control of the	PROCEGURE SAME AS 7-64; 03=1150951 M	IB75L8·A
	WITH 2x8 VERT. MEMBER, 0= 798 PSI LB.F.	
	WIM ZY & VERT. MEMBER:	V-62518 Pr V
	7=C=6.186M; I=177.31N4 0=(1875)(0)(6.286) 798 PSi OK	
7-66	• • • • • • • • • • • • • • • • • • • •	
Similar (Survey or or all and operated to	PROCEOURE SAME AS 7-64 WITH DOUBLE-WIDTH	
	WITH 2-2×6 VERTICAL MEMBERS: $\vec{V} = C = 4.5$ $C = \frac{(1875)(12)(-4.519)}{146.9} = 692 \text{ ps}; \text{ OL}$	19 M; I= 146.9 IN4
7.1.9	141.9 = 692 PS; OK	
7-67	DESIGN PROBLEM - MULTIPLE SOLUTIONS PO	55/0 LE
7-68.	IN THE MIDDLE OF THE DECK, EACH FOOT	DE JOIST LENGTH
Collegeographical	CARRIES A 16 IN WIDE PART OF THE DECK	
	N= 100 LB , U6 W/(12H) . 1FT2 = 133	
	SPECIFY NO.2 HEMLOCK: OF USO PSI	M= 1067 LB.
		AV = 13 LB/FT
	- W 11 DA PALIM.	SIJLE FT 533
	USE 2XB; 3=13.141N	
7-69	JOISTS ARE 12 FT LONGE BEAMS	497
	AT ENOS: W= 133 LO/FT:	1067 7-333
	MMAX = 2400 LB.FT (2880) LB.IN)	
	REO'D S = M = 28800L8·IN. = 25.0 IN3 -USE	ر برد کا ۱۲ه کا در برد کا در برد کا در برد کا در
	1150 LB/INE 625.0 IN -105E	Entrice Jul 1911

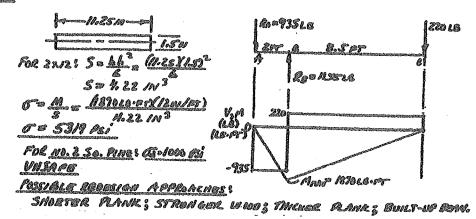


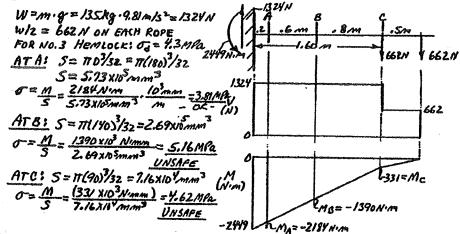


7-15



7-76





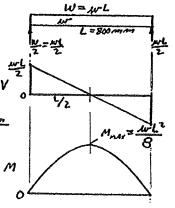
7-78 $M_{MAX} = 6400 L8 \cdot IN AT B$ ASSUME 2×4 PLACED AS; $S = 3.06 W^3$ $O = \frac{M}{3} = \frac{6400 L8 \cdot IN}{3.06 IN^3} = 2042 PS'_1 + 1.5$ $O = 1000 PS'_1 FOR NO. 2 SO. PINE - UNSAFE$

80018 P=8018 8 80m C

MHAX = 3.89 XID NIMM = W L2/8

WMAX = 8 MMAX = (8 X 3.89 XN NIMM) = 4.86N/mm

L2 (800 MM) 2



7-80
FROM P 6-9: I = 1.35 × 10 mm 1, C = 20,0 mm

MMAX = (2,25 &N X 0.20 m) = 450 N·m

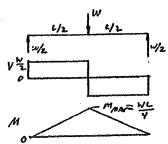
0 = MC = (450 N·m)(20,0 mm) . 10 mm = 66.7 MPa

1.35 × 10 5 mm 1 m

REO'D. FLEXUAL STRENGTH = 30 = 3(66.7) = 200 MPa

COULD USE: NYLON 6/6, POLY 1 M/ 18E

 $\frac{7-81}{60} = \frac{7-81}{2} = \frac{90 \text{ mps}}{2} = \frac{15.0 \text{ mm}}{2} = \frac{10.0 \text{ mm}}{2}$



$$\frac{7-82}{\sigma} FROM PB-12 : I = 1.7xN^{1} mm^{1}, C = 12.39mm$$

$$\sigma = \frac{MC}{I} = \frac{(81.2 \text{ N'm})(12.39mm)}{[.7 \text{ Niffmm}^{1}]} \frac{10^{2}mm}{m}$$

$$\sigma = 59.3 \text{ N/mm}^{2} = 59.3 \text{ MPa}$$

$$N = \frac{54}{\sigma} = \frac{76 \text{ mPa}}{59.3 \text{ NPa}} = \frac{1.20}{321 \text{ N}}$$

$$C = 1.28 \text{ IN}$$

$$\sigma = \frac{51}{3} = \frac{1000 \text{ PS}}{3} = 3667 \text{ IS} = \frac{m_{\text{MAU}} C}{I}$$

$$M_{\text{MAX}} = \frac{\sigma_{\text{G}} I}{C} = \frac{3667 \text{ IS} (0.02) \text{ SIN}^{3}}{128 \text{ IN}} = \frac{85}{128 \text{ IN}}$$

$$M_{\text{MAX}} = \frac{2367 \text{ IB} \text{ IN}}{C} = \frac{4(2367 \text{ IB} \text{ IN})}{140 \text{ IN}} = \frac{67610}{C}$$

$$M_{\text{MAX}} = \frac{4(2367 \text{ IB} \text{ IN})}{140 \text{ IN}} = \frac{67610}{C}$$

7-86	HAT	SECTIO	N FROM	P 6-14	` <i>₩ /™</i> !० ० ४	· LAWER F	PLATE
PART	AIN	Am		4	Ad2	I+AJ2	
	12 .05	.006	Paragraphic of Spinson				BOTTOM FLANGE (2x.6x.1)
2 .:	30 ,75	.225					2 WEBS 2x1.5x.1
3 .	2 1,45	.124					TOP FLANGE (1.2 x 0.1)
1A	TY EAM	=.465					Posteriora contentamento de la contentamento del contentamento del contentamento de la contentamento del contentamento del contentamento de la contentamento del contentamento del contentamento de la content
7 -87	Ix = M MMAX = WMAX = FROM OD = MMAX	140/1.5 15 00 11 15 00 11 16 - 19 16 - 19 16 - 19 17 00 11 18 00 11	$\frac{1}{2} = \frac{7250}{1N^2} = \frac{7780}{27M}$ $\frac{1798 L}{27M}$ $\frac{1}{2} = \frac{1}{1500 L}$ $\frac{1}{100 L}$	0 (1.30) ² 12 1417 2417 - 7 2506 / A	= 0.174 IN 15 IN = 17	98 LB V H 70 M 100 PS i 18 LB M	1.20 1.50 X 1.30 1.40 1.40 MAY = WL = WL ²

$$\frac{7-88}{M_{MAX}} = \frac{\sigma_3 \pm}{C} = \frac{6830 \pm 6}{10^2} \cdot \frac{0.8263 \text{ in}^2}{1.28 \text{ in}} = \frac{4409}{6} \pm \frac{41081}{6} = 6.83 \text{ ksi}$$

$$W = \frac{2m_{MAX}}{L^2} = \frac{2.14402 \pm 6.10}{42 \times 10^2} = \frac{5.00 \pm 8/\text{in}}{1.28 \times 10^2}$$

BEAMS WITH STRESS CONCENTRATIONS

AND VARYING CROSS SECTIONS

7-89

Mx = ALLOWABLE MOMENT AT JOINT

\(\tau = \text{Ke Mx/S} \) \(\text{S=2.39Y/N}^3 \) FOR \$\frac{1}{2} \text{In RPE} \) \(\text{HDO} \)

Mx = \(\text{CBS} \) \(-\text{Z0000LB/M}^3 \) \(\text{Z-39Y/N}^3 \) \(\text{LOND} \) \(\text{LE} \)

Mx = \(\text{CBS} \) \(-\text{Z0000LB/M}^3 \) \(\text{Z-39Y/N}^3 \) \(\text{LE} \)

\[
\text{My = \(\text{LE} \) \(\text{MOD} \) = \(\text{LE} \) \(\text{LE} \)

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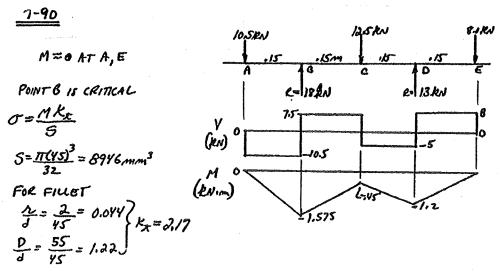
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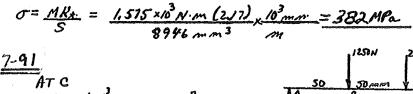
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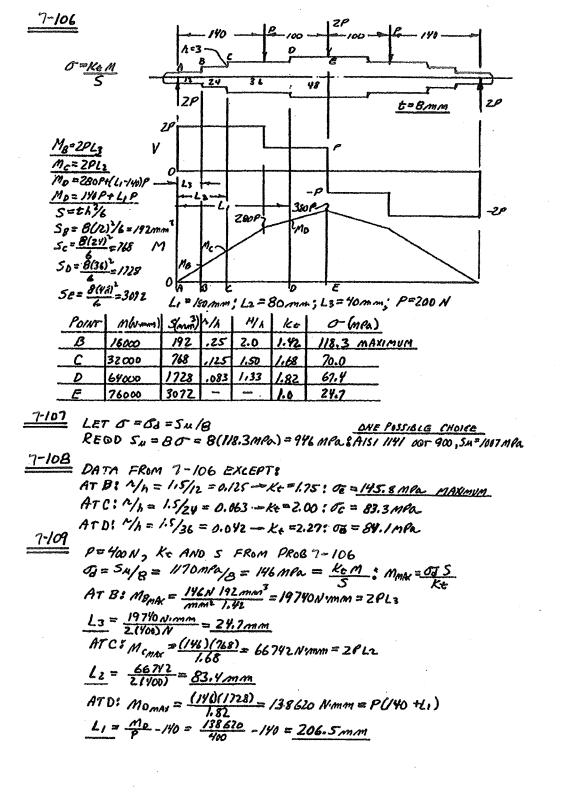


 $\frac{7-91}{S^{2}} = 572.6 \, mm^{3}$ $\sigma = \frac{MK_{6} - (114 \, N \cdot m)(3.0)}{S} \times \frac{10^{3} \, mm}{S}$ $\sigma = 398 \, MPa$

```
FOR DI: S= TIDI/2 = TT 10.65 3/32 = 0.03687 IN3
                                                                                                                                                           28012 1650LE
                             FOR DZ: S= TT(1.00)/32 = 0.0982 IN3
                                                                                                                                           3.0
                                                                                                                                                              2.0
                              FOR D3: S= # (0.94) 32 = 0.08154 IN3
                                                                                                                                    141918
                                                                                                                                                                                   2.K-
                       ATC: Ke=2.0 (Keksem)
                                                                                                                                                                                   2.00
                                                                                                                             419
                             0 = KL.Mc = 2.0(1535) = 3/270 (5)
                                                                                                                          (L8)
                    ATO: 1/d= .01/94= .0106: 1/d=1.00/.94=1.06
                                     Kt = 2.55; Mo = 15928-1A (GROOVE)
                   Kt = CSS, MO = 135720111 

O = (25$) 13$9; \lass = 4250005;

AT E; \( \begin{align*} \land \delta \d
                                                                                                                                                               1535
                                                                                                                                                                                   1359
                                                                                                                                              1251
                                                                                                                        (LB·/N)
            7-93
                      AT FULCROM C:
                                                                                                                                                                                        ZØ
                     S= 613/6 > .75/2.01) 1/6=0.50/N3
                                                                                                                        600
                          = M = 400018.1N = 8000 PSI
                                                                                                                            1200
                                                                                                                                1800
                  AT HOLE B: DH=0.75=d
                         d/w= .25/20=0.375-Kt=1.0
                   O = \frac{Ke 6MM}{(M^2 6^3)(e)} = \frac{(1.0)(6 \times 24/6)(7.6)}{(2.0^3 - .75^3)(0.25)} = \frac{506765i}{}
                                                                                                                                   2400
                  AT B2 : M= R0 : 0 = 3800 PSi
                  ATB3: N= 1200! 0 = 2534 151
                                                                                                                                                                       400
                                                                                                                                        400
                 ATBY! M= 600; 0= 1267 85i
              ATC! 0=8000 PSi (FROM 7-93)
             ATBI: 3/4 = 1.38/2.0=0.69-K+=1.40
                                                                                                                                                                                    ZOIH
               0= K= 6Mw _ 1.40 /6) (2400) (2.00)
                     (w3-d3)+ (203-1.583)(.75)
             AFB21 0=150605i : AFB2:0=5001 PSi
                                                                                                                                                                                        200
                                                                                                                    M (LB.IN)
                                                                                                                                                        0 200
V(LB)
             Ar By! 0 = 2500 PSi
1-95 d/w= 1.25/2.00 = 0.625 - Kt=1.27 AT HOLE
                                                                                                                                             AT FULCRYM, C
                                                               1.27)(6)(2.00)
                                                                                                             M<sub>B,</sub> = <u>3.36 M</u> B,
                                                                                                                                                S=0.50 IN3 (SEE 7-93)
                                                                                                                                               0= Me/3=2.0Me
                                                                (2.03-1.257.75)
                                                      CD
                                                                                                                          RA
                     PIVOT
                                                                         Me
                                                                                                  OF
                                                                                                                                          A8,
                                                                                                                                                            MB,
              a) END HLE
                                                                                                 8000 Psi
                                                                       4000 LB-N.
                                                     ZOIN.
                                                                                                                      200 LB
                                                                                                                                        121H.
                                                                                                                                                      240018.14.
                                                                                                                                                                                BOGYA;
               b) HOLE BY
                                                    17 IN.
                                                                      3400
                                                                                                 6800
                                                                                                                      170
                                                                                                                                         9
                                                                                                                                                      1530
                                                                                                                                                                                5141
               C) HOLE B3
                                                   141H.
                                                                      2800
                                                                                                5600
                                                                                                                     140
                                                                                                                                                        840
                                                                                                                                                                                2822
               d) HOLE B2
                                                                                                4400
                                                   11 IM.
                                                                      2200
                                                                                                                    110
                                                                                                                                                       330
                                                                                                                                                                               1109
               C) HOLE B,
                                                   8 IN.
                                                                      1600
                                                                                              3200
                                                                                                                     80
                                                                                                                                                         0
                                                                                                                                                                                 0
   7-96 M= F(52 + 25/2)=/2500NY64.5 mm)=16/250 N.mm
                    AT A-A; S=bh2/6=16(25)2/6=1667 mm
                     0= M/s = 16/250 N.mm)/1667mm3 = 96.8 MPa
   7-97
AT B-B: d/w = 12/25 = 0.48 - Ke = 1.0
                     O = \frac{ke 6 M w}{(w^2 - d^2)(t)} = \frac{(1.0)(6)(16/250)(25)}{(25^2 - 12^2)(6)} = \frac{108.8 \text{ mPa}}{108.8 \text{ mPa}}
```

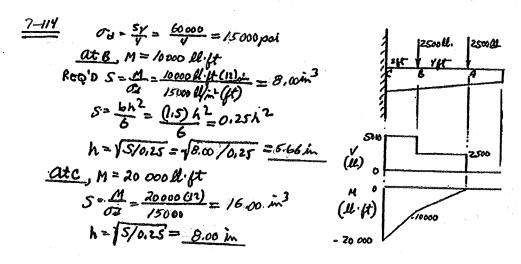


$$\frac{7-110}{AT B1} P_{MMN} = \frac{O3 36}{Kea} = \frac{126.8 M Pac}{M mm^2} = \frac{17138 M mm}{1.492} = 17138 M mm^2 = 2PL3$$

$$\frac{AT B1}{P_{MMN}} = \frac{O3 36}{Kea} = \frac{126.8 M Pac}{M mm^2} = \frac{17138 M mm^2}{1.492} = 17138 M mm^2 = 2PL3$$

$$\frac{AT C!}{P_{MMN}} = \frac{(126.8)(168)}{2(10)} = \frac{57943 M mm}{2(10)} = \frac{2PL3}{M mm} = \frac{17138 M mm^2}{2(10)} = \frac{2PL3}{2(30)} = \frac{362 M}{362 M mm} = \frac{17138 M mm}{2(10)} = \frac{17138 M mm^2}{2(10)} = \frac{17$$

 $\frac{7-1/3}{0J} = \frac{SM}{8} = \frac{793 \, mR_0}{8} = \frac{99.1 \, mR_0}{9} = \frac{99.1 \, mR_0}{9} = \frac{1200 \, N}{99.1 \, mR_0} = \frac{1200 \, N}{99.1 \, mR_0} = \frac{1200 \, N}{99.1 \, mR_0} = \frac{144000 \, N \, mR_0}{99.1 \, N \, lmm} = \frac{144000 \, N \, mR_0}{99.1 \, N \, lmm} = \frac{144000 \, N \, lmm}{99.1 \, N \, lmm} = \frac{144000 \, N \, lmm}{99.1 \, N \, lmm} = \frac{144000 \, N \, lmm}{99.1 \, N \, lmm} = \frac{144000 \, N \, lmm}{1200 \, N \, lmm} = \frac{144000 \, N \, lmm}{1200 \, mM} = \frac{144000 \, N \, lmm}{1400 \, lmm} = \frac{144000 \, lmm}{14000 \, lmm} = \frac{144000 \, lmm}{14000 \, lmm} = \frac{144000 \, lmm}{14000 \, lmm} = \frac{144$



OBF 0,66 SY = 0.66(SUES)) = 33 KS 1 = M/S REQ'D. S= M/OB = (15 K.F.F) (121N/F.F) /33K/INT SMIN = 16.36 IN3: USE W 12×16; S=17.11N S WEIGHT = (1618/F.F)(12FT) = 19218 15K 15K1 (k) o -15 7-116 USE WIDER WITH COVER PLATES ON MIDDLE PART IX = 53.8 IN2, DEPM = 9.87 IN, S = 10.9 IN3 Ix = 53.8 IN2, DEPM = 9.87 IN, 3 = 10.9 IN3
WITH COVER PL: IT = Ix + ZAd = 53.8+ (.875) (5.31)(2) = 103.1 S=I/c = 103.1/5.185 = 19.881N3 - OK FOR MMAX FIND ALLOWABLE M FORW 10X12 ONLY Mx = 02 S = B3KS1 (10,91N3) = 359 K.IN = 29,975K.FT Mat C=5./85 9.87 AM FROM MMAXTUMY: 45.0-29,975 = 15,025 KIFT=AY 5.3/IN Vy = 2.5 M : DM = Vy M/2 = 2.5 M/2 = 15.025 10137 M=3.467 FT. SEECIFY X=2.5FT, M=3.5 ft PLATES COVER MIDDLE 7.0 FT. OF BEAM C1/11X3.5PL, WT. OF PLATES! = Z PAL = 2 (0.283 W/, N) (0.8751N) (84.01N) = 41.6 LB; WT OF WIOXIZ = (12 LB/FT(12FT) Ap= 6.25 (3.50) = = 144 LB1 TOTAL WT = 144+41.6 = 185.6LB An=0.875/N2 WI SAVINGS = 192 -185.6 = 6.4 LB - SMALL

FLEXURAL CENTER

 $C = \frac{b^2 h^2 t}{4Ix}$ • $I_X = \frac{38(76)^3}{12} - \frac{34(69)^3}{12} - 4.992 \times 10^5 mm^4$ 6=38-2=36 mm; h=76-4=72 mm; t=4mm e= (362)(72)2(4) = 13.5 mm FROM MIDDLE OF WEB QIS AT C-Z = 11.5 MM FROM LEFT FACE OFWEB.

7-119								display-and and an analysis an	T
t	C'	d'	Ix	6	1	e(mm)	e'= e- %		
2.5	375	15	7/731	37.75	75.5	14.16	13.91	-e'	
1.6	364	14.8	219 745	37.20	74.4	13.94	13.14	x Q + x	76 1
3.0	0 35.0	70.0	389674	36.50	73.0	13.66	12.16	he H	ī
7-120	P ty								
	h=2	2.00-0	1./2 = 1.86	MIC=	.50+	12 = 0.56	SN 16=2.0	0012=1.88/w	1
	b/h=	1.00	; %/A=	0.298;	e/1:	F0.46		- C	
	0=0	0.46	1 = 0.460	(1,88) = 0	865.0	~		I'x = Cd' - Cd'	
	≃′≃	e-t	1/2 = _865	r- 106 =	0.805.	IN FROM	LEFT FAC	(E	

t	1 6	C	6	c/h	6/A	9/B	e	e'	
•020	1.980	,5100	1.980	.258	1,00	.48	.950	,940	ALL DIMENSIONS
,063	1.937	,53/5	1.932	.274	1.00	.46	,891	.860	IN INCHES
./25	1.875	5625	1.875	.300	<i>/.</i> 00	.45	.844	,781	

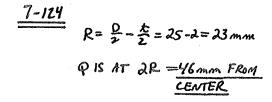
$$\frac{7-122}{h=80-3=77mm}; C=20-1.5=18.5mm; b=50-3=47mm$$

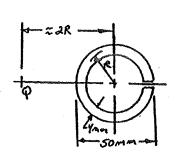
$$\frac{6}{h}=\frac{47}{17}=0.61; C/h=18.5/17=0.24:THEN 6/h=0.35$$

$$C=0.35 h=0.35(77)=27.0mm$$

$$C=0-\frac{1}{2}=27.0-1.50=25.5mm FROM LEFT FALE$$

7-123	t	h	C	6	1 %	6/A	e/h	e	e1
	a.50	79.5	19.75	49.5	0.248	0.623	.38	30.2	30.0 .mm
and the second	1.60	78.4	19.20	48.4	0.245	0.617	.37	29,0	28.2 111 11
\$	3.00	77.0	18.5	41,0	0,24	0.61	0,35	27.0	25.5 MINT

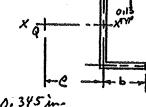




IX = 0,288 IN (CFROM APPENDIX) OVERALL DIMENSIONS 2.00 IN. DEPTH = D · 1.00 IN. NIOTH = B

h= D-t= 2.00-0.13 = 1.8111 $b = B - \frac{t}{2} = 1.00 - \frac{0.13}{2} = 0.935 \text{ IN.}$

 $C = \frac{b^2 h^2 \pm}{4 I_x} = \frac{(0.935)^2 (1.81)^2 (0.11)}{4 (0.288)} = 0.345 \text{ in}$



1-126 = 25+5=30mm: C=20-2,5=17.5mm: b=45-5=40 mm %= 0.58 : 6/6 = 1.33 : THEN 8/A & 0.43 BY EXTENDIATION e = 0.43 h = 0.43(30) = 12.9 mm

BEAMS MADE FROM ANISOTROPIC

FROM P6-15: I = 0.3572 INV; C6=1.068 IN 5 Ct = 1.332 IN; L=6.5FT = 78/N
FOR TENSION ON BOTTOM: MAN = AT I 19000 LB 0.3572 INV 6355 L6.1N

FOR COMP. ON TOP: MAX = CBI _ 14000 LB . 0.3512/N = 3754 LB VAL FROM 8-47: MMAY = W-L7/1

WMAX = 8 MMAX = 8(3754LB-1A) = 4.94LB/IA

 $\frac{7-128}{TENSION MT BOTTOM; M_{MAX} = \frac{O3I}{C} = \frac{(19000)(0.2512)}{1.332} = \frac{5095}{C}$ $COMP. ON TOP: M_{MAI} = \frac{(21000)(0.3512)}{1.068} = \frac{1024}{1.069} LIMIN$ $W_{MAX} = \frac{BM}{L^2} = \frac{8(5095)}{(78)^2} = \frac{6.70}{1.068} LIMIN$

7-129 FROM P6-6: I = 6.167 × 10 mm (C6=12.5 mm; C6=17.5 mm)

TENSION AT BOTTOM: MMAX = 05 I (100 m) (12.5 mm) = 4.93 × 10 N·mm

(OMPRESSION AT TOP: MMAX = 05 I (70) (6.167 × 10) = 2.47 × 10 N·mm

LIMITING VALUE MMAX = WL/4 (SEE 8-81)

WMAX = 4 MMAY = 4 (247 x10 Nmm) = 822 N

```
FROM P6-6 : I=6.167 ×10 mm
                                                                                              12.5 MM
             C+ = 125mm, C+= 17.5mm
            COMPRESSION AT TOP: MMAX - GCI
                MMAX = 70 N (6.167 XID MAX) = 3.45 NO N. amon - LIPITING VALUE
                                                                                              17.5 mm
            TENSION AT BOTTOM: MAN C. = (100) 6.167 K/04) = 3.52 K/0 5 Nomm
             WMAX = 4 MMAX = 4(3.45 ×105 Nemm) = 1/50 N
          FROM P6-8: I=5.36x10 mm; C, =C=20mm
           COMPR. AT TOP: MMAX = THE I (70NKS.36XH MM) = 1.876XH N.MM

CE MM (20.0 MM) LINITHE VALUE
           TENSION AT BOTTOM: MAX = GE [ = (100)(_S36XIB) = 2.68XID NIMM

WHAT = 4 MMAY = 4 (1.876 XID NIMM) = 625 N

1200 mm
          FROM P6-9: I = 1.35 x10 5 mm 1. C1 = Cc = Z0 mm
           COMPRESSION AT TOP IS LIMITING
              M_{MAX} = \frac{O_{0}c I}{Cc} = \frac{10N(1.35 \times 18 \text{ mm}^{9})}{mm^{2}} = 4.73 \times 10^{5} \text{ N.mm}
W_{MAX} = \frac{4 \text{ max}}{L} = \frac{4(4.23 \times 10^{5} \text{ N.mm})}{1200 \text{ mm}} = 1525 \text{ N}
7-133

FROM P 6-4: I = 4,64 × 10 mm '; C6= 7= 152,5 mm; Ce=72.5 mm

C= ASTM AV 8, GK 40: O36 5 At 276 MPA = 69 MR; O4C - 5MC = 765 = 241 MPA

O= MC: MARE C = 241 ... (4.64 × 17 mm)

[ 1.0 m | .8 m | 10 m | R-P
           COMP. AT TOP: M = OSE I 24/N (4.84 x 17 mm)

MAR = 1.54 X 10 8 N. man
           TENS. AT BUTTON: MAAN GG. F. (89 X4.5/AN)
              MMAX = 2.10 x10 N.mm -LIMITHE VALUE = (1040)(P)
              PMAX = MMAX/1.0m = 2.10 x/8 N. MM/1000 MM = 21.0 X/8 = 21.0 RM
         FROM P 6-5 : I= 2.66x0 mm; Cb= \( = 35.0 mm; Cb = 25.0 mm

ASTM AZZO, 8000ZE OFE = SAFY = 655/4 = 164MPa; OFE = 54/4 = 1650/4 = 413 MPa
            O = MC . MMAX : OFE
                                                                                  -La 1.20m --
          COMP. AT TOP : MMAK = OGC F - 4/3 N(2.66X6 MM)
              MMAR = 4.39 X10 ( NIMM
          TENS. AT BOTTOM: MARK = To I _ (64 X2.646)
              MAN = 1.25 X10 Nimon - LIMINAL VALUE " WITE
             WMAX = BMMAX = B(1,25×10 Ningm) = 6.94 N, 10 mm = 6.94 RN/m
             TUTAL LOAD = AV-L = (6.94 KN/m) (1.80 m) = 8.33 KN
```

7-136 Ode = 5m/10 = 827/0Pa/10 = 82.7 MPa & Ode = 544/10 = 1240MPa/10 = 124 MPa

A | N | AN | I | J | AJ2 | I+AJ2 | 56250 1625 9.14x106 26.4x106 25 35.11x106 61.56x106 TOP = 75000 244=10.31x106 I = 191.4 x106mm4 EA = 75000 ZA 4= 10.31206 Y= 137.5 mm = Cb; Ct = (200-Y)= 62.5 mm

TENSION AT BOTTOM: MANY = 450 I _ 82.7N . 191.4 x10 mm = 1/5.1 x106 Nomm COMPR. AT TOP: MMAX = Tac I = (124)(191.4)(104) = 379.8×10 Nomm

zρ

MMAX = 2.4 P PMAX = MMAX - 1/5/X/0 N/mm = 48.0 KN INCREMSE DEPTH OF RIGS TO ZSOMM zp V THEN Y=222.5 mm = Cb; Ce #325-7-102.5mm I = 815,8 x/1 mm4 TENSION AT BOTTOM: MMAX= (82.7) &15.8×10)

MMAX = 303. Z X/8 & N. mm.

Comer. AT TOP: MMAX = (12448/5.6 XII) = 986X/6

PMAX = MMAX 303X/6 Nomm = 126 kN

7-138 DESIGN PROBLEM - MULTIPLE SOLUTIONS POSSIBLE

7-139 ASTM A48 GAST IRON. $S_{M}=276MPA-BRITTLE$ $O_{d}=S_{M}/_{6}=276MPA/_{8}=46.0MPA.$ $ACTUAL O_{MAX}=\frac{M}{S}=\frac{(2.4\times10^{3}N)(350mm)}{TT(50mm)^{3}/_{32}}-68.4MPA/_{9}$ UNSAFE

7-140 FROM FIG. 7-15: MMAX = 45900 LBIN. OI = SW/8 REPEATED LOAD

AL. 6061-TG SM = 45000 PSi. OM = 45000 PSi/0 = 5625 PSi

O = M/S. REQ'D S = M/OJ = 45900 LB-IN/5625 LB/IN²

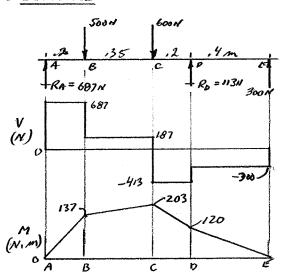
SPECIFY GIX 4,692 ALUMINUM I-BEAM SHAPE. S= 8.50IN³

7-141 FIND MAX. STRESS. POINTS B OR D

POSSIBLE SECTIONS

AT B; d = 40 mm, $M_B = 150 \text{ 000 N·mm}$ $\leq 1EP$; $d/_D = \frac{80}{40} = 2.80$ { K = 1.91 $1 = 3.0/4_D = 0.075$ } APPA = 1.91 $S = \frac{\pi}{32} = \frac{11}{32} = \frac{111}{40 \text{ mm}} = 6283 \text{ mm}$ (N) $GR = \frac{M_B \cdot Kc}{56} = \frac{(50000 \text{ N·mm})(1.91)}{6283 \text{ mm}} = \frac{47.0 \text{ Mlo}}{150000}$ $AT D^4$; d = 60 mm; $M_D = 300000 \text{ N·mm}$ (N·mm) GROOVEI D/dq = 80/60 = 0.10) APP A2-9 $S = \frac{\pi}{60} (60) = 0.10$ APP A2-8 $S = \frac{\pi}{60} (60) = 0.10$ APP A2-10 $S = \frac{\pi}{60} (60) = 0.10$ APP A2-

7-142 SHAFT D=30.0 mm, MmAx=203 N·m $S = \Pi \frac{O_{32}^2}{32} = \Pi \frac{(30 \text{ mm})^3}{32} = 2651 \text{ mm}^3$ $\frac{O = M}{S} = \frac{203 \text{ N·m}}{2651 \text{ mm}^2} \cdot \frac{10^3 \text{ m/m}}{m} = 76.6 \text{ MPa}$ $O_d = \frac{SM}{B} = 600 \text{ MPa}/B = 75.0 \text{ MPa}$ A15/10% W QT 1300. Sn=608 MPa $BECAUSE O_{MAX} > O_d - UNSAFE$



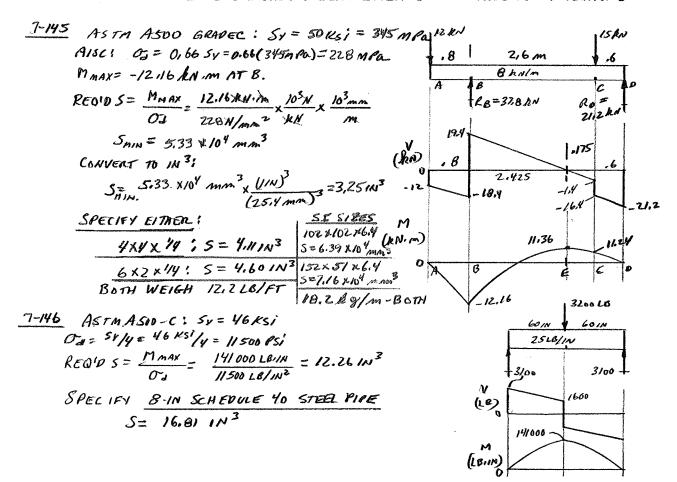
154 7-143 ASTM A.992, SY=50000PSi, STATIC LOAD YKIFT A156: 02 = 0.66 Sy = 0.66 (5000) = 33000 PS, A 8FT Mnax = 183, ZK-FT x 1000 LBx x 1214/FT = 2,20 ×106 LBM tra=36.6K REO'D $S = \frac{M_{Max}}{\sigma_0} = \frac{2.70 \times 10^6 \, LS \cdot IN}{33000 LB/IR^2}$ (K) 5 MIN = 66.7 IN3 -15.4 SPECIFY WIBX40; S= 68.41N3 -30.4 14.8 -183.2 CHELK SHEAR STRESS IN WEB. CHECK LATERAL BRACING AND DEFLECTION (K-F1) SAME. AS 7-143 BUT ASTM ASTZ, GR 65 Sy = 65000 ps;; Of = 0.66 Sy = 0.66(65000 Psi) = 42900 Psi REO'D 5 = MMAX = 2,20×106 LB.IN = 51.3 IN3

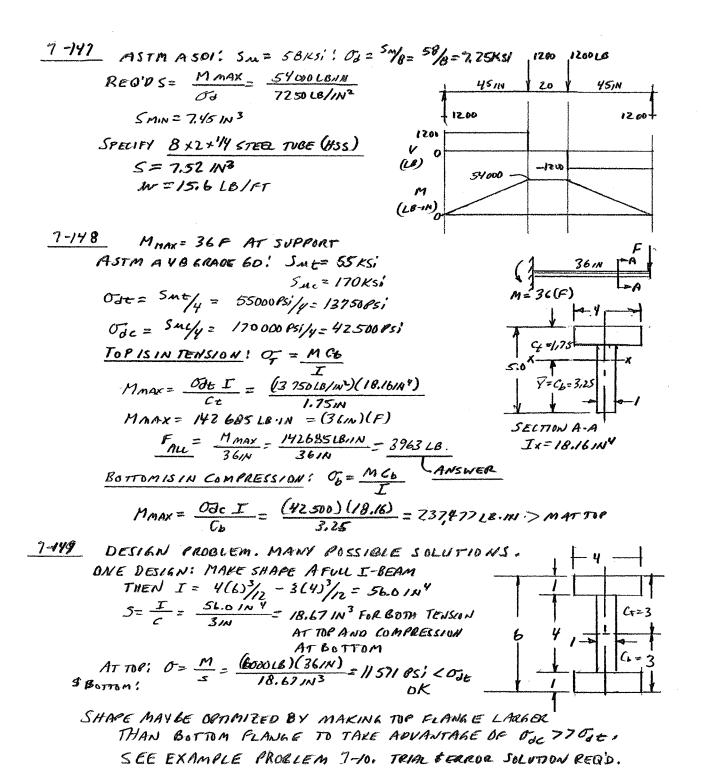
SPECIFY W18x40; S= 68.41H3. NO BENEFIT, BUT CHOICES ARE

LIMITED IN THIS BOOK. SEE ALSO MANUAL FOR LARGER SECUTION.

COST/LB MAY BE HIGHER. ALSO CHELL WEB SHEAR, DEFLECTION,

AND LATERAL BRACING REQUIREMENTS FROM ALSO SPECIFICATIONS.





6750LB 5800 LB 7-150 ASTM AG92; SY=5000083; 30 Od = 0.66 (50 @00) = 33 000 PSi 2,=11300LB REO'D 5= MMAX = 202 500 LB-IN = 6.14/143 4550 SPECIFY WBX10 S=7.81IN3 (LB) 0 CHECK BEAM FOR COMPACINESS, WEB SHEAR, AND LATERAL 1250 SUPPORT REW VIREP. TOTAL WT = 10LB x 1FT x 1001N = 83 LB 6750 PROS X 1×2 8-152 7-151 M 25000 SHAPE IS IDENTICAL TO (LBIIN) O THAT IN PROBLEM 6-44. $I_{x} = 34.95 IN^{4}$ | $O_{d} = 0.66(3600085i) = 2376085i$ $C_{\pm 2}C_{b} = 3.50 IN$ | $S = \frac{m}{\sigma_{d}} = \frac{202500}{23760} = 8.52 IN^{3}$ 185 686 S= 1/c=34.95/3,50=9.99/N3>8,52 IN3. -202500 6x2+14 TUBE WEIGHS 12.2 LB/FT x 100/Nx 1FT = 101.7 LB. PLATES! VOL. IN 1.0 FT 2[(2(0,5) IN2)/2/N] = 24/N3 WT = ZYIN3 x G. 283 CB/103 = 6.79 LB: 6.79 LB x MON, IFT = 56,646 TOTAL WT = 101.7 + 56.6 = 158.3 LB MUCH HEAVIER THAN W 8x 10.

7-152 DESIGN PROBLEM - MANY POSSIBLE SOLUTIONS.

CONSIDER USING A SMALLER, LIGHTER SECTION FOR RIGHT PORTION OF THE BEAM WHERE M IS MUCH SMALLER. THEN ENHANCE THE SECTION WEARRI TO ENABLE IT TO WITH STYND THE LOCALLY HIGH M. PLATES COULD BE ADDED TO THE TOP AND BOTTOM AS IN PROBLEM 7-151 BUT USING A SMALLER TUBE DROTTER SHAPE AS A BASE.

CHAPTER 8 Shearing Stresses in Beams

GENER AL SHEAR FORMULA

$$T = VQ = \frac{(0.500 \text{ N} \times 2.5 \times 10^{5} \text{ m/m}^{3})}{1 \pm (33.3 \times 10^{5} \text{ m/m}^{4}) \times 1.125 \text{ M/m}^{3}} = 1.125 \text{ M/m}^{3} = 1.125 \text{ M/m$$

$$\frac{8-3}{T} = \frac{(1.5)(7.25)^{3}/(2 = 47.63)N^{4}}{(1.813)^{2}} = \frac{(1.813)^{2}}{(1.813)^{2}} = \frac$$

$$\frac{84}{T} = (3.5)(11.25)^3/12 = 415 1N^4 : 0 = (5.625)(3.5)(2.813) = 55.37 1N^3$$

$$T = \frac{V0}{It} = \frac{(20.000)(55.37)}{(415)(3.5)} = \frac{762.051}{12.000}$$

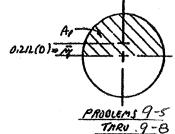
$$\frac{8.5}{A_{p}} = 170^{9}/69 = 17(50^{9})/64 = 3.07 \times 10^{5} \text{mm}^{9}$$

$$A_{p} = 170^{2}/8 = 17(50)^{2}/8 = 982 \text{ mm}^{2}$$

$$A_{p} = 0.212 \ 0 = 0.212(50) = 10.6 \text{ mm}$$

$$0 = A_{p} = 982 \times 10.6 = 10.6 \text{ mm}^{3}$$

$$T = \frac{VQ}{LL} = \frac{(4500)/(040)}{(3.07 \times 10^{5})(50)} = 3.05 \text{ MPa}$$



$$\frac{8-6}{T} I = 77(38)^4/69 = 1.024 \times 10^5 mm^4 : 0 = 17(38)^{\frac{1}{4}} \cdot 0.212(3) = 4568 mm^3$$

$$T = \frac{(2.500)(4568)}{7.024/0^5)(38)} = 2.94 mpa$$

$$\frac{8-1}{T} I = \pi (2.0)^4/64 = 0.785 \text{ m}^4: 0 = [\pi(2.0)^4/8][0.212(2.0)] = 0.666 \text{ m}^3$$

$$T = \frac{(7500)(0.666)}{(0.725)(2.0)} = \frac{3180 \text{ esi}}{(0.725)(2.0)}$$

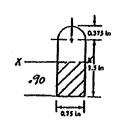
$$\frac{B^{-\theta}}{T} = \frac{1}{\pi (0.63)^{\frac{1}{2}}/64} = 0.00773 / N^{\frac{1}{2}} : Q = (\pi (0.65)^{\frac{1}{2}}/8) [0.412(0.63)] = 0.0208 / N^{\frac{3}{2}}$$

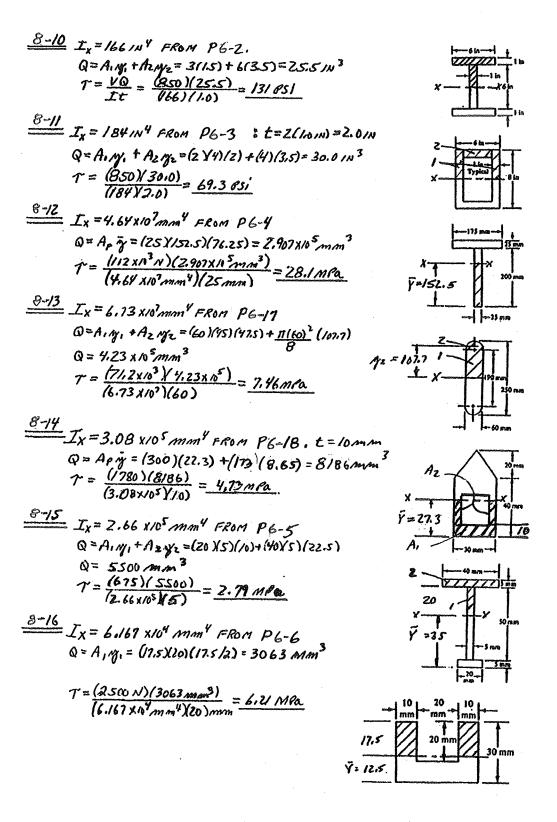
$$\gamma = \frac{VQ}{Tt} = \frac{(850)(0.0208)}{(0.00773)(0.63)} = \frac{3632 \, 0851}{3632 \, 0851}$$

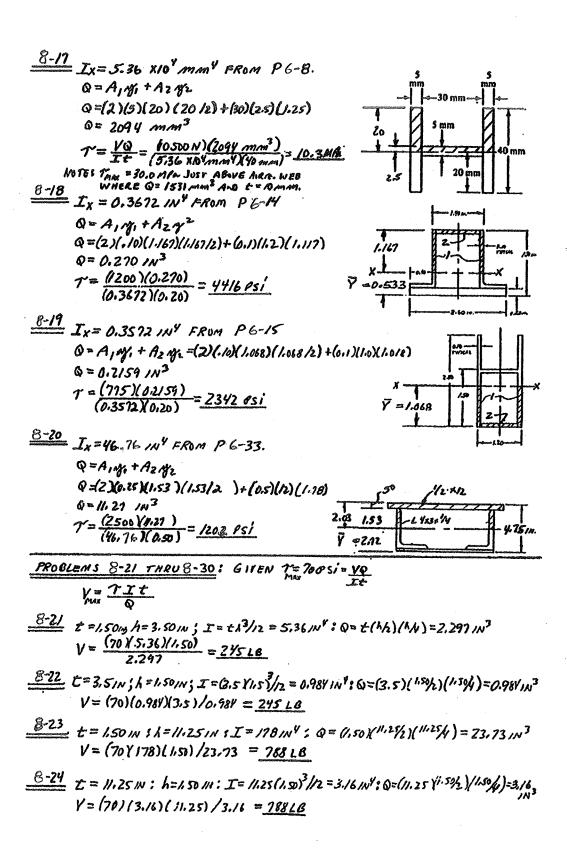
$$\frac{8-9}{Q} I_{x} = 0.366 \text{ int : } \bar{Y} = 0.90 \text{ in } FROM P7-16.$$

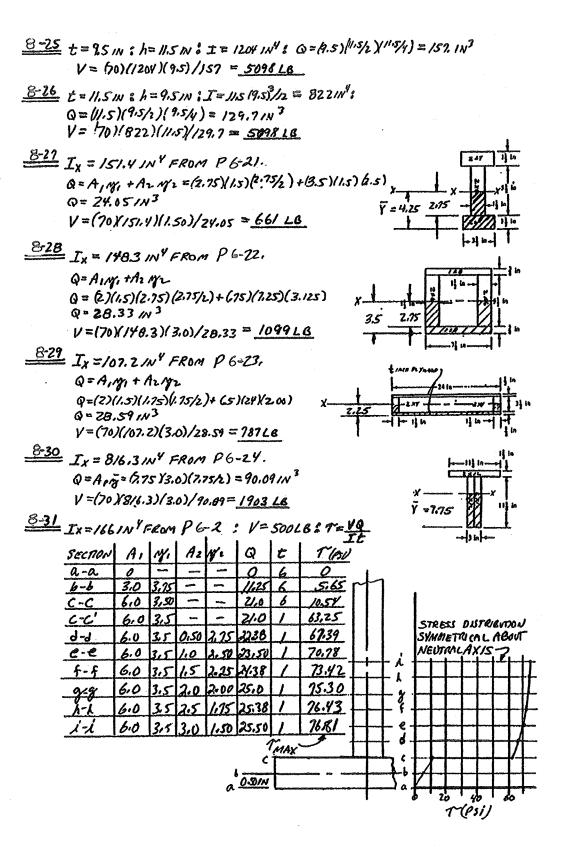
$$Q = (0.75)(0.90)(0.45) = 0.304 \text{ in}^{3}$$

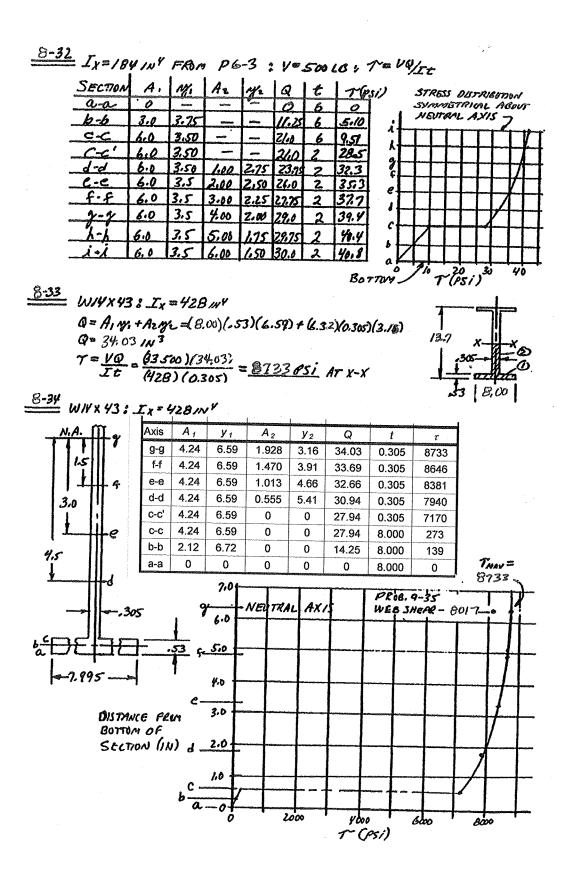
$$T = \frac{VQ}{It} = \frac{(S00)(0.304)}{(0.366)(0.75)} = \frac{1661 \text{ PSi'}}{}$$











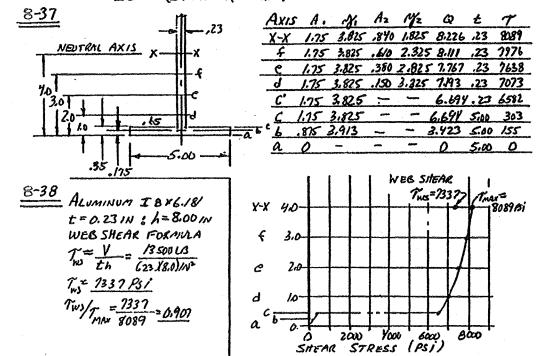
8-36 WIY X43: FOR WEB SHEAR FURMULA: t = 0.305 IN; h=/3.7 IN

Two V = 33500 LB

PROM PROB 8-34: TMAX = 8733 PSi

Two/TMAX = 8017/8733 = 0.92

 $\frac{8-36}{Q} I B * 6.181 ALUMINUM I-BEAM! I_x = 59.69 IN^{9}$ $Q = A. N. + A. N. = (5.00 Y 0.35)(3825) + (3.65 Y 0.23)(1.825) = 8.226 IN^{3}$ $I = \frac{VQ}{II} = \frac{(13500 LB)(8.226 IN^{3})}{(59.69 IN^{9})(0.23 IN.)} = 8089 PSi$



8-39 SEE PROB. 5-4, VMAX - 10K = 10 000 psi; MMAX = 30K-PT = 3.6 x10 5 LB-IN

WIZNO: S = 17.1 IN ; DEPON = 12.00 IN, tw = 0.220 IN.

TWS = \frac{10000 LB}{6.22\)(12.00) IN = 378885; To = 0.40(50000) = 26000 Psi

OF

\[
\text{S} = \frac{10000 LB}{6.22\)(12.00) IN = 21053 Psi; To = 0.66(50000) = 33000 Psi

OK

\[
\text{S} = \frac{17.1 in 3}{17.1 in 3} = \frac{21053 Psi}{10.66(50000)} = \frac{33000 Psi}{3000 Psi}

\]

\[
\text{MMAX} = \frac{3.60 \text{X}(0^5 LB \cdot IN); REO'D S = \frac{10}{2000 Psi} = \frac{3160 \text{X}(05 LB \cdot IN)}{38000 LB/IN^2} = \frac{10.9 \text{IN}}{38000 LB/IN^2}

\]

\[
\text{SPECIFY W 10 x12; S = 10.9 IN \(\frac{3}{2} \); DEP \(\text{R} = 9.87 IN, \text{tw} = 0.190 IN \)

\[
\text{T}_d = 0.45y = (0.4)(50000 Psi) = 20000 Psi - 0K
\]

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8-41 FROM PROB. 5-52: VMAX 44.5K = 44500LB
                                                                                     ASTM A992 STEEL
              MMAX = 148K-FT = 1.776 × 106 LB.IN; OB = (0.66)(5000) = 33 000 PS/

REGD. S = M = 1.776 × 166 LB.IN = 53.8 IN - SPECIFY WIB×40

S = 68.4 IN 3; DEPTH = 17.9 IN; EW = 0.3150 N.

TWS = V = 44506LB = 7892 PSi; To = 0.454 = 0.4(50KSi) = 20KSI
8-42 FROM PRUB 5-54: VMAX=162.9 RN=162.9 X103 N
              MMAX = 228 KNIM x 103 N/RN x 103 Mm/m = 228 X106 NIMM
              REO'D. 5 = M/O3: 03 = 0.66(SV) = 0.66(345APa = 227.7 MPair A 992
               S_{min} = \frac{228 \times 10^{6} N \cdot mm}{227.7 N / mm^{2}} = 1.00 \times 10^{6} mm^{3} - W460 \times 60
S = 1.12 \times 10^{6} mm^{3}; DEPTH = 45 mm; tw = 8.00 mm
T = \frac{V}{th} = \frac{162.9 \times 10^{3} N}{8.00)(455) mm^{2}} = 44.75 mPa; to = 0.4(345) = 138 mPa OK
           FROM PROB. 5-511 VMAX = 804 LB; MMAX = 2528 LB-IN
            ASTMA53, GRIB: Sy =35KSi; OB=SY/3 = 35/3 = 11.67KS = 116678Si
             REQ'D S = M = Z528 LB.IN = 0.2171N3 - 1/4 SCMY 0 STEEL PIPE

S=0.23461N3, A=0.6691N2 PIPE 1/4 STD

\gamma = \frac{2V}{A} = \frac{2(80488)}{0.6691N^2} = \frac{240405}{240405}; LET T_3 = \frac{0.55}{N}; N = \frac{0.55}{T}

N = \frac{0.5(35000005)}{30405} = \frac{7.28}{2} \text{ ok}

            FROM PROB 5-9 : VMAX = 1557LE : MMAX = 6228 LB-11
             03 = Syly = 40000 PSily = 10000 PSi: To=0.53/4=5000 PSI
             SMIN = 10 6228 LO.IN = 0.623 IN 3: C SX2.2/2 ALUM. CHANNEL
             7= <u>V0 (1557)[[2)(26(1,52)(1.57/2)</u>
Le (0.98)(.52)
            T' = 1835 PSi SAPE
SHEAR: T= 31 = 7595; (RECT. SECTION)
           Reod A = 31 - 3(/20016) = 24/19? 4x88EAM
                                                                   1200 1
                                                                                    -3600 LB • FT
          BENDING: J= # = OF = 1150PS;
          REOD S = M - B60060FT)(N=1FF) = 37.61N3 4210 BEAM
8-46 FROM PROB 5-53: YMAX = 2950N: MMAX = 3350 Nom
           SHERR & AMH = 31 (3)(0.66 N/mm) = 6705 mm 2 2 x8/BEAN OR YM BENN
          BENOIG: 5 = M = 3350Nim x 108mm = 609 x 103 mm : USE 4 x 10 BEAM
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8-47 FROM PROB 8-28% IN=148.3 INF3 C=3.50/N 3 Q=28.33/N3. SEE ALSO P6-22.
           VMAX = P & MMAX = P(3FT) = 36(P)EON & TS = 80051 5 0mm = 14.00 PSI
          T = \frac{\sqrt{6}}{T^{2}} ? V_{mAx} = P_{mAx} = \frac{TIC}{6} = \frac{(80)(146.3)(3.0)}{28.33} = \frac{1256 LB}{1256 LB} = P_{mAx}
O = \frac{M^{2}}{T} = \frac{36PC}{T} : P = \frac{O3I}{36C} = \frac{(900)(146.3)}{(36)(3.50)} = \frac{1648 LB}{1256 LB}
8-48 FROM PROB P5-8 : VMAN = 21.36 DN = 21360N : I 229 x 12.44
           I9 x 8.361: t=0.27 M (254mm/m)=6.86 mm: h=9.00/N/25.4)=279 mm
           Two th = 2/360 N = 13.6 MPA
8-50 TOTAL LOAD = W = NL = BOLB/FF)(12 FF) = 960LB: VMAX = WZ = 480LB
          T = 3V = (3)( 480LB) = 66.2Psi : Ta = 70Psi OK
          CHECK BENDING: MMA = WL/B= (80 1/2) = 1440LO.PT (121N/A)=17 280 LB:IN

O= M = 17280 LB:IN = 1315 PSi: Of = 1000 PSi UNSAFE
8-51 FROM PROB P5-10 : VMAY=1500LB: MMAX=9000LB-1X
         (a) SHEAR: \gamma = \frac{3V}{2A} = \frac{31/500LC)}{(2.1/500/10)} = 1/25PSi
        (b) BENDING: 6-= M = 9000 LB-1A S = 6750 851
        (C) 73 = 0.5 Sy/3: REQD Sy = 3To/o.5 = 3(1125)/0.5 = 6750 151
             O3 = 54/3 : Rego Sy = 3 O3 = 3(6750) = 202008i ANY STEEL
8-52 FROM PROB P5-6 : VM = 1457N : MAR BIS NIM
         (a) SHEAR: r = \frac{3V}{2A} = \frac{3(145)(N)}{(2)(16)(60)mm} = -2261 mla
         (b) BENDING: ( = M = 318 Nom (03mm/m) = 33.1MPa
         (C) T_d = 0.55y/3 ? Read Sy = \frac{3(r)}{0.5} = \frac{3(2.261)}{0.5} = \frac{/3.6 MPa}{0.5}
             Od = 51/3: REOD Sy = 30 = 3(334) = 99.3 HPA OR SEIGHAL OTHERS
                                                                            6061-TY: Sy=148 MPa
8-53 FROM PROB. P5-47 : VMF 450 N & MMF 172.5 NVM
        O_{3} = Sv/N = 276NPa/4 = 69MPa = M/5:

REGOD S = \frac{M}{O_{2}} = \frac{172 SDO N mm}{69 N / mm^{2}} = 2500 mm^{3} = \frac{bh^{2}}{6}

REGOD h = \frac{165}{b} = \frac{16(2500) mm^{3}}{12 mm} = 35.4 mm
         T = \frac{3V}{2A} = \frac{3(450 \text{ N})}{(2)(12)(35,4) \text{ mm}^2} = 1.59 \text{ MBL} = 0.55 \text{ V}
         N = 0.5 SV = 0.5/276 MAN) = 86.7 SAFE. VERY HIGH N.
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$$\frac{8.54}{6.0} FROM PROS P5-48: V_{MAF} 1290 N: M_{AAF} 370.8 N·m$$
(a) $T = \frac{4V}{3A} = \frac{4(1290N)}{3(7)(40)^2/4} = \frac{-1.31}{1.31} \frac{MPa}{MPa} = T_0 = \frac{0.55y}{4} = \frac{5y}{8}$
(b) $T = \frac{M}{5} = \frac{376.8 \times 10^3 N \cdot mm}{17(40)^3/32} = \frac{59.0 MPa}{5} = \sigma_0 = \frac{5y}{4}$;
(C) FOR SHEAR: $PEOOSy = 8T = 8(1.37) = \frac{11.0 MPa}{5}$
FOR BENDING: $PEOOSy = 4T = 4(59.0) = \frac{236MPa}{236MPa} = \frac{A151/820 HR}{5} = \frac{331 MPa}{5}$

8-55 FROM PRIB P5-47:
$$M_{na}=172.5 \text{ N/m} ? N_{na}=450 \text{ N}$$

Re 60. $S = \frac{M}{C_{3}} = \frac{(172.5 \text{ N/m})(10^{3} \text{m/m}/\text{m})}{172.5 \text{ N/m}} = 1438 \text{ m/m}^{3} = 17(0)^{3}/32$

$$D = \left[\frac{32}{7}\right]^{1/3} = \left[\frac{32(1438)}{7}\right]^{1/3} = \frac{24.5 \text{ m/m}}{3.6} : A = 170^{3}/4 = 470 \text{ m/m}^{3}$$

$$T = \frac{4V}{3A} = \frac{4(1450 \text{ N/m})}{3(470 \text{ m/m})} = \frac{12800^{3}}{1120 \text{ m/m}}$$

$$\frac{8.56}{7} = 4V/3A : V_{AF} = \frac{3A7}{4} = \frac{3(\pi)(1.50)^{2}N^{2}(7068fN^{2})}{(4)(4)} = 92.8LB$$

$$\frac{8.57}{7} = \frac{0.554}{6} = \frac{0.5(4800)}{6} = 4000 PS : \approx \frac{2V}{A}$$

$$\frac{7}{6} = \frac{5V/6}{6} = 49.000 /6 = 8000 PS : \approx \frac{7}{4}$$

$$\frac{7}{6} = \frac{3600L8.1N}{6} = \frac{3600L8.1N}{6} = 0.45 IN^{3}$$

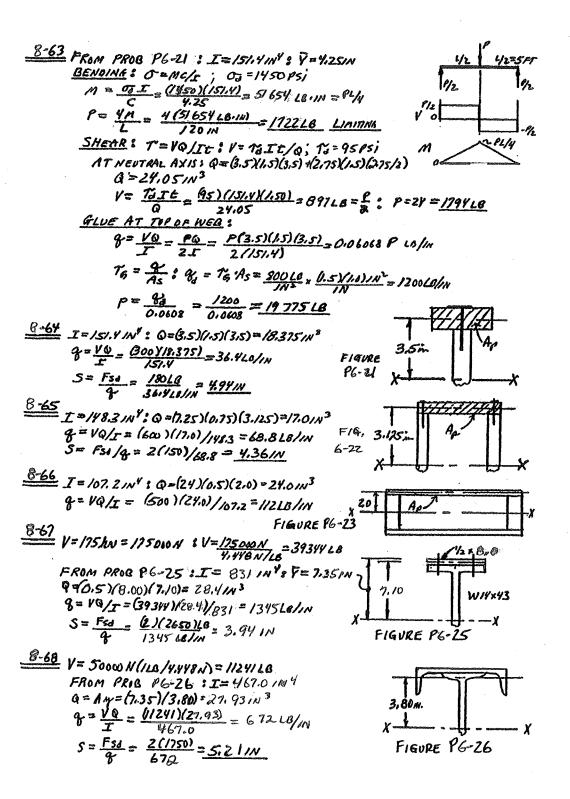
$$A = 1.075IN^{2}$$

$$Y = \frac{2V/A}{6} = \frac{2(200)/.075}{6} = \frac{372.65}{6} = 0.6$$

WY.	
(a) 1.50 1050 0.0875 1495	5668 UK
(b) 3.00 2100 0.175 14 .669	4/85 OK
(c) 4.50 3150 0.263 1/2 .799	3504 OK
(d) 6.00 4200 0,350 2 1.075	2605 OK

$$\frac{8-59}{SHEAR} = \frac{1000 \text{ AT } Joint = 9 = \sqrt{9} / I}{FROM FIG P G-14!} = \frac{0.3672 / NY}{I = 0.3672 / NY} = \frac{0.533 / N}{I} = \frac{0.533 /$$

8-61 FROM PROB PG-33 : I=46.0 IN4 03 = 54/4 = 2/00/4 = 525085i Y = 2.772 1, = 0.5 SY/4 = 2625 851 BENDING: 0 = MC/E $M_{ALLOW} = \frac{O_0 I - (5250)(46.8)}{C} = 90330 L_8-INT$ $W = \frac{8M}{L^2} = \frac{8(90330 L_8 IN)}{(720 IN)^2} = 50.28 IN$ NL/2 WL/2. SHEAR AT NEUTRAL AXIS : Q=(0,5 X/2)(2.03-0.25) + 2(1,53)(0.25)(.53/2) 0= 11.27 IN3: t= 2(0.25) =0,50.N T = VQ : V = TaIt (2625 Y 46, 8(0,50) M $M = \frac{Z(V)}{L} = \frac{Z(5V50LB)}{120/N} = \frac{90.8LB/N}{1}$ SHEAR FLOW AT WELDS: 9 = VQ: V=QI = 1800)(46.8) =7888 LB M= 2V/L= 2(7888)/120 = 131 LB//N RIVETS : S=SPACING = 4.0 IN & FSU = 2(600)=1200 LB = 593 Pd = Fsd = 1200 LB = 300 LB/IN 9 = VO : V = 8I (300 LB//N (46.87N4) = 2/64 LB W = 2V/L = 2(264/101/12011 = 36.4 10/11 (1211/FF) = 433 18/FT 8-62 FROM PROB P6-24 : I = 816.314 : 7=7.151 #350UDIBEN PANE 01 = 650 PSi BENDING: 0 = MC/I $M = \frac{OaI}{C} = \frac{(650)(8/6.2)}{7.75} = 6846966.1N = Mc^2/8$ 13= 70 PSi $M = \frac{8M}{L^2} = \frac{8(68464)}{(120)^2} = 38.0 LB/N$ SHEAR AT NEUTRAL AXIS: Q = A x = (3.0)(7.75)/775/2) = 90.09/113 $T = \frac{VQ}{It}$: $V = \frac{TdIt}{Q} = \frac{(70 \times 8)(6.3)(3.0)}{96.09} = \frac{1903 LB}{ML/2}$ $w = \frac{2V}{L} = \frac{2(1903)}{120} = \frac{31.7101}{120}$ NAILS: 5 = 6,0 m: Fsd = 2 (160) = 320 LB = 59: 90 = 5 = 320 LB = 53.3 LB/M $Q_0 = \frac{VO}{I}$: $V = \frac{Q_0I}{Q} = \frac{(53.3)(8/6.3)}{(1.5)(1/2.5)(1/2.75-7.75-0.75)} = 607 LB$ W= 2V = 2(607) = 10./LO/IN (12/N/FT) = 121 LO/FT LIMITING



- $\frac{8-69}{T^{2}} W18 \times 55: \ t = 0.390 \text{ in , } h = 18.1 \text{ in . As TM A992, } 5y = 50 000 \text{ psi}$ $T^{2} \frac{V}{th} = \frac{36606 \text{ M}}{(0.39 \times 18.10) \text{ in}^{2}} = \frac{5185 \text{ psi}}{50000 \text{ psi}} \frac{\text{SAFE}}{\text{OX}}$ $T_{3} = 0.40 \text{ Sy} = 0.40 (50000095i) = 20000 \text{ psi} \text{ OX}$
- 8-70 WIB * 40 ! t = 0.315in, h = 17.90 in . ASTMA 992, Sy=50000 PSi $T = \frac{V}{th} = \frac{36600 \text{M}}{(0.315)(17.91)} = \frac{6491 \text{ PSi}}{54\text{FE}} = \frac{54\text{FE}}{56000}$ $T_{j} = 0.405y = 0.40(50000 \text{ PSi}) = 20000 \text{ PSi} \text{ OK}$
- 8-71 W14 × 26: t = 0.255in, h = /3.90in. ASTMA992, 5y = 50600 PS; $\gamma = \frac{V}{th} = \frac{1000016}{6.255)(13.90)in^2} = \frac{2821}{5000} \frac{1000}{500} \frac{5000}{500}$ $T_d = 20000$ (PROB 9-70)
- $\frac{8-12}{T^2} = \frac{6I \times 4.692 \text{ ALUMINUM: } t = 0.21 \text{ in } k = 6.00 \text{ in}}{(0.21)(6.00)} = \frac{793785i'}{5AFE} = \frac{59}{2N} = \frac{59}{2N} = \frac{59}{2N} = \frac{59}{2N} = 0.255y}$ $T_d = 6.25)(40000PSi) = 10000PSi' \text{ ok.}$
- 8-13 W10 + 12; t= 0.190 IN h=9.87; N, ASTM A992, Ta=20000PSi T= V = 6150 LB = 3599 PSi SAFE (PROB 8-69)
- $\frac{8-79}{Q = A_1 N_1 + A_2 N_2 = 2(2.767)(0.233)(1.389) + (2.080.233)(2.889)}{Q = 1.798 + 1.349 = 3.192 IN^3}$ $V = \frac{VQ}{It} = \frac{(6750 \text{ ll.})(3.192 \text{ IN}^3)}{(13.11N^4)(0.966 \text{ IN})} = \frac{3494 \text{ ps.}}{3494 \text{ ps.}} \frac{SAFE}{Sy = 46000 \text{ ps.}}$ $T_3 = \frac{5y}{2N} = \frac{46000085}{7(22)} = 11500 \text{ ps.}; \text{ OK}$ Sy = 46000 ps.
- B-75 2×8 WOOD BEAM: A=10.87/N2. NOZ SOUTH.PINE, Ta=70.085; $T = \frac{3V}{2A} = \frac{3(480 \text{ M})}{2(10.87/N^2)} = 66.2 \text{ PS}i \quad SAPE$
- $\frac{8-16}{T^{2}} \frac{F(G, P8-29)}{F(G, P8-29)} = \frac{(7504)(28.591N^{3})}{(28.591N^{3})} = \frac{66.795}{66.795} \frac{SAFE}{SAFE}$ No. 2 DOUGARS GR, To = 9595i OR

HSS 8x2 x /4: I= 28.51N4, t= 0.2331N - DESIGN VALUE 8-77 Q = A1 M31 + A2 M2 = 2 (0.233)(3.767)(1.894) + (2.0)(0.233)(3.884) Q= 3.307 + 1.810 = 5.117 IN3 7 = VQ = (120004)(5.117 = 4623 PSi SAFE ASTM ASOD, GRIB TJ= 54/2N = 46000PSi/2(2) = 11800 PSi OK 5x=46000PSi 8-18 FROM PROBLEM 6-42, I= 60,58, NY, t=0.280 (WYX/3) Q= AIMI + AZM2 +A3M3 1 ,486 8:16 4.16 -Y 1.908 2.673 - W4x13 2 1.401 4×2×14 3 2,440 3.080 7.515 D= 10,610 IN3 7= VQ = (800 M) (10.61-113) = 1826 PSi SAFE AT AXIS X-X TI = 5 1/2N = 50 000 PSi/2(2) = 12 500 PSI FOR ASTM A992 - W4 X/3 8-79 C10 x 6.136 ALUMINUM CHANNEL IV = 6,33 IN, t= 0.4/IN Q FOR LOWER PART OF FLANGES Q=AM= Z(0.41)(Z.48)(Z.48/E)=Z.522IN3 $T = \frac{VQ}{It} = \frac{(430.11)(2.5221N^3)}{(6.331N^4)(2.50.411N)} = \frac{209 PSi}{SAFE} \qquad 6061-76 ALVM.$ TI= SY/2N = 40000/2(2) = 10000PS/ OK DATA OF PROB. 8-78. SHEAR FLOW 9 = VQ 8-80 I= 60.55/N4, V= 1800ll-Q = ANY FOR ONE YALX'Y TUBE $Q = (2.44/N^2)(3.08)iN = 7.515/N^3$ $Q = \frac{VQ}{I} = \frac{(1800 \text{ M})(7.515/N^3)}{60.55.1N^4} = 223 \text{ M/in}$ FIG. P8-29: I = 107,2 INY 4.50 x 1.75 Q=AY FOR TOP PANEL Q= (0.50)(24) (2,00)=24.0 1N3 q = \frac{VQ}{I} = \frac{(500 \, U)(24.0 \, IN^3)}{107, 2 \, IN\frac{4}{3}} = 1/2 \, U/IN 2414 FSJ = 135 St./NAIL X2 NAILS = 270 H MAX, SPACING-SMAFFSd/q = 270 ll/12 ll/IN = 2.41 IN MAXIMUM SPECIFY S= 2.25 IN

CHAPTER 9 Deflection of Beams

$$A23-(6): M = -\frac{9.12}{49851} = \frac{(3000)(200)^3}{(300720)(3617720)} = \frac{20.0/mm}{2.0/mm}$$

$$E = 207 \times 10^{\frac{1}{10}} \times \frac{10^{\frac{1}{10}}}{(100mm)} = 207 \times 10^{\frac{3}{10}} N/mm^2$$

$$I = \frac{170^7}{6V} = \frac{17(32.0mm)^4}{6V} = 5/472 \times 10^{\frac{3}{100}} N/mm^2$$

$$M = -\frac{2.0}{19261} = \frac{6}{19261} = \frac{5/400}{192(20720)(5.14720)} = -0.503 mm$$

$$M = \frac{-91^3}{19261} = \frac{-3000(30)^3}{192(20720)(5.14720)} = -0.252 mm$$

$$M = \frac{-91^3}{19261} = \frac{-3000(30)^3}{48(20720)(5.14720)} = -0.252 mm$$

$$M = \frac{-91^3}{19261} = \frac{-3000(30)^3}{48(20720)(5.14720)(5.14720)(700)} = -0.252 mm$$

$$M = \frac{-3000(700)^3}{48(20720)(19175)} = \frac{-5400}{3621} = \frac{-3000(75)^2(525)^2}{3(20720)(700)}$$

$$M = \frac{-3000(700)^3}{48(20720)(19175)} = \frac{-3000(75)^2(525)^2}{3(20720)(5.14720)(700)} = -\frac{1/3}{1000} mm$$

$$M = \frac{-9100}{6(20720)(75)(350)} = \frac{-1/3}{6(20720)(700)} mm$$

$$M = \frac{-1/38}{620} mm$$

$$M = -\frac{1}{1000} \frac{1}{1000} = \frac{-1/38}{6200} mm$$

$$M = -\frac{1}{1000} \frac{1}{1000} = \frac{-1/38}{62000} mm$$

$$M = -\frac{1}{1000} \frac{1}{1000} = \frac{-1/38}{1000} = \frac{-1/38}{1000} =$$

```
AZ3-(0): I = 0.3/0 in
                          M = \frac{P L^3}{486T} = \frac{-650(38)^3}{49/342/06)(03/0)} = \frac{-0.032 \text{ m}}{-0.032 \text{ m}}
   9-9
                    A23-6): I=59.69in4; E=10x106 poi
W=11125 D1/fix(10ft)=11250 il
                             l = 10 ft x 12 in/ft = 120 in
                      \gamma = \frac{svl^3}{384 \, \text{EI}} = \frac{-s(11250)(120)^3}{324 (102106)(29.10)} = \frac{-0.424 \, \text{in}}{324 (102106)(29.10)}
 9-10
                     A23.6): X= 3.5FT (12 in JFT) = 42 IN.
                                     W = (1/25 LB/FT) ( /FT/1210) = 93.75 LB/IN
                      N_{y} = \frac{-w\chi}{24E\Gamma} \left( L^{3} - 2L\chi^{2} + \chi^{3} \right) = \frac{-(33.75)(42)}{24(100)(92)(59.65)} \left( (20^{3} - 2(120)(42) + 42^{3} \right)
                      N = - 0.379 IN
                  LOADING IN FIGURE P5-12.
I=238 in : A23-(g) ; a=48 in ; l=120 in; P=15000 M
                    \eta = \frac{-Pa^{2}}{3(2010^{4})(238)} (48+120) = -0.271 \text{ in}
\frac{972}{\gamma} = \frac{A23-(9)}{3EI} = \frac{241}{3} = \frac{15000(24)^2}{3(3010)(238)} = \frac{-0.0678111}{3(3010)(238)}
                   + max at x = 0.511 (1)= 0.517 (20) = 69.2 m FREA A
             N_{f} = \frac{.06415 \text{ Pal}^{2}}{ET} = \frac{(.06415) (.5000)(48) (.20)^{2}}{(.3480)(.238)} = \frac{0.093 \text{ in (UPWARD)}}{(.0000)(.238)}
 \frac{9-14}{4} \quad A24-(a) : N=\frac{P0^3}{367} = \frac{-120(8)^3}{3(9\times 10^6)(0.08734)} = 0.0078 \text{ in}.
 \frac{9-15}{7} = \frac{A23-(A)}{48ET} : REQ'D I = \frac{-PL^3}{48ET} = \frac{-3008(700)^3}{48ET} = 8.63 \times 10^{5} \text{mm}^4
               I = 1704 .: 0 = [64 I/7] 4 = [64(8,63×105)/7] 1/4 = 64.8 mm
 9-16

T = (500)(350mm)(32.4mm) = 19.7 mBa 30KN 30KN
                REQ'D Si = 8 (19.7MPa) = 158 MPa (ANY STEEL)
\frac{9-17}{\gamma_{MAX}} = \frac{-PL^{3}}{3EL} : REO'O L = \frac{-PL^{3}}{3E\gamma} = \frac{-0.52(1.20)^{3}}{3(300.00)(0.15)} = 6.6552.00 \frac{8.47}{12}
I = \frac{bk^{2}}{12} : t = \left[\frac{bL}{b}\right]^{1/3} = \left[\frac{12(6.656 \times 10^{3})}{0.100}\right]^{1/3} = 0.030 \frac{1}{b}
-0.100 \frac{1}{b}
```

Statically Indeterminate Beams

9-19

FOR ASTM A992 SY=345 MPW: 0= 0.66 SY=227 MPW OK

AT LOAD, NB = -13 939/EI = 5.25 mm

CASE A-25 (b);
$$P = 35RN$$
, $L = 4.0$, $\alpha = 2.50m$
 $b = L - \alpha = 4.0 - 2.5 = 1.5 m$
 $R_A = \frac{Pb}{2L^3} \left(\frac{3}{2} L^2 - b^2 \right) = \frac{35kN(1.6)}{2(4)^3} \left(\frac{3(4)^2 - 6.5}{2} \right)^2 \right) = \frac{18.76 kN}{28.76 kN} = V_{AB}$
 $R_C = \frac{Po^2}{2L^2} \left(\frac{b}{2} + 2L \right) = \frac{35kN(2.5)^2}{2(4)^3} \left[\frac{1.5}{2} + 2(4) \right] = \frac{16.24 kN}{24 kN} = V_{BC}$
 $M_A = \frac{-Pob}{2L^2} \left(\frac{b}{2} + L \right) = \frac{-35(25)(1.5)}{2(4)^2} \left(\frac{1.5}{2} + \frac{2(4)}{2} \right) = \frac{-22.56 kN \cdot m}{2(4)^3}$
 $M_B = \frac{Po^2b}{2L^3} \left(\frac{b}{2} + 2L \right) = \frac{35(2.5)^2(1.5)}{2(4)^3} \left(\frac{1.5}{2} + \frac{2(4)}{2} \right) = \frac{24.35 kN \cdot m}{24.35 kN \cdot m}$

DEPLETION

FROM A TO B:
$$l=35008N$$
; DISTANCES IN M.

$$M_{AB} = \frac{-0x^{2}b}{12EIL^{3}} (3C_{1}-C_{2}x)$$

$$C_{1} = aL(L+b) = 2.5(4)[4+1.5] = 55$$

$$C_{2} = (L+a)(L+b) + aL = (6.5)(5.5) + 10 = 45.15$$

$$M_{AB} = \frac{(-25080)(x^{3})(1.5)(3(55) - 45.75x)}{12EI(4)^{3}}$$

$$= \frac{-68.36x^{2}[165 - 45.75x]}{EI}$$

$$\frac{3120}{12} \frac{4x^{3}}{12} (1220)x^{2}$$

$$M_{AB} = \frac{3/27.4 \chi^3 - 1/279 \chi^2}{EI}$$

USING A GRAPHING CALCULATOR FUNCTION IS A MINIMUM AT X=2.404 m FROM A. THEN MAY 15:

$$N_{\text{max}} = \frac{-2.1734}{EI}$$
At $X = 2.5$, $N_{\text{B}} = \frac{-2.1628}{EI}$

SPECIFY W200 x15 ASIN PROB 9-19, 9-20 LIGHTEST OR W8 X10

I = 1.28 × 107 mm4

$$\frac{N_{mAX}}{N_{mAX}} = \frac{-2/734 \text{ N/m}^{3}}{(207 \times 10^{7} \text{ N/m}^{2})(1,28 \times 10^{7} \text{ m/m}^{4})} \times \frac{10^{15} \text{ m/m}}{M_{s}} = \frac{8.19 \text{ m/m}}{ET}$$

$$N_{B} = \frac{-21620}{ET} = -8.15 \text{ m/m}$$

$$\frac{STRESS!}{O = \frac{M}{S} = \frac{24.35 \text{ kN.m}}{1.28 \times 10^3 \text{ mm}^3} \times \frac{10^3 \text{ N}}{10^3 \text{ kn}} \times \frac{10^3 \text{ mm}}{10^3 \text{ mm}} = \frac{190 \text{ MPa}}{190 \text{ MPa}}$$

$$ASTM A 992 Sy = 50 \text{ Ks}; = 345 \text{ MPa} \qquad \frac{(0 \text{ K} \cdot 50 \text{ CS})}{9 - 20}$$

$$O_0 = 227 \text{ MPa}$$

CASE A-25 (C): w = 400 \$/ \$t, L = 14.0 ft W=WL= (10011/pr)(14.0 ft)=560011 RA= 5/8 W= 3500 1 = VA; R8= 3/8 W = 2100 # = VE MA = -0.125 WL = -0.125 (5600) (14.0) = -9800 Meft ME = 0.0703 WL = 0.0703(5600)(14.0) = 5512 W. ft POINT E IS SEL FROM A (FIXED END) 14.0pt XE = 5/8(14.0ft) = B.75ft DEFLECTION: 3500 ATC AT X= 0.579L=0.579(14.0)=8.11ft Mc = MMAX = -WL3 = 5600UX14 ft) (ii) o $N_{\text{MAX}} = \frac{-83.061 \text{ Lb ft}^3}{\text{EI}}$ $LET M_{\text{MAX}} \leq L/360 = \frac{14.0 \text{ ft} (2M/4t)}{360} = 0.467 \text{ m} \text{ (lb ft)}$ $REQD. I = \frac{-83.06 \text{ lb ft}^3}{(3000^4 \text{ lb/m}^3)(-0.467 \text{ m})} \times \frac{(2 \text{ m})^2}{167^3} = 10.25 \text{ ln}^4$ W 8 XN STEEL BEAM IS LIGHTEST, I = 30.8 IN , 5 = 7.81 IN 3
ACTUAL NY MAX = -83061 M-At 3
(30 X/0 (M/N)(30.8 IN)) (211) = 0.155 IN. $\sigma = \frac{M}{5} = \frac{9800 \text{ M} \cdot \text{Jt}}{7.81 \text{ m}^2} \times \frac{R \text{ m}}{\text{Jt}} = 15058 \text{ psi}$ CAN USE ASTA A992; 05 = 0.66(50ksi)= 33.0KSi-OK

9-23

CASE A-25(C): N= 50 H/IN 3 L=16.0IN W=NC = (50 H/N)(16.0 IN)= 800 H-RA=5/8 W= 500 H; RB=3/8 W=300 H-MA=-0.125 NL=-0.125(800)(16)=-1600 Him NE=0.0703WL=0.0703(800)(16)= 900 Him XE=5/8 L=5/8(16)=10.0 IN DEFLECTION;

SKETCH SIMILAR TO 9-72.

ATC = 0.519 L = 0.519 (16) = 9.264 M $M_{C} = M_{\text{MAX}} = \frac{-WL^{3}}{185EI} = \frac{-800(16)^{3}}{185EI} = \frac{177/2}{EI}$

DESIGN COVLO RESULT IN MULTIPLE SOLUTIONS.

9-24 CASEA-25(d);
$$P=350M$$
, $L=10.8M$, $\Delta=2.50M$.

$$\frac{R_A = \frac{-3Pa}{2L} = \frac{-3(350)(2.50)}{2(10.8)} = \frac{121.5M}{2(10.8)} DOWN$$

$$R_B = P\left(1 + \frac{3\alpha}{2L}\right) = 350M\left[1 + \frac{3(2.50)}{2(10.8)}\right] = \frac{471.5M}{2(10.8)} UP$$

$$\frac{M_A = P\alpha/2 = (550)(2.50)/2 = \frac{437.5M}{2(10.8)} = \frac{10.8}{250}$$

$$\frac{M_B = -P\alpha = -350(2.5) = 875M \cdot \hat{m}}{P(2.50)}$$

$$\frac{M_B = -P\alpha}{EI} \left[\frac{\alpha^2}{4U^2} + \frac{\alpha^3}{3L^3}\right]$$

$$= \frac{-350(10.8)^3}{EI} \left[\frac{2.5^2}{4(10.8)^3} + \frac{2.5^3}{2(10.8)^3}\right]$$

$$M_C = \frac{7129}{EI} M \cdot \hat{m}^3$$

$$M_C = \frac{7129}{57} M \cdot \hat{m}^3$$

$$M_C = \frac{7129}{57} M \cdot \hat{m}^3$$

$$\frac{9-25}{R_{A}=R_{C}=\frac{9}{2}=\frac{35}{2}=17.5\text{kN}}$$

$$R_{A}=R_{C}=\frac{9}{2}=\frac{35}{2}=17.5\text{kN}$$

$$M_{A}=M_{B}=M_{C}=\frac{PL}{8}=\frac{(85000\text{N})(4.0\text{m})}{8}=17500\text{ N·m}$$

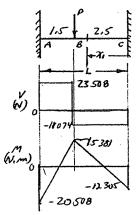
$$M_{B}=M_{MAX}=\frac{-PL^{3}}{192\text{EI}}=\frac{-35000(4.0)^{3}}{192\text{EI}}=(\text{ku}) \circ \frac{17.5}{17.5}$$

$$M_{B}=\frac{11667\text{ N·m}^{3}}{EI}$$

$$M_{B}=\frac{11667\text{ N·m}^{3}}{EI}$$

9-26 CASEA-25(4): P=35RN, L=4.0 m, a=1,50m, b=4.0-a=2,5m
THIS LOADING IS THE MIRROR IMAGE OF THAT IN 9-27
NOTATION OF CASE A-25(4) REQUIRES a 76. THEN

CALCULATIONS ARE THE SAME. $R_A = 23926 N$, $R_C = 11074 N$ $M_A = -20508N \cdot m$ $M_B = 15381 N \cdot m$ $M_C = -12305 N \cdot m$ $M_{MX} = M_D = \frac{-10127 N \cdot m^3}{EI}$ $X_1 = 2.222 m$ FROM C TO D



$$\frac{9-27}{RA} = \frac{Pb^{2}}{L^{3}} (3a+b) = \frac{35800 (15)^{2}}{(40)^{3}} (3(2.5)+1.5) = 11074N$$

$$\frac{Rc}{Rc} = \frac{Pa^{3}}{L^{3}} (3b+a) = \frac{35000 (2.5)^{2}}{(4.0)^{3}} (3(1.5)+2.5) = 2392bN$$

$$\frac{MA}{Rc} = \frac{Pab^{2}}{L^{2}} = \frac{-35000 (2.5) (1.5)^{2}}{(4.0)^{2}} = -12305N \cdot m$$

$$\frac{MB}{L^{2}} = \frac{2Pa^{3}b^{2}}{L^{3}} = \frac{2(35000)(2.5)^{2} (1.5)^{2}}{(4.0)^{3}} = 15381N \cdot m$$

$$\frac{Mc}{L^{2}} = \frac{Pa^{3}b}{L^{2}} = \frac{-35000 (2.5)^{2} (1.5)^{2}}{(4.0)^{3}} = 15381N \cdot m$$

$$\frac{Mc}{L^{2}} = \frac{Pa^{3}b}{L^{2}} = \frac{-35000 (2.5)^{2} (1.5)}{(4.0)^{2}} = -20508N \cdot m$$

$$\frac{DEFLIELTION}{3EI (3a+b)^{2}}$$

$$\frac{Mmx}{3EI (3(2.5) + 1.5)^{2}} = \frac{-10127 N \cdot m}{3}$$

$$\frac{7}{3EI (3(2.5) + 1.5)^{2}} = \frac{-2022m}{3a+b} = 2.222m FROM A TO D.$$

9-28 CASE A-25(g):
$$w = 400 \text{ ll/ft}$$
; $L = 14.0 \text{ ft}$
 $W = w - L = 400 \text{ ll/ft}$)(14.0 ft)= 5600 ll

 $R_A = R_C = w/_2 = 2800 \text{ ll}$
 $M_A = M_C = -w/_{12} = -5600 (14)/_2 = 6533 \text{ ll/ft}$ (u) 0

 $M_B = w/_2 y = 3267 \text{ ll/ft}$
 $DEFLECTION$:

 $M_B = N_{MAX} = \frac{-wL^3}{384EI} = \frac{-5600 (14)^3}{894EI} = \frac{-40017 \text{ ll/ft}}{EI}$
 $-6533 = 267$

9-29. CASE A-25(g):
$$W = 50 M/m_1 L = 16.0 M$$
,

 $W = WL = (50 M/n)(16 M) = 800 M$
 $RA = R_c = W/2 = 400 M = VA = Vc$
 $M_A = M_c = -W/2 = -800(16)/12 = -1067 M$
 $M = WL/24 = 523 M$
 $DEFLECTION$:

 $N_B = N_{MAX} = \frac{-WL^3}{384EI} = \frac{-900(16)^3}{844EI} = \frac{-8533 M}{EI}$

CASE A-25 (h): w= 400 l/pt L= 7.0 fx W=W-L=400M/f+)(7ft) = 2800M ON 15 PAN. RA=Rc= 3W/8= 3(2000)/8=105011=VA=VC Ro = 1.25W = 1.25(2800) = 3500 ll (W) 0 VB= 5W/8= 5(2800)/8=1750 A MB=ME=0.0703WL = 0.0703 (2800)(7) =1378.16.ft MB = -0.125 WL = -0.125 (2800) (7)= -2450 M-++ DEFLECTION: MAX AT XI= QYZISL FROM A ORC. X,=0.4215(70 At)=2.9505ft 3L = 2.625 fr 18/MAX = -WLY + (400)(7) -- 519/11.63

CASE A-25 (A): W= 50 11/M, L=8.8 IN W=WL=(5011/10)(81A)=400 NONEACH SOAN SKETCH SIMILAR 10 9-30 RA=3W/B=3(400)/B=15016=Rc=VA=VC RB = 1.25W= 1.25(400) = 500 ll V8 = 5W/8 = 5(400)/8 = 250 lb M, = Me = 0.0703 WL=0.0703(400)(A)=22516.1N MB = -0.125 WL = -0.125 (400)(B) = -400 Nm DEFLECTION MAX AT XI= 0.4215L FROM A OR C. X,=0.4215(8,010)=3,3721N $N_{\text{max}} = \frac{-wL^4}{185EI} = \frac{-50(8)^4}{185EI} = \frac{-1/01}{EI}$

9-32

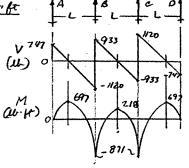
CASE A-28(i): W= 400 U/H 3 L= 56M, W=NL=1867U-RA= RO = 0.4W = 0.4 (186711) = 746.7 11 =VA=VO Re= Rc = 1.10 W= NO(1867) = 2053 ll-

ME= MF = 0.08 WL = 0.08(1867)(4.67)+)=69711-ft

M&= Mc = - 0.10 WL = - 87116. FT

MG=0.025 WL=0.025(1867)(4.67 pt) = 2/8 ll. ft

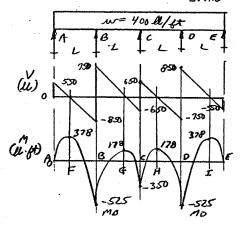
DEFLECTION FORMULAS NOT AVAILABLE



CASE A-28(L): W = 50 M/M, L = 5,333 M, W = ML = 266.7 M $R_A = R_D = 0.4 W = 106.7 M$ $R_B = R_C = 1.10 W = 293.3 M$ $M_E = M_E = 0.08 W L = 0.08 (266.7)(5.333) = 113.8 M - 1N$ $M_B = M_C = -0.10 W L = -0.10(264.7)(5.333) = -142.2 M \cdot 1N$ $M_A = 0.025 W L = 0.025(2.66.7)(5.333) = 35.6 M \cdot 1N$

9-34

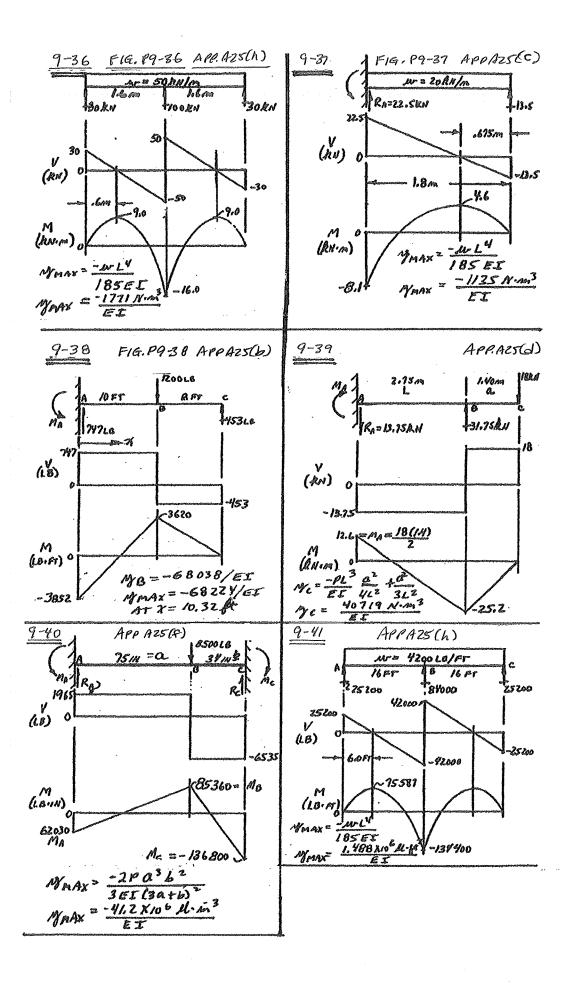
CASE A-25(j): W=400 M/gr, L=3.5ft, W=WL=1400H EACH SPAN

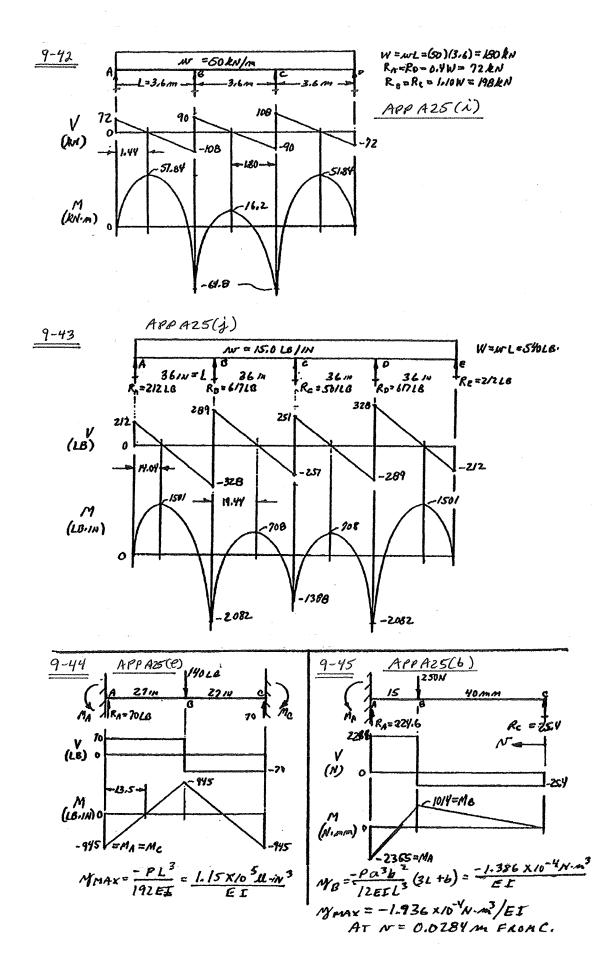


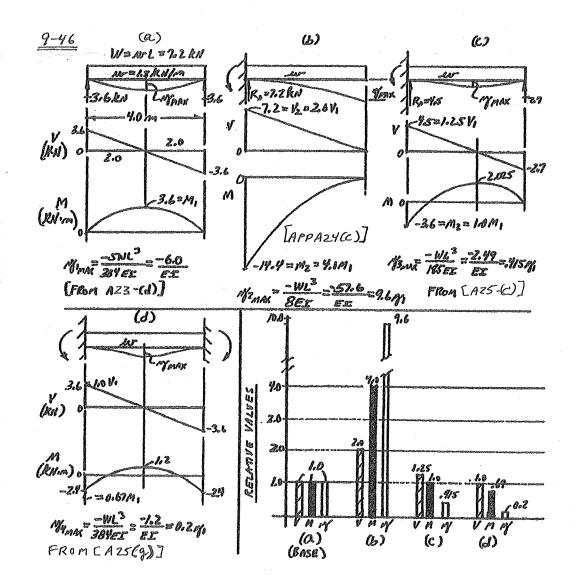
9-35

CASE A25(j): W= 50 W/IN, L = 4.0 IN W= WL = Zooll

$$V_A = R_A = 78.6 \text{ M}.$$
 $-V_B = R_A - W = -121.4 \text{ M}.$
 $+V_B = -121.4 + 228.6 = 107.2 \text{ M}.$
 $-V_c = 107.2 - W = -92.8 \text{ M}.$
 $+V_c = -92.8 + 185.6 = 92.8 \text{ M}.$
 $-V_p = 92.8 - W = -107.2 \text{ M}.$
 $+V_0 = -107.2 + 228.6 = 121.4 \text{ M}.$
 $V_C = 121.4 - W = -78.6 \text{ M}.$







The objective is to compare the results of the beam loading and support conditions for five different beams in **problems 9-22, 9-28, 9-30, 9-32, and 9-34.** Details were reported earlier in this solutions manual for each problem. Note that each beam design has a total length of 14.0 ft and carries a uniformly distributed load of 400 lb/ft resulting in a total load of 5600 lb. Changing the manner of support or adding additional supports affects the shearing force, V, the bending moment, M, and the maximum deflection, y, for a given EI value for the beam material and shape. Vertical shear stress and bending stress are directly propostional to the values of V and M respectively. Therefore, a reduction in either value will result in a reduction in stress or will allow the use of a smaller or lighter section for the beam. Comparisons are shown as ratios of V, M, and y/EI to those values for the first design, a supported cantilever. The other designs are a fixed-end beam and continuous beams on 3, 4, and 5 supports.

Prob.	V _{max}	V/V1	Mmax	M/M ₁	<i>Ymax</i>	y/y1
9-22	3500 lb	1.00	9800 lb in	1.00	-83061/EI	1.00
9-28	2800 lb	0.80	6533 lb in	0.667	-40017/EI	0.482
9-30	1750 lb	0.50	2450 lb in	0.250	-5191/EI	0.0625
9-32	1120 lb	0.32	871 lb in	0.089	N/A	•
9-34	850 lb	0.24	525 lb in	0.054	N/A	•

Note that maximum shearing force, bending moment, and deflection all decrease for successive designs. Deflection formulas are not available (N/A) in this book for the last two designs. But it stands to reason that deflection would be reduced by adding additional supports and reducing the span between adjacent supports. The comparison illustrates the advantages of using fixed ends for beams and of using more supports for a given load, thus reducing the effective span between adjacent supports. Fabrication problems and costs must also be considered when selecting a method of supporting a load on a beam.

9-48

This problem has the same objective as 9-47. Refer to that problem for a discussion of the objectives and the results. Data listed here are for different beam loadings (w = 50 lb/in; total beam length = 16.0 in) but the support conditions are the same as in 9-47.

Probler	n V _{max}	V/V1	Mmax	M/M1	ymax	y/y1
9-23 9-29 9-31 9-33 9-35	500 lb 400 lb 250 lb 160 lb 121 lb	1.00 0.80 0.50 0.32 0.24	1600 lb in 1067 lb in 400 lb in 142 lb in 86 lb in	1.00 0.667 0.250 0.089 0.054	-17712/EI -8533/EI -1107/EI N/A N/A	1.00 0.482 0.0625
	APP. A23 (M= 120 L0 140 2.1 FT	IFT	9-50 APP. APP. APP. APP. APP. APP. APP. APP	20 LB/FT 12 FT	8FT T	APP. A 25 (1) P=120 LB/FT B PT B PT 1052 1062 354
(is) of	800		540 900	80	-5%	-576 -450 -384
(LB·FT)			olus	2160	o or	763 -768

COMPARISON OF 9-49, 9-50, 9-51

W= 12018 | FT = 1018/14: La= 24 FT + 121N = 288 IN

DEFLECTIONS : [9-49] MMAX = 5 Nr L4 = 5 (10) (288) = -896 X10 = 70

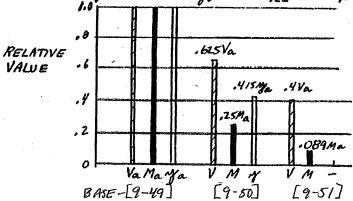
[9-50] Nyman = -wl = -(10)(288) -372×10 = 76 = 0.415 Ma IF EE IS
[9-50] Nyman = -wl = -(10)(288) -372×10 = 76 = 0.415 Ma IF EE IS

[9-51] DEFLECTION EQUATION NOT AVAILABLE; LESS THANNY

SUMMARY !

SHEARING FORCE: Vamax = 1440LB: Vine = 900LB = 0.625 Va: Vc=576LB = 0.4 Va MOMENT: Ma= 8640LB.FT; Mg=2/60LB.FT=0.25 Ma: Mc=168LB.FT=0.089 Ma

DEFLECTION: ME = 896XIN/EI & MY = 372XIO/EI = 0.4/5MA IF EI IS EQUAL.



BEAM SIZE: FOR NO. Z SOUTHERN PINE & 76=7085; 03=1000 esi

FORA RECTANGLE : TMAX = 3V/2A 3 5 = th 3/6

$$M_{MAX} = (8640L8 \cdot F7) \times I_{MM} / F_{T}) = 103680 L8 \cdot IN : \sigma = \frac{M}{3}$$

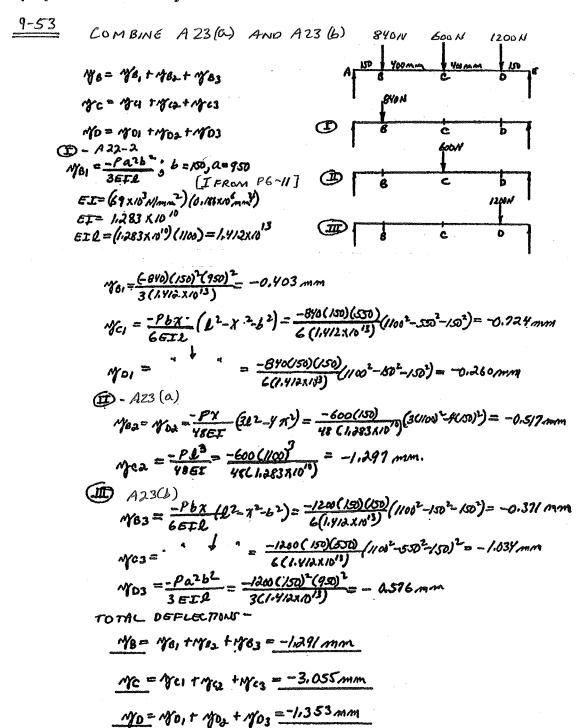
$$S_{MIN} = \frac{M}{03} = \frac{103680 L8 \cdot IN}{1000L0 I / IN^{2}} = 103.7 \cdot IN^{3} = \frac{6112 \text{ BeAM REOD}}{I = 697 \text{ IN}^{3}, 5 = 121/N^{3}, A = 63.3/N^{2}}$$

$$V_{A} = \frac{6000 L0 I / IN^{2}}{I = 697 \text{ IN}^{3}, 5 = 121/N^{3}, A = 63.3/N^{2}}$$

[9-50] VMAX = 900 LB: A = 3(900) = 19.3/H2

[9-51] VMAX = 576 LB: Amin = 3 (576) = 12.34 M2

Superposition - Statically Determinate Beams



 $E = 73 Gpa = 23 \times 10^{9} N/m^{2} = 73 \times 10^{9} N/mm^{2}$ $EI = (13 \times 10^{3})(16956) = 1.238 \times 10^{9} N.mm^{3}$ $EI = (1388 \times 10^{9})(1200) = 1.4985 \times 10^{12} N.mm^{3}$ $II = \frac{PX}{188 I} (36^{2} - 47^{2})$ $II = \frac{PX}{188 I} (36^{2} - 47^{2})$ $II = \frac{PX}{188 I} (36^{2} - 47^{2})$ $II = \frac{PX}{188 I} (36^{2} - 47^{2}) = -8.000 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -1/.632 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -1/.632 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -1/.632 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -1/.632 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -300(300)(60)(1.20^{2} - 60) = -300^{2}) = -10.000 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -300(300)(60)(1.20^{2} - 60) = -300^{2}) = -10.000 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -300(300)(60)(1.20^{2} - 60) = -300^{2}) = -10.000 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -300(300)(60)(1.20^{2} - 60) = -300^{2}) = -10.000 mm$ $II = \frac{PX}{185 I} (1.238 \times 10^{9}) = -300(300)(60)(1.20^{2} - 60) = -300^{2}) = -10.000 mm$ $II = \frac{PX}{185 I} = \frac{PX}{$

LOADING IN FIGURE P5-7. FIGURE 15-7 W18-55 STEEL BEAM: W460+82 TOTAL LDADING USE SUPERPOSITION 40 KN LOAD ONLY AT B, SUPERPOSITION Haken a 1.8.7 CASE A23 (6): L= 9900mm a= 8700 mm, b=1200 mm IOKN IOKN TWO TORN LOADS AT C AND E. CASE A-23 (C) : L=9900 mm a = 3700 mm IDAN LOAD ONLY AT F. a=8700 mm, b=1200 mm CASE AZ3 (6): L=9900mm

POINT OF MAXIMUM DEFLECTION IS
NOT DBVIOUS BECAUSE EACH CASE
PRODUCES A MAXIMUM DEFLECTIONAT
A DIFFERENT POINT. DEFLECTION
AT C, D, AND E ARE COMPUTED FOR
EACH LOKOING, THEN SUMMED. THE
MAXIMUM DEFLECTION FOR CASE I
OCCURS BETWEEN C AND D ATTHE
POINT CALLED H, 4226 mm FROM A.
DEFLECTION COMPUTED THERE ALSO.

PRODUCT OF EI
APPEARS IN ALL
EQUATIONS, $E = 207 \times 10^{3} N / mm^{2}$ $I = 890 / N \times 4.162 \times 10^{5} mm^{4}$ $I = 3.70 \times 10^{8} mm^{4}$ $EI = 7.66 \times 10^{13} N \cdot mm^{2}$

SUMMARY OF RESULTS:

I
$$N_C = -3.802 \text{ mm}$$
 II $N_C = -4.438 \text{ mm}$ III $N_C = -0.809 \text{ mm}$
 $N_D = -3.76 \text{ mm}$ $N_D = -4.816 \text{ mm}$ $N_D = -0.940 \text{ mm}$
 $N_C = -3.235 \text{ mm}$ $N_C = -4.438 \text{ mm}$ $N_C = -0.957 \text{ mm}$
 $N_C = -3.85 \text{ mm}$ $N_C = -4.689 \text{ mm}$ $N_C = -0.877 \text{ mm}$

BY SUPER POSITIONS

NO = -9.049 MM APPARENT MAXIMUM DEFLECTION AT

NE = -8.624 MM MIDDLE OF BEAN AT D.

WH = -9.416 MM

APP. AZY (a) AND AZY (b)

EI=(30x104)(0.08734)=2.62 x106

$$M_{6} = \frac{-15(8)^2}{6(2.62\times 0^6)}[3(10)-8] = -0.6085in$$

$$\eta_{0,2} = \frac{-P D^3}{3 E T} = \frac{-75(12)^3}{3(2.62 \times 10^5)} = -0.0165 \text{ in}$$

$$II) \eta_{B_2} = \frac{-Pa^2}{3ET} = \frac{-85(8)^3}{3(2.64 \times 10^9)} = -0.0055 \text{ in}$$

$$rac{1}{2} = \frac{-\rho a^{2}}{6ET} [31-a] = \frac{-85(8)^{2}}{6(0.64405)} [3(12)-8] = -0.0097 in$$

70 TAL DEFLECTION

$$I = \frac{bh^3}{12} = \frac{20(80)^3}{12} = 8.533 \times 10^5 \text{mm}^4$$

$$E I = \left[207 \times 10^3 \text{ p/mm}^2\right] \left[8.533 \times 10^5 \text{mm}^4\right] = 1.766 \times 10^{11}$$

$$(47)(6)$$

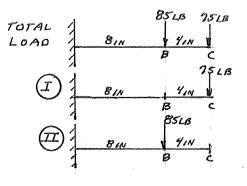
$$\underbrace{T}_{\text{Mel}} = \underbrace{\frac{P L^3}{3 = L}}_{\text{2COMM}} = -0.777 \text{mm}$$

$$\frac{A24-60}{\text{Mer} = \frac{Pa^{2}}{667}[3L-a] = \frac{-600(3c0)^{\frac{3}{2}}}{6(1/76640)^{\frac{3}{2}}}[3(700)-300]$$

TOTAL DEFLECTION

DEPLECTION INVERSELY PROPORTIONAL TO E

$$M_{c} = -0.869 \text{ mm} \times \frac{E_{3}}{E_{MAG}} = -0.869 \times \frac{207692}{45690} = \frac{-3.997 \text{ mm}}{45690}$$

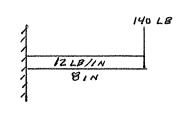


I= 110 /64 = 17 (0:80)/64 = 0.620 1 m W= TOTAL LOAD = LOL = (12 LB/W.)(8m)= 96 LB

$$\frac{A24.(c)}{7!} = \frac{\omega L^3}{8ET} = \frac{-96(8)^3}{8(30\times10^6)(6.0241)} = -0.01 \text{ 02 in}$$

$$\frac{A24-(0.)}{N_0} = \frac{-\rho l^3}{3ET} = \frac{-140(8)^3}{3(30(10)(0.020))} = -0.0396 \text{ in}$$

TOTAL m= m1+m2= -0.0102 -0.0396= -0.0498 in



9-61

FROM FIG P5-7, L=9900 mm

L/360 = 27.5 MM; LET MAN = -27.5 MM FROM PROBLEM 9-55 ; MMAX = -9.516 MM

FOR A W 18-55 BEAM WITH I = 890 INV

DEFLECTION INVERSELY PROPORTIONAL TO I.

SPECIFY: WIBXYO-LIGHTEST W460 x60 METRIC

OR W10 X60 -LEAST DEPTH W250X 89 METRIE

RESULT COULD HAVE BEEN FOUND BY USING

SUPERPOSITIN APPROACH OUTLINED IN

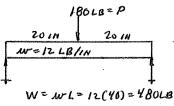
PROBLEM 9-55 WITH I TREATED AS AN

UNKNOWN. THEN SET MMAX E AND

SOLDE FOR IMIN FORM = 27.5 mm.

9-62

$$N_{MAx}^{2} = 0.080 \, \hat{M} = \frac{A23(\Delta)}{V86I} - \frac{A23(d)}{38YEI}$$



Superposition - Statically Indeterminate Beams

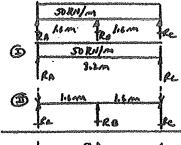
9-63

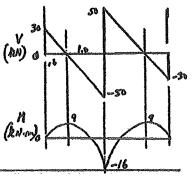
$$M_{C1} = \frac{-5 \text{ w.b.}^{3}}{397 \text{ g.T.}} \left(\text{CASG(d)} \right) \text{ TABLE A-23}$$

$$M_{C1} = \frac{-5 \left(/60 \times 10^{3} \right) \left(3200 \right)^{3}}{387 \text{ g.T.}} = 6.827 \times 10^{13}$$

$$M_{C2} = \frac{+P\ell^3}{4962} = \frac{+R6(3200)^3}{4967} = \frac{6.827 \times 10^8 (Re)}{(A2360)}$$

MG1 +MG2 = 0 -6.827×10¹⁸ + 6.827×10⁶ (Re) = 6 Re= 6.927×10¹³/6.827×10⁸ = 1.0×10⁸N Re = 100 kN THEN RA =RE = 30 kN





9-64

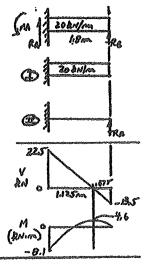
M81 + MB2 = D

-2.624x/63/EI + ROC1.944x/09)/EX = 0

RB = 262 4 NIB /1.944X109 = 13.50 RN = RB

THEN RA = 36-13.5 = 22.5 kN'=RA

MA = 36(0.9) - 13.5(1.9) = 8.1 kN /m (NEGATIVE)



9-65

$$M_{C_1} = \frac{F16. P9 - 38}{6EI} (3L - a) = \frac{-1200)(120)^2}{6EI} (3(216) - 120) = \frac{-152210^4}{6EI}$$
(A24(6)]

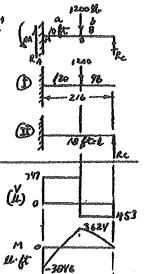
ye + yez = 0

-1.52/x10 /ET + 3.35/x10 (RJ/ET =0

Re= 1.521×109/3.359×106 = 45306=RC

THEN RA= 1200-453 = 747 IL = RA

(MA = 1200(10) -Re(18) = 12010 - 453(18) = 3846, B. At (MEGATUE)

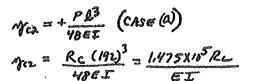




Superposition 1 Me + Me2 = 0

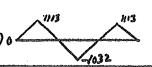
Me1 = $\frac{-\beta \alpha}{2462} (30^2 - 49^2) (CAS6(C))$ There A-23

Me1 = $\frac{-800(36)}{2462} [3)(192)^2 + (3\omega^2) = -6.265 \times 10^8$ The superposition of the



THEN MCI + MCZ =0 (W) 0 -1/265 1/108 1/1475 X 105 PC = 0 -441

Re- 1,265×10 / NV75×10 5 = 858 1 M BECAUSE OF SYMMETRY; RA=Re=37/11 (1.17) 0

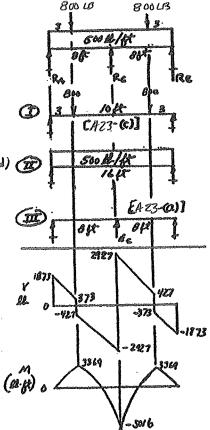


800 LB

9-67

F16. P9-67

 $M_{C_1} = \frac{-\rho_a}{246E} (3L^2 - 4a^2) = \frac{-1.265 \times 16^8}{EE}$ $M_{C_2} = \frac{-SWL^3}{3846E} = \frac{-S(8000)(192)^3}{9846E} = \frac{-157 \times 10^8}{EE}$ $M_{C_3} = \frac{+PU}{486E} = \frac{R_c(192)^3}{486E} = \frac{(1.475 \times 10^5)R_c}{EE}$ $THEN M_{C_1} + M_{C_2} + M_{C_3} = 0 \qquad A23 (4) (2)$ $-1.265 \times 10^6 = 7.37 \times 10^8 + R_c(1.475 \times 10^8) = 0$ EE = EE $R_{C_2} = \frac{1.265 \times 10^8 + 7.37 \times 10^8}{1.475 \times 10^5} = 5854 U = R_c$ $THEN RA=R_6 = 1873 M$



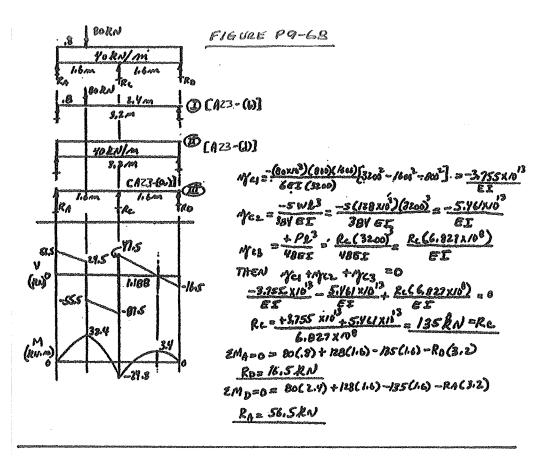
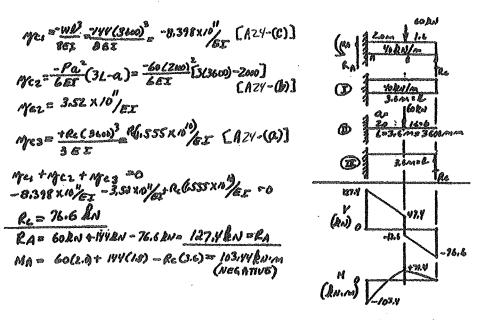
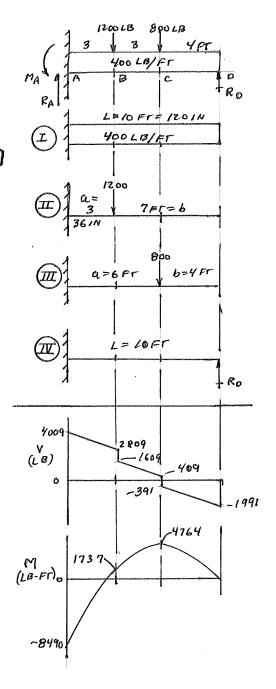


FIG. P9-69

W=N-L=(40 RN/m)(3.6m)=199.RN



 $\frac{1}{86\pi} = \frac{-4000(100)^3}{86\pi} - \frac{-4000(100)^3}{86\pi} - \frac{-1200(36)^2}{66\pi} [31100^{-36}]$ $\frac{1}{102} = \frac{-40^2}{66\pi} [3(0-a] = \frac{-1200(36)^2}{66\pi} [31100^{-36}]$ $\frac{1}{102} = \frac{8.398 \times h^2/ET}{66\pi} [424-(b)]$ $\frac{1}{103} = \frac{-800(72)^2}{66\pi} [31/20] - 72] = 1.991 \times 10^8/ET$ $\frac{1}{104} = \frac{-800(72)^2}{66\pi} [31/20] - 72] = 1.991 \times 10^8/ET$ $\frac{1}{104} = \frac{-400(100)^3}{66\pi} = \frac{5.76 \times 10^6 (Ra)}{61} [424-(a)]$ $\frac{1}{104} = \frac{-400(100)^3}{36\pi} = \frac{5.76 \times 10^6 (Ra)}{61} [424-(a)]$ $\frac{1}{104} = \frac{-400(100)^3}{36\pi} = \frac{5.76 \times 10^6 (Ra)}{61} [424-(a)]$ $\frac{1}{104} = \frac{-400}{36\pi} = \frac{-400}{36\pi} = \frac{-1200}{36\pi} = \frac{-1200(100)}{36\pi} = \frac{-1200(1$



APPENDIX AZS -(4) APP. A-19 (WOOD)

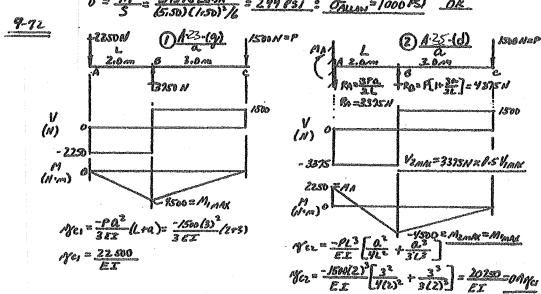
V_{MAX} AND M_{MAX} OCCUR AT SECOND SUPPORT

V_{MAX} = 0.607 AVL = 0.607 (100LB/FT)(2FT)= /21.4 LB

T_{MAX} = 3<u>V</u> = 3(121.4LB) = 22.00 Psi : T_{ALLOW} = 7085i - 0 &

MARK = 0.187 NF L2 = 0.187(1001.0/FT)(2.0FT)2 42.816.FT & 1211/FT = 5/3,618.118

6 = M = 518.6 18.11 = 249 831 : OALLOW = 1000 FSI OR



NO MAJOR DIFFERENCE BETWEE DESIGNS. (2) IS 10% CTIFFER. (2) HAS SO % HIGHER SHEARING FORCE.

9-73

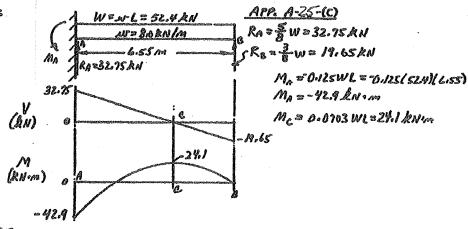
MULTIPLE DESIGNS POSSIBLE: USE VAME AND MARK FROM PROB. 9-72.

SPECIFY MATERIAL, DESIGN STEESS, DESIGN FACTOR, SHAPE OF

CROSS SECTIONS DIMENSIONS. BECAUSE BENDING MIMENT IS EQUAL

FOR BOTH DESIGNS, BOTH MAY BE THE SAME. BUT CHECK SHEAR.

9-74

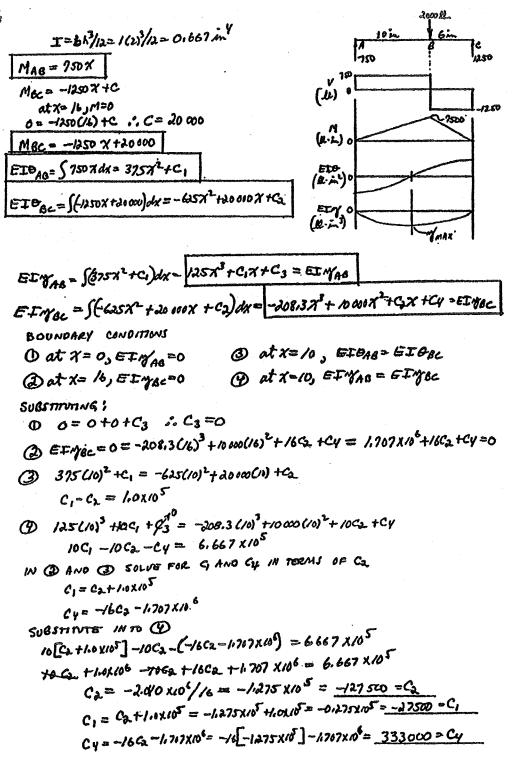


9-75

MULTIPLE DESIGNS PASSIBLE

Successive Integration Method

9-76



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FINAL GQUATIONS

ETO<sub>AB</sub> = 375X^2 - 27500

ETO<sub>BC</sub> = -625X^2 + 20000 \% - 127500

ETM<sub>BC</sub> = 125X^3 - 27500\%

ETM<sub>BC</sub> = -208.3X^3 + 10000X^2 - 127500\% + 333000
```

```
MAX of occurs where GFB = 0

SET GIGAS = 0 = 375X^2 - 27500

X = \sqrt{27500/375} = 8.56 in

MAXETY = (EIM_{AB})_{X=8.56} = 1.25(8.56)^2 - 27500(8.56) = -1.56 997 ll·in³

MAX of (EIM_{AB})_{X=8.56} = 1.25(8.56)^2 - 27500(8.56) = -1.56 997 ll·in³

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MAX of (EIM_{AB})_{X=8.56} = 1.25(8.56)^2 - 27500(8.56) = -1.56 997 ll·in³

Check: (CIM_{AB})_{X=8.56} = 1.25(8.56)^2 - 27500(8.56) = -1.56 997 ll·in³

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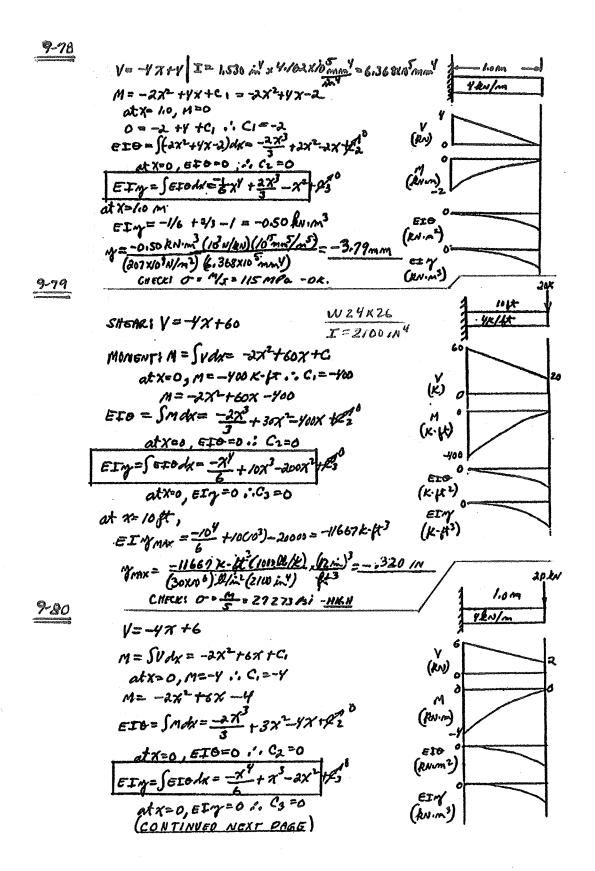
(CIM_{AB})_{X=8.56} = 1.25(8.56)^2 - 27500(8.56) = -1.56 997 ll·in³

(CIM_{AB})_{X=8.56} = 1.25(8.56)^2 - 27500(8.56) = -1.56 997 ll·in³

(CIM_{AB})_{X=8.56} = 1.25(8.56)^2 - 27500(8.56) = -1.56 997 ll·in³

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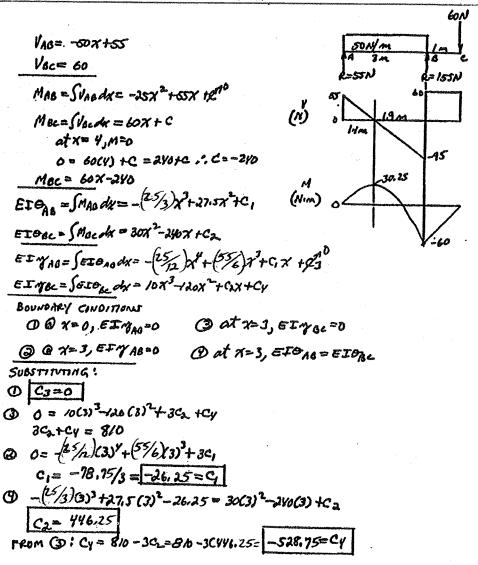
(CIM_{AB})_{X=8.56} = 1.25(8.56)^2 - 27500(8.56) = -1.
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9-80
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CONTINUED

9-81



(CONTINUED NEXT PAKE)

FINAL EQUATIONS

ETOAB = $-(25/3)\pi^3 + 27.5\pi^2 - 26.25$ ETOBC = $30\pi^2 - 240\pi + 446.25$ ETMAS = $-(25/2)\pi^4 + 35/6\pi^3 - 26.25\pi$ ETMAS = $-(25/2)\pi^4 + 35/6\pi^3 - 26.25\pi$

SMAPE OF DEFLECTION
CURVE

MMAX OCCURS WHERE EIB = O OR AT RIGHTEND OF OVERHANG,
EVALUATE EIBAG AT SEVERAL PHATS + USE SOLVER.

0 -26,25 20	† † † † † † † † † † † † † † † † † † †
0.5 -20.4/7	
1.0 -7.0'83	
1.5 7.50 EIO 0	1 15
2.0 17.003	1) 1/31 4 1/34 (1 1 1 1
25 15.417	
3,0 -3.75	610=0 AT X=124 M
ROOTS FOR EIDAB! 20	AND X= 2.93 M
$x_1 = 1.2351 \text{m}$	
$\chi_2 = 2.9341 \text{m}$	

EVALUATE EIN AT X=1,24 m, X=2.93 m, AND X=4.0 m.

$$\begin{split} & \left[\text{EIM}_{A=1,24m}^{1} = -2.083 (1.24)^{4} + 9.167 (0.24)^{3} - 36.26 (1.24) = -30.0 \text{ N·m}^{3} \\ & \left[\text{EIM}_{AB} \right]_{A=2.93m}^{1} = -2.083 (2.93)^{4} + 9.167 (2.93)^{3} - 26.26 (2.93) = +0.121 \text{ N·m}^{3} \\ & \left[\text{EIM}_{BL} \right]_{X=2}^{1} = -2.083 (2.93)^{4} + 9.46.25 - 528.7 = -23.75 \text{ Nam}^{3} \frac{\text{MAX}}{\text{MAX}} \\ & \left[\text{REQ'D ID} \frac{-23.75 \text{ N·m}^{3}}{\text{EMMAX}} - \frac{-33.75 \text{ N·m}^{3}}{(207 \text{ N/m}^{3})^{2} (-1.12m)} \frac{(10^{3} \text{ m/m})^{5}}{\text{M}^{5}} = 14.5 \text{ LOS mm}^{3} \right] \\ & \text{CONVERT ID} \frac{1.15 \times 10^{5} \text{ m/m}^{4} \times 2.403 \times 10^{5} \frac{1}{\text{m/m}^{4}} = 0.276 \text{ m}^{4}}{\text{M}^{4}} = 0.276 \text{ m}^{4} \end{split}$$

POSSIBLE BEAM DESIGNS &

METRIC

1. 12 IN. SCHYO PIPE: I = 0.3099 1H4

PIPE 38 STP

Z. C3×6 CHANNEL: Iy=0.300 1N4 Y-

680 x 8.9

- 3. 2x2x 4 HOLLOW STEEL TUBE: I=0,747 /N" HS55/X5/X64
 CHECK: 0 * M/S OK FOR ALL DESIGNS.
- 4. MECHANICAL TUBING: 2.0 IN O.D X O.1341A WALL I=0,3441N4

 METRIC: 50.8 mm OD X 3.464 mm WALL; I=1.43 X/05 mm 4

ZORN 30RN SELECT ALUMINUM I'S SAM ; 02 = 121 MPR 5 = M = 17.6x/03 Nim x 103 am = 1.46 7x/05 mm3 USE I/18 x 8.630; 5 = 2.01 x 105 mm3 I = 1.79 x 107 mm 4 RNEDI Rolerdo ZB SAME AS ITX5,800 (kn) 8 MOMENT -ZZ $M_{AB} = 28X$ 17.6 MACE OX to BUT AT X= 1, M=11.2 M RNIM 11.2 = 8Q4) +C C= 11.2-32=8.0 MOL = 8X +8 ero MCD = -22X +C BUT AT X= 210, M=0 (AHML)0 0 = - 22(2,0) +C c= 44 ery o Mc0 > -22x +44 (RNIM3) SLOPS -EIDAG = SMARCH = 14x2+C ETOBE = SMOC AX= 4x++8x+C2 5 IOCO = SMCO dx = -11 x2+44 x+C3 DEFLECTION -EINAB = SEIONE EX= (14/3) x3+C, X+C4 EINBC = SETOBLOW= (4/3) X3 +4x2+c2x+C5 EIT co = SEIO co du - ("/3) x3+20x2+C3X+C6 BOUNDARY CONDITIONS 3 atx=0.4, ETONG=ETON (5) atx=12, ETONC=ETONO O atx=0, EIMB=0 Datx=0,4, EIT AB=EITHE (6) AtX=1,2, ETTEL=EITE @ at x= 2.0, = I 700=0 SUBSTITUTING O 0= C4 @ ETTEO = 0 = - (1/3)(2)3+ 22(2) + 2C3 +C6 203+06=-58.66 (CONTINUED NEXT PAGE)

1,29 + 45 -1,263-6=17.28

Solve Simultaneously
$$C_1 = -10.56 \qquad C_2 = 0$$

$$C_2 = -12.16 \qquad C_5 = 0.2433$$

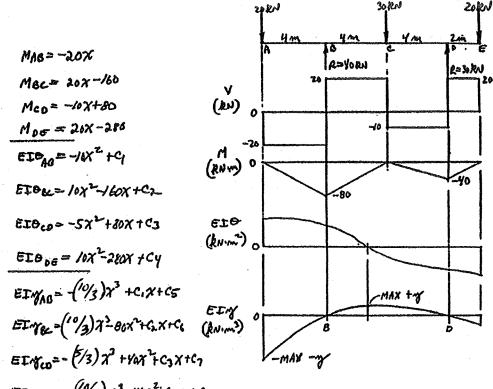
$$C_3 = -33.76 \qquad C_6 = 8.8533$$

FINAL EQUATIONS

EIGAB = $147^2 - 10.56$ EIGAB = $4.667x^3 - 10.56x$ EI

SET GIOBC = 0 =
$$4x^2 + 8x - 12.16 = x^2 + 2x - 3.09$$
 $x = \frac{-2 \pm \frac{1}{2}}{\sqrt{9 - 9(-3.01)}} = -1 \pm 2.01 = \pm 1.01 \text{ m} - 42.10 \text{ POINT}$

THEN MAY occups At $x = 1.01 \text{ m}$
 $\left[\text{EINSE}\right]_{x = 1.01} = \left(\frac{4}{3}\right) \left(\frac{7}{101}\right)^3 \pm 9 \left(\frac{7}{101}\right)^2 - 12.16 \left(\frac{7}{101}\right) + 0.213 = -6.615 \text{ kN/m}^3$
 $\left[\text{EINSE}\right]_{x = 1.01} = \left(\frac{4}{3}\right) \left(\frac{7}{101}\right)^3 \pm 9 \left(\frac{7}{101}\right)^2 - 12.16 \left(\frac{7}{101}\right) + 0.213 = -6.615 \text{ kN/m}^3$
 $\left[\text{Borns}\right]_{x = 1.01} = -6.615 \text{ kN/m}^3 - \frac{6.615 \text{ kN/m}^3}{61 \times 10^3 \text{ km/m}^3} \left(\frac{7}{101}\right) + \frac{7}{101} \left(\frac{7}{101}\right) + \frac$



ETYDE= (10/3) 73-148x2+C4X +C8 BOUNDARY AND CONTINUITY CINDITIONS

CONSTANTS OF INTEGRATION -FROM SIMULTANEOUS SOLUTION OF @ THRU @

$$C_1 = 306.66$$
 $C_5 = -0.63.33$
 $C_2 = 626.66$ $C_6 = -19.40$
 $C_3 = -333.33$ $C_7 = 1/20$
 $C_4 = 1826.66$ $C_8 = -7520$

CONTINUED NEXT PAGE

FINAL BOUATIONS

EIOR = $-10x^2 + 306.\overline{66}$ EIOR = $-10x^2 + 60x + 606.\overline{66}$ EIOR = $-10x^2 + 60x + 606.\overline{66}$ EIOR = $-5x^2 + 80x - 333.\overline{33}$ EIOR = $-(9/3)x^3 + 30\overline{6}x - 10/3.\overline{33}$ EIOR = $-(9/3)x^3 - 80x^2 + 60\overline{6}x - 1940$ EIOR = $-(9/3)x^3 + 100x^2 - 333x + 1000$ EIOR = $-(9/3)x^3 + 100x^2 - 333x + 1000$ EIOR = $-(9/3)x^3 - 140x^2 + 180\overline{6}x - 7500$

SET BEBBC = 0 = 10x2-160x+626 = 72-16x+62.6

X= 16 ± \(\frac{16^2-4(62.6)}{2} = 8 ± \(\frac{1}{2}(2.37) = 9.16 \text{ or } \(\frac{6.84\text{not}}{10}\)

LUNYALID -NOT IN
SEGMENT. 8C

MAK of AT X= 0 OR X= 6.84 m OR X= 14 m

OR X=0; EIMAB = -1013 RII. m3 MAY NEG. M

at x = 6.84m ; EI yec =+ 170 kmm3 MAX POS. m

at X= 14; EINO6= -240 km3

E = 207 × 109 M/m2 W360 × 39 STEEL BEAM

I = 1.02 × 108 mm 4 APP. A7 (SI) S = 5.79×105 mm³

atx=0; m= -1013×103 N·m3 (105mm5/m5) = -48.0 mm

 $atx = 6.84 \text{ m}; \ \gamma = -48.0 \times \frac{170}{-10/3} = +8.07 \text{mm}.$

atx= 14m; y= -48.0mm x -240 = -4.37m M

CHECK BENDING STRESS $O = \frac{M}{S}$, $M_{MAX} = 80$ kN in $O = \frac{80$ kN·m $\times \frac{10^3}{5.79} \times \frac{10^3}{10^5} \times \frac{10^3}{M} \times \frac{10^3}{M} = 138$ MPa ASTM A992 STRUCTURAL STEEL $S_y = 345$ MPa $O_0 = 0.66$ $S_1 = 0.66$ (345) = 228 MPa $O_0 = 0.66$

MOMENT: MAB= -X Mox = 2,2X -0.64 Mc0 = -1.8X+0.46

MD6 = 3.0 X - 4.8

ETOAB = SMAG HX = -0.5x2+C1

EIOBL=SMBLOW= N/X2-0,64X+C2

EIOco = SMco Ax = -04x2+0.96x+C3

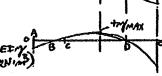
EIODE = SMOE dx = 1.5x2-4.8x+Cy

EI MAG = SEIBAB dx = -0.16673+C, X+C5

EIMBC= SEIBACON = 0.366 x3-0.32x2+C2x+C6 (bu.n)

EIMCO - SEIOCO dx = -0.3x3 + 0.48x +C3x+C7

ETy = SEIO DE dx - 0.5x3 - 2.4x2+C4x +C8



GORN YORN

12,12

(NA)

(Lim)

3,0 RM

REY.BRN

.1.8

BOUNDARY CONDITIONS

Oct 7= 0.2 , ETNAB=0

3 at x = 0.2, ETO A8 = EIO &C

(Datx=0,2, EIMBC=0

(B) at x= 0.4, ETOGE= \$10co

Dat x=1,2, EI yco =0

O ATX= 1,2, ETOED = ETODE

(9) at x=1.2, EI you=0

@ at x= 0.4, EIMOL = EIMCO

CONSTANTS - FROM SIMULTANEOUS SOLUTION OF (1) THROUGH (3)

C1= 0.4906

C5=-0,0968

022 0.1586

C6 - -0.02/86

 $C_3 = -0.16/3$

C7 = 0.020B

C4 = 3.2946

 $C_{B} = -1.316$

(CONTINUED NEXT PAGE)

FINAL EQUATIONS

 $EID_{AB} = -0.5\chi^{2} + .4096$ $EIM_{AB} = -0.466\chi^{3} + .4906\chi - 0.0968$ $EID_{BC} = 1.1\chi^{2} - 0.64\chi + 0.1586$ $EIM_{AC} = 0.366\chi^{3} - 0.32\chi^{2} + 0.5804 + 0.02$ $EID_{CO} = -0.9\chi^{2} + 0.96\chi - 0.1613$ $EIM_{CO} = -0.3\chi^{2} + 0.48\chi^{2} - 0.161\chi + 0.0008$ $EID_{CC} = 1.5\chi^{2} - 4.8\chi + 3.2446$ $EIM_{CO} = 0.5\chi^{3} - 3.4\chi^{2} + 3.244\chi - 1.3616$

DEFLECTION AT N= 0.8577 m IN SEGMENT CO EIN/CO = -0.3 (0.8586)3+6.48(0.836)2-0.161(0.8586)+0.0208 = 0.0461kN·m3

AT X=0 EIMAB = -0.166(0)+0.496(1)-0.0968 = -0.0468 & N.m3

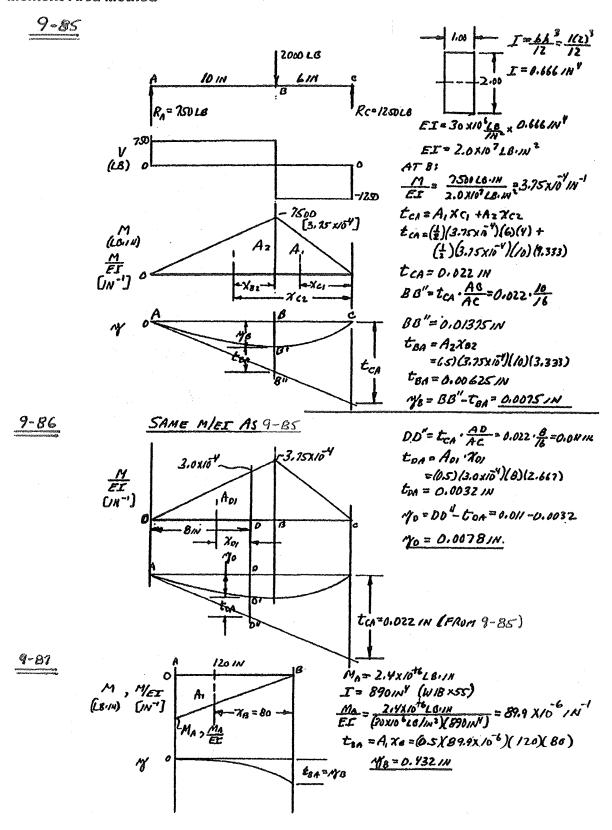
ATX= 1.6 m EINO==0.5(1.6)3-2.4(1.6)2+3.295(1.6)-1.362=-0862/2.1.m3 MAXIMUM

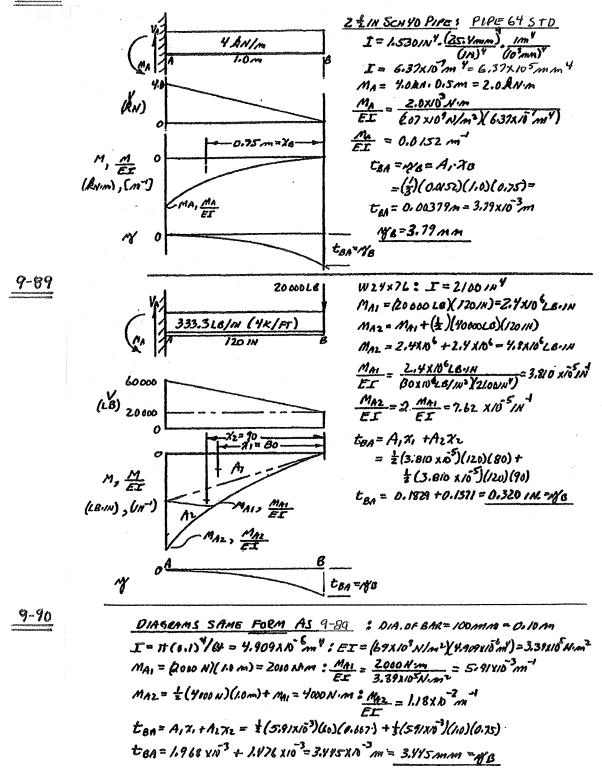
FOR MAX = -0.13 mm & E=207×103 N/mm²

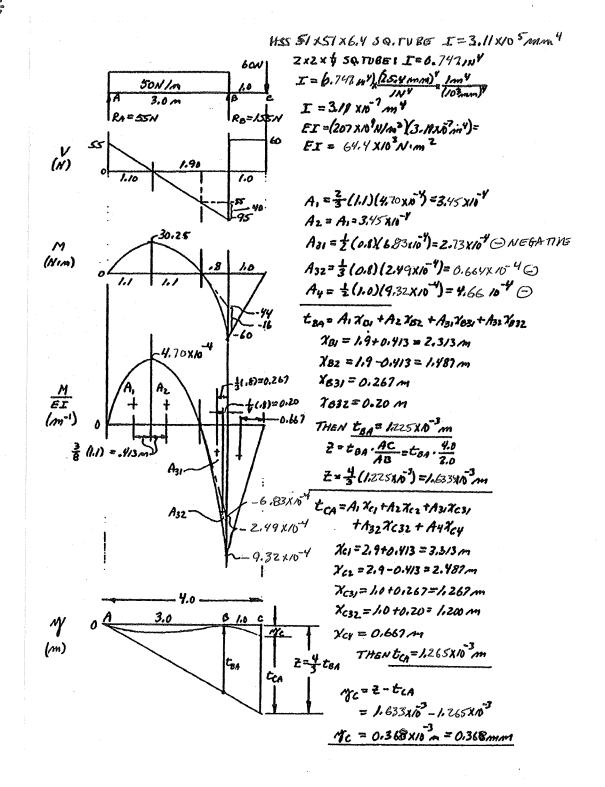
I = EIN - -0.186×103 N·m³ (103mm) = 6.91×105 mm4

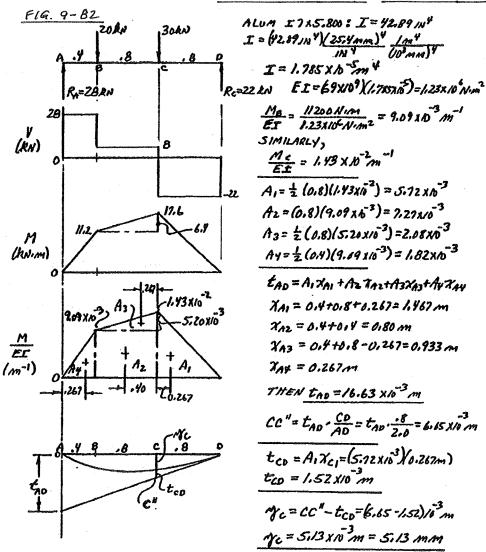
Eng (207×103 N/mm²)(-0.13 mm) m³ = 6.91×105 mm4

Moment-Area Method

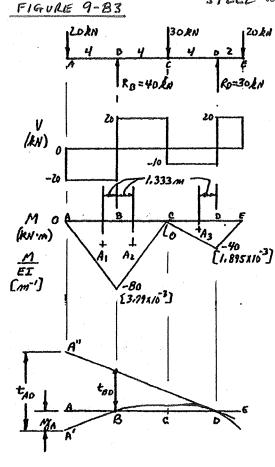








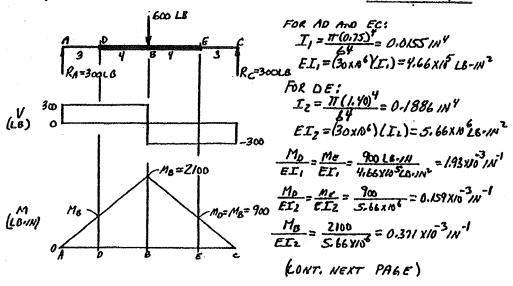
STEEL W360 x39 I= 1.02 x108 mm4

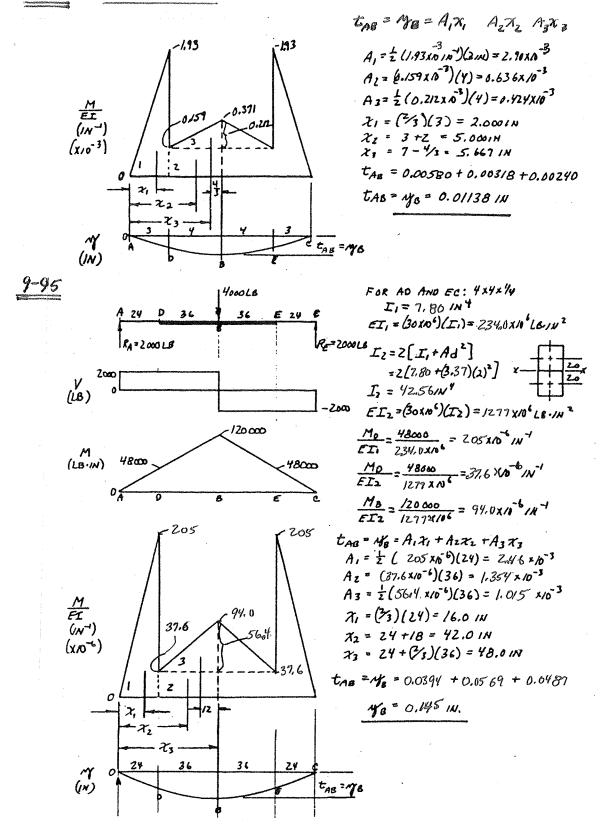


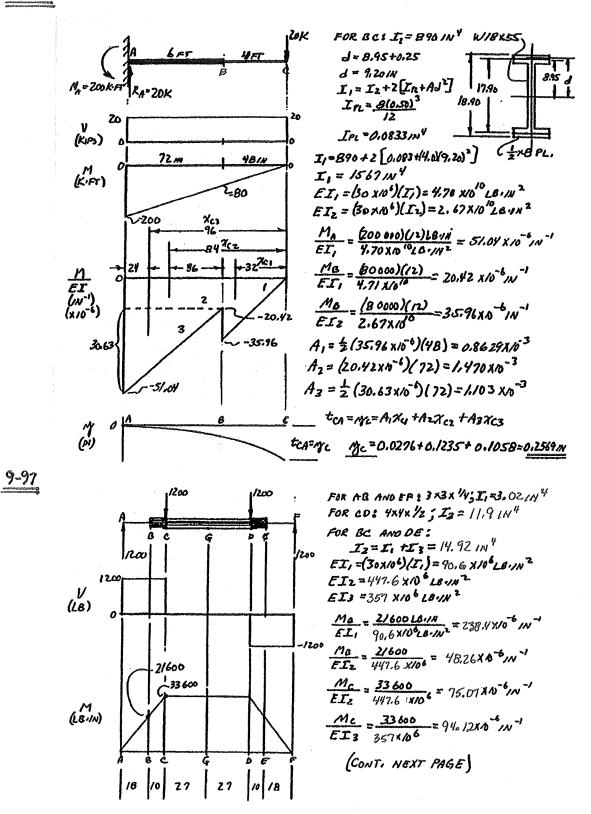
$$V/4 \times 26$$
: $I = 245/N^4$
 $I = 245/N^4) \frac{(25,4000)^4}{(10^2 mm)^4} \frac{1}{(10^2 mm)^4}$
 $I = 1.02 \times 10^{-4} m^4$
 $EI = 1.02 \times 10^{-4} m^4$
 $EI = 1.02 \times 10^{-4} m^4$
 $EI = 21.1 \times 10^{-6} N \cdot m^2$
 $\frac{M_0}{EI} = \frac{80000 N \cdot m}{21.1 \times 10^{-6} N \cdot m^2} = 3.79 \times 10^{-3} m^{-1}$
 $\frac{M_0}{EI} = \frac{1}{2} \frac{M_0}{EI} = 1.895 \times 10^{-3} m^{-1}$
 $\frac{M_0}{EI} = \frac{1}{2} \frac{M_0}{EI} = 1.895 \times 10^{-3} m^{-1}$
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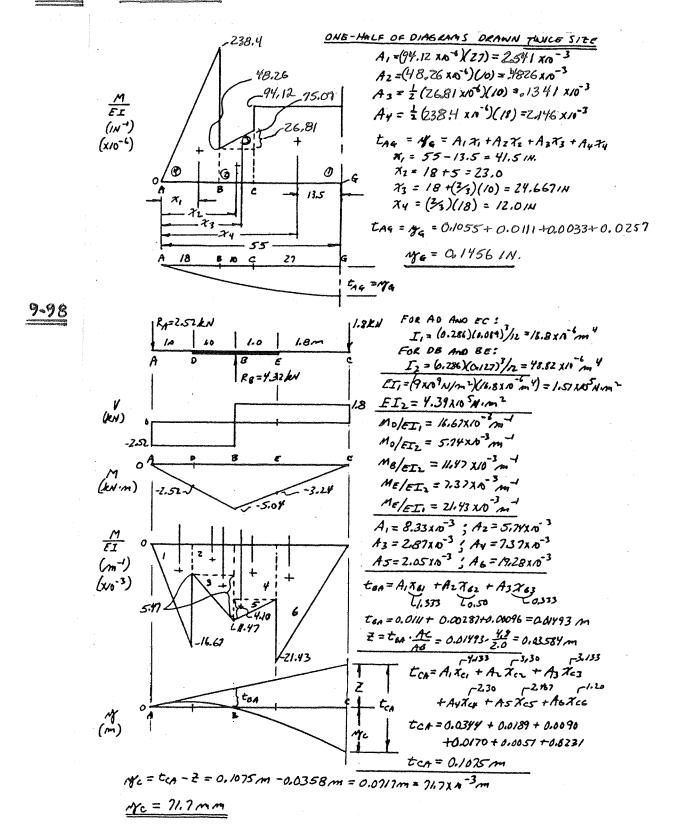
MA = tAO - AA" = (101.1 - 53.1)(103) m = 48.0 x N3 m = 48.0 mm = MA

9-94









CHAPTER 10 **Combined Stresses**

Combined Normal Stresses

$$\frac{1D-1}{M} = \frac{1230L6 \times 481N}{1040L6 \cdot 1N^{2}A} = \frac{1.7041N^{2}}{1.0141N^{2}} = \frac{1.040L6 \cdot 1N^{2}}{1.0141N^{2}} = \frac{1.0510PSi}{1.0141N^{2}} = \frac{1.0510PSi}{1.0141N^{2}}$$

$$O_{MAX} = \frac{F_h}{A} + \frac{M}{S} = \frac{1700 \, \text{N}}{1350 \, \text{mm}^3} + \frac{1.029 \, \text{N} \cdot \text{O}^3 \, \text{N} \cdot \text{Im}^3}{16875 \, \text{mm}^3} = \frac{62.2 \, \text{MPa}}{62.2 \, \text{MPa}}$$

400 Fh = FCOSYO' = 4596LB WIZXIB BEAM ! A = 477114 \$5=17.114 ---- F=6000LB Fv = F S/N YO = 38.57LB MOMENT DUE TO FU! M2= FV.52M M3 = 2.006x10 LB.IN

AT N:
$$O_N = \frac{F_A}{A} + \frac{M_2}{S} - \frac{M_1}{S} = \frac{4596}{4.91} + \frac{2.606810^5}{17.1} - \frac{55750}{17.1} = \frac{9480 \, PSI}{17.1}$$

AT M: $O_m = \frac{F_A}{A} - \frac{M_2}{S} + \frac{M_1}{S} = \frac{-7530 \, PSI}{5}$

$$\frac{104}{0} M = 6000LB \cdot 52/N = 3./2 \times 10^{5} LB \cdot /N$$

$$0 = \frac{M}{5} = \frac{3./2 \times 10^{5} LB \cdot /N}{17.1/N^{3}} = \frac{18246 PSi}{18246 PSi} TENSION AT N; COMPR. AT M$$

$$\frac{10-5}{AT N} = \frac{15}{A} + \frac{15$$

$$\frac{10-6}{\sigma} = \frac{(125N)(145mm)}{5} = \frac{18125 \text{ Normal } 85 = \frac{6h^{3}}{6} = \frac{H)(10^{3})}{6} = 66.67 \text{ mm}^{3}$$

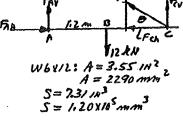
$$\sigma = \frac{-F}{A} - \frac{M}{5} = \frac{-125N}{40mm^{3}} = \frac{18125 \text{ Normal}}{66.67mm^{3}} = -3.125 - 271.9 = \frac{-215 \text{ MPA}}{2}$$

$$\frac{100}{\text{FAY}} = \frac{F_{CV}}{\text{FAN}} = \frac{12 \text{kn}}{2} = \frac{6.0 \text{kn}}{2}$$

$$\frac{100}{\text{FCh}} = \frac{F_{CV}}{\text{FAN}} = \frac{6.0 \text{kn}}{2} = \frac{9.6 \text{kn}}{2}$$

$$\frac{100}{\text{FAN}} = \frac{F_{CV}}{2} = \frac{6.0 \text{kn}}{2.0 \text{kn}} = \frac{9.6 \text{kn}}{2}$$

$$\frac{100}{\text{FAN}} = \frac{F_{CV}}{2.0 \text{kn}} = \frac{9.6 \text{kn}}{2.0 \text{kn}} = \frac{7.6 \text{kn}}{2.0 \text{kn}} = \frac{7.2 \text{kn}}{2.$$



h=4596LB

Fy=3851LB

10-B M=160N. BOMM = 12 BOO NIMM & A= \$ (02-12)=\$ (22-10) = 34.6 mm2 S= # (DY-JY) = 17(124-104) = 87.8 mm3 ATPOINTA: 0= - F - M 5= -160N 12800 Himm 10-9 F.B.D. OF TOP PART OF CLAMP M=F(26+5,5)=31.55F G = 8.45 DESIGN STRESS: Of = SA = 400 MPa = 100 MPa 3/15F(8,45) LET 07 = 07 = 100 MPa = -0.2408 F COMPL. I= 1032 mm F = 100/0.2408 = 415 N A= 51 mm2 ATB: $OB = \frac{F}{A} + \frac{MCb}{F} = \frac{F}{57} + \frac{3.55F(5.55)}{1032} = 0.1872 F TENSUM$ LET OB = 0] = 100MPa = 0.1812 F F=100/0.1872 = 534N LIMITING VALUE OF F=415N IF SM IS EQUAL IN TENSION AND COMPRESSION. NOTE THAT SMC > SMt FOR COME CAST ALLOYS. 10-10 ASTM AZZO 45008: Su= 448 MAC, Suc= 1650 MAC. Od= 448/4 = 112 MPa: Odc=1650/4= 412 MPa M=F(42+11.2)=53.2F $O_A = \frac{F}{IIY} - \frac{53.2 F(14.8)}{A80L}$ OA = -0.0806 F = OJc = 4/2 MPa. I = 8806 mm 4 F = 412/0,0806 = 5109 N ATB: 0 = F + 10 Cb = F + 53,2F(11,2) = 0,0764 F = O34 = 112 MOa F = 1/2/0.0764 = 1465 N LIMITING VALUE | 10-11 FOR M/6 = 2 THREADED ROD; STRESS AREA = 151 mm (APPA3) | COMPUTE SECTION MODULUS BASED ON P_{ROST} : $S = \frac{110x^3}{32} \frac{11(3x^2)}{32} = 226 \text{ mm}^3$ $C = K + \left[\frac{\mu}{A} + \frac{M}{3} \right] = 3.0 \left[\frac{1200}{159} + \frac{1200}{226} \right] = \frac{724 \text{ MBa}}{724 \text{ MBa}} \text{ TENSION}$ POR 02 = SV/2 & Sy = 20 = 2(724) = 1448 MPa USE AISI 4140 DOT 700, Sy=1462 MPa - ONE POSSIBLE CHOICE

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FROM PROBLEM P5-77: M=120 N·m : P=800N ANNL TENSION

  \frac{\sigma = \frac{P}{A} + \frac{M}{S} = \frac{P}{a^2} + \frac{M}{a^3/6} = \frac{P}{a^2} + \frac{6M}{a^3}}{MULTIPLY BY a^3}

                                                                       003= Pa+6M: 003-Pa-6M=0: LET 0=42Mla=42N/mm2
                                                                                  42 03- 800 a - 6(120000) = 0 8 THEN 0=26 mm
                   10-18 FROM PS-78 ? M=344LBIJN ? P=250LB AXIAL COMPR.
                                                                       0 = \frac{P}{A} = \frac{M}{S} = \frac{P}{A^2} = \frac{M}{A^2} = \frac{P}{A^2} = \frac{P}
                                                                       003 = -Pa - 6M: 003+ Pa+6M=0: LET 0=-6000PS; COMPR.
                                                                         -6000 03+250 a + 6(344)=0 & THEN a=0.720 IN
                         10-19 FROM P5-79: M= 42200 Nomm 1 P= 1200 N AXIAL TENSION
                                                                      FRONID-19: 0-03-Pa-6M=0: 4203-1300046/42200)=0:0=18.7mm
                         10-20 FROM P5-80: M = 52018-IN : P = 40018 AXIAL TENSION
                                                                  FROM 10-17: 0-a3-Pa-6M=0: 6000 a3-400a-6(520)=0: a=0.8321N
Combined Normal and Shear Stresses
                 \frac{1021}{A = 11(40)^{2}/4 = 1259 \, mm^{2} \, \text{? } \geq_{9} = 11(40)^{3}/L = 12566 \, mm^{3}}
C = \frac{L}{A} = \frac{150600 \, N}{12537 \, mm^{2}} = 119 \, MPa \, \text{? } T = \frac{T}{29} = \frac{500000 \, N \cdot mm^{3}}{12566 \, mm^{3}} = 39.8 \, MPa
T_{\text{MAX}} = \sqrt{\left(\frac{9}{2}\right)^{2} + 1^{2}} = \sqrt{\left(\frac{11}{2}\right)^{2} + 39.8^{2}} = \frac{71.6 \, MPa}{1.6 \, MPa}
              \frac{10-22}{10-22} A = \pi(2.25)^2/y = 3.98/H^2 : Z_p = \pi(2.25)^3/1 = 2.24/H^3
0 = \frac{P}{A} = \frac{4700016}{3.98/H^2} = 1180985; : P = \frac{T}{2p} = \frac{850016\cdot 11}{2.24/H^2} = 379585
                                                     TMAX = V[11809)2+37952 = 7019 PSI
             \frac{10.23}{A - 7(4.00)^{2}/9 = 12.57 / n^{2}} \stackrel{?}{\geq}_{\rho} = 77(4.00)^{3}/6 = 12.57 / n^{3}
\sigma = \frac{f}{A} = \frac{-40000 L^{6}}{12.57 / n^{2}} = \frac{3/8305}{12.57 / n^{2}} = \frac{25000 L^{6} \cdot / n^{2}}{12.57 / n^{2}} = 198905i
T_{MAX} = \sqrt{\frac{3/83}{2}} + 1989^{2} = \frac{254805i}{2}
                  10-24 FOR 12 IN PIPE & A = 15.74 IN2 : 2p = 94.18 IN3

0 = 7 = -250 000 LB = 15.74 IN2 = 15883 PS; & T = 7 = 180 000 LB:IN = 1911 PS;

T'MIX = \( \left( \frac{45883}{2} \right)^2 + 1911^2 = \frac{8168 PS}{2} \)
                  10-25 FOR 3 IN PIPE: A = 2.228 IN 2 2 = 3.448 IN 3

0 = P = 25000 LB = 1/221 PS; 2 = 15500 LB 1A = 4495 PS;

THAX = \( \frac{\frac{11271}{2}}{2} + 4495 \frac{2}{2} = \frac{7189 PS}{2} \]
              T = (20 LB)(8 PT)(12 M/PT) = 1920 LB \cdot IN 8 M = (20 LB)(15 PT)(12 M/PT) = 3600 LB \cdot IN
Te = \sqrt{7^2 + 17^4} = \sqrt{1920^2 + 3606^2} = 4080 LB \cdot IN
Zp = \frac{17}{16} \frac{D^4 - 1^4}{D} = \frac{17(1.50^4 - 1.375^4)}{18(1/.50)} = 0.195 / N^3
T = \frac{Te}{20} = \frac{4080 LB \cdot IN}{0.195 / N^3} = 20920 85 \frac{1}{18} = \frac{1}{18} \frac
                                                                LET TO = SY/2N & N= SY = 40000 = 0.96 UNSAPE
```

```
10-27 NEAR SUPPORT & T=300 F=300(1200)=3.6×105 Norman
                                         M = 450 F = 450 (/20) = 5.4 X/05 N MM
            Te = \sqrt{7^2 + M^2} = 6.49 \times 10^5 N \cdot mm : 2p = \frac{11}{16} (40)^3 = 12.566 mm^3
T = \frac{Te}{2p} = \frac{6.49 \times 10^5 N \cdot mm^3}{12.566 mm^3} = 51.6 m Pa
18-28 TOTAL DOWNWARD LOAD = ZOO + ZOO + 300 + 600 = 13 00 LB
               M=(1300 LB)(3614) = 46 800 LB.IN AT SUPPLRT
               NET TORQUE = 600(40) +300 (20) - 200(20) -200(20) = 18000 LB-IN /V
                Te = 172+112 = 18002 + 468002 = 50 142 L8 1N
                   REOD 20= Te = SO 142 LBITH = 6.27 IN 3 USE 4 IN SCHYO PIPE
Rotating Shafts - Combined Torsional Shear and Bending Stresses
\frac{10-29}{Z_{P}} = \frac{10^{3}}{16} = \frac{11(20)^{3}}{16} = 1571 \, \text{mm}^{3} : T = \frac{T}{2P} = \frac{1500000 \, \text{NMm}}{1571 \, \text{mm}^{3}} = 955 \, \text{m/s}^{2}
                 \sigma = \frac{M}{5} = \frac{360\,600\,\text{N'mm}}{785\,\text{mm}} = 459\,\text{MPa}
\tau_{\text{MAX}} = \sqrt{\left(\frac{Q}{2}\right)^2 + 1^2} = \sqrt{\left(\frac{457}{2}\right)^2 + 955^2} = \frac{982\,\text{MPa}}{2}
                                                                                                                                    13200 N
    10-30 S= #03 T(25)3 = 1534 mm3
          ZP = \frac{\pi D^{2}}{16} = 25 = 3068 mm^{3}
O = \frac{M}{5} = \frac{760000 N mm^{3}}{1534 mm^{3}} = 495 MPa
Y = \frac{I}{2p} = \frac{4500010}{3068} = 1467 MPa
T_{MAX} = \sqrt{\frac{(495)^{2}}{2} + 1467^{2}} = 1488 MPa
                                                                                                 3200
                                                                                                                                          3600
                                                                                         BO
                                                                                      (N) 0
                                                                                                                                            -3608
                                                                                                   760
\frac{ID-31}{T} = \frac{63000 (P)}{M} = \frac{63000(25)}{J/50} = J370 LB1A
\frac{AT B!}{ZP} = \sqrt{T^2 + JN^2} = \sqrt{J320^2 + J380^2} = J945 LB1N
\frac{ZP}{Jb} = \frac{ID^3}{Jb} = \frac{J7(J)}{Jb} = 0.196 JN^2
T = \frac{Te}{ZP} = \frac{J945}{0.196} = 9923 PS' = TS = \frac{SV}{ZN}
                                                                                                              460LB
                                                                                                                                  1685LB
                                                                                                                      Ra=917
                                                                                                                                                 228
                                                                                                               451
                                                                                                 (LB)
                                                                                                                                                  128
                                                                                                      -460
                                                                                                                                    1362
                RED D Sy = 2NT = 2(6)(9923) = 119 000 151
               AISI 1141 OOT 900 Sy=129 KS1,15% ELWA (W.IN) 0
  10-32 (a)

TA = (450-90)(6) = 2/60 LB · IN CCW = TAC
                                                                                                                                    Ro= 900
                                                                                                                                              1260
                                                                                                            1540
                To = 6200-240 X4) = 3840 LB.IN CW
          T_{E} = (0.50 - 2/0)(2) = 16.80 LB \cdot N CCW = T_{CE}
(b) Z_{P} = \frac{170^{3}}{16} = \frac{11.05}{16} = 1.05 N^{3} \cdot S = \frac{17}{32}D^{3} = 0.526 N^{3}
\frac{Ar C: T = \frac{2160(1.6)}{1.05} = 3291P3;}{0.526}
\sigma = \frac{9720(1.6)}{0.526} = 29.567 PS;
(C) T_{MAX} = \sqrt{\frac{9}{2}} + T^{2} = 15145PS; = T_{O} = \frac{5V}{2N}
                                                                                                                       RB=510
                                                                                                V ETO
                                                                                                                       -34
                                                                                                                      9720
                                                                                                                                          250
                  LET N=4
                  REOD SY = 2NT = 2(4)(15145) = 121 16142 (B.IN)
                 AISI /141 OOT 900, Sy=129KS), 15% ELONG.
```

```
10-33
TR = (500 - 200) 50) = 60000 Nomm
                                                                                                                                                                                                                                                                                                          TZON
                                             Tc = (600-120)(125) = 60000 N.MM
                                                                                                                                                                                                                                                                                                                                وعرا
                                    ATB: 70= $\frac{\pi(28)^3}{16} = 43/0 mm^3 : A = \frac{\pi(28)^2}{4} = 6/6 mm^2

S = \frac{\pi(28)^3}{2} = 2/55 mm^3
                                                                                                                                                                                                                                   W) 4
                                             T=T/2,=[60000/43/0]1.6=22.3 MPa
                                                                                                                                                                                                                                                              ... 840
                                        0= = 1/2 = [-6200/2155] 1.6 = 142.6 MPD NET TENSILE DE = -16.1 MPD TENSILE DE = 126.5 MPD T
                                                                                                                                                                                                                                                                                   192000
                                                                                                                                                                                                                                                                                                             24000
                18-34 REDO SY = ZN(67.1) = 5 37 MAR - USE AISI 1840 1100
Combined Axial Tension and Direct Shear Stresses
                                  8-32 UNC THREAD: DM=0.164IN: A= 0.0140 IN-
                                     IN THE EAOS: P= O-A+ = (5000 LB/W2)(0.0140 112) = 210 LB
                                     FOR PM: As = Am = # Dm/y = 17 (0.164) /4 = 0.02/11/12

G = P/Am = 2/0/0.0211 = 994/05i: T= Fi/As = 120/0.021 = 568/85i

TMAX = \(\frac{0}{2}\) + T = \(\frac{994}{2}\) + 568/ = 7548 PS/
              1036 FOR 14-20 UNC THREND: DA=0.150 N : At= 0.83/8 IN "
                                        P= 0-A+=(15000)(0.0818) = 477 LB
                                         FOR Dm : 0.250/N : AN=As = 17(0.25) 3/4 = 0.049/11
                                            \sigma = P/A_{p} = \frac{477}{0.6491} = \frac{9117051}{17051} = \frac{775}{0.0491} = \frac{1578895}{1578895}
T_{MAV} = \sqrt{\left(\frac{47}{2}\right)^{2} + 7^{2}} = \sqrt{\frac{(9717)^{2}}{2}} + \frac{15788^{2}}{2} = \frac{1651995}{1651995}
               10-37 FOR 4-48 UNF THREAD: DM= 0.112 IN: At= 0.006611N2
                                          P= O-A+= 15000 (0.00661)= 99.2 L8
                                           FOR Dn = 0.112 IN: An = As = TT (0.112) 1/4 = 0.009BSINZ
                                          0= P/A= 99.2/0.00985 = 10 069 15; 1= 1/As = 50/0.40985 = 5075 15;
TMAX = \[ \frac{(10069)^2}{2} + 5075 = \frac{7/49 851}{2}
              10-38 FOR 14-12 THREAD: DM=1.2501N: At=1.0731N2
                                         P= OAt = 15000 (1.073) = 16095LB
                                        FOR OM: AR = As = 17(1.25)2/4 = 1.227112
                                        \sigma = \frac{P_{A_A}}{A_A} = \frac{16095}{1.227} = \frac{1311505}{1.227} = \frac{15}{100} = \frac{2500}{1.227} = \frac{2037}{100} = \frac{13115}{2} + \frac{2037}{100} = \frac{13115}{100} = \frac{1311
               103 FOR M16+2: DM=16 mm : At= 157 mm2
                                     P= 1-A== (120 N/mm2)(157mm2)= 18840 N
                                     FOR On = 16mm: An = As = 11(16) 1/4 = 201 mm2
                                    0= P/An = 13840 N/201 mm = 93,7 MPa: T = Fs/As = 8000 N/201 mm = 39.8 MPa

TMAX = V(\frac{\pi}{2})^2 + T^2 = \frac{(93.7)^2}{2} + 39.8^2 = 4.5 MPa
            1040 FOR MY8×5: Dm=48mm : A+= 1473 mm
                                     P= OAt= (120 N/mm2) (1473 mm2) = 1.77x15N
                                     FOR DA = 48mm: An = As = T(48) 1/4 = 1810 mm 2
                                     0= P/A = 1.77 ×10=N = 97.7 MPa: 7 = Fs = BOODON = 44.2 MPa
                                    TmAx = 7 (97.7)2+ 44.22 = 65.9MPa
```

Combined Bending and Vertical Shear Stresses

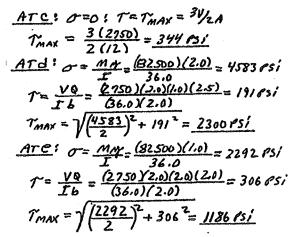
ID-41

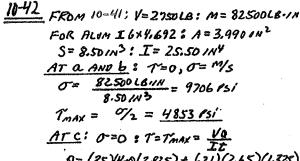
AT B:
$$V = 2750 LB : M = 82500 LB : IM$$
 $V_{MAX} = \sqrt{(0/2)^2 + V^2}$

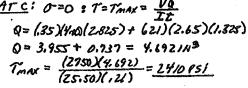
FOR BEAM CROSS SECTION 8

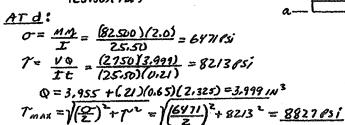
 $A = Bh = (216) = 12.00 IM^2$
 $S = bh^2/6 = (2)(6)^2/6 = 12.00 IM^3$
 $I = bh^2/12 = (2)(6)^2/12 = 36.00 IM^4$
 $AT = \Delta : V = 0 : O = M/S$
 $O = \frac{82500 LB : IM}{12.00 IM^2} = 683585i$
 $V_{MAY} = \sqrt{(2)^2 + V^2} = \frac{G}{2} = \frac{3438 /5}{12.00 IM^2}$

AT b: SAME AS (0.)



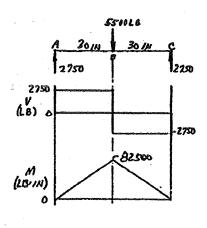


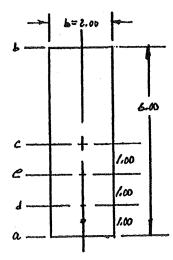


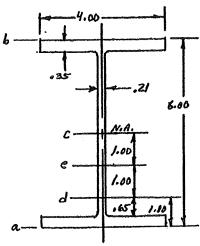


AT
$$e$$
:
$$\sigma = \frac{MM}{I} = \frac{82500(1.0)}{25.50} = 323575i$$
: $0 = 3.955 + 10.00$)(1.65)(0.825) = 4.241 i 3
$$T = \frac{V0}{It} = \frac{(2750)(4.241)}{(25.50)(0.01)} = 217875i$$

$$T_{MAX} = \sqrt{\frac{3235}{2}}^2 + 2178^2 = 271315i$$







```
10-43 SEE 10-41 FOR BEAM SECTION PROPERTIES
                                                                                         TOTAL LOAD = GOSBLB
            AT MIDDLE OF BEAM - B
             AT a ANO b: 0= M = 45000 = 3750 PS!
             T=0: TMAX= = 1875 PSi
            AT 6: 0=0: T=0: TMAX=0
            AT d: 0= MM = 45000 (2.0) = 2500 (5)
              T=0: TMAX = 0/2 = 1250 PSI
            ATE: 0= MM = 4500(10) = 120 PSi : T=0 : TMAX = == 625 PSI
            AT SUPPORTS A AND C: Y=3000LB:M=0:0=0
            AT a ANOb: T= 0: TMAK=0
           ATC: T= 3 U/21 = 3(3000)/(2)(12) = 325 PSI = TMAX
           ATO & T = TMAX = VO = (3000 (20)(10)(2.5) = 208 85;
           ATC: 7=7 MAX = VO = (3000)(1.0)(2.0)(2.0) = 333/5/
            AT D - 15IN FROM A: V= 1500 LB : M= 33750 LB :IN
           AT a AND 6: T=0: 0= M = 337.50 = 2813 PSi : TAN = = 1406 PSi
           ATC: 0-0: T= 3V = 3(1500) = 188/5/ -TMAX

\frac{AT d:}{I} \sigma = \frac{MN}{I} = \frac{(337501(2.0) - 187505)}{36.0} \\
T = \frac{V0}{It} = \frac{(1500)(2.0)(1.0)(2.5)}{(36.0)(2.0)} = 10475i

T_{MAI} = \sqrt{\frac{1875}{2}} + 104^{2} = 94365i

          AT @: \sigma = \frac{MM}{\pm} = \frac{(33.250)(1.0)}{36.0} = 93883i
T = \frac{V\Phi}{EE} = \frac{(500)(2.0)(2.0)}{(36.0)(2.0)} = 16785i
T = \frac{V\Phi}{EE} = \frac{(500)(2.0)(2.0)}{(36.0)(2.0)} = 16785i
Noncircular Sections – Combined Normal and Torsional Shear Stresses
            FROM FIG 4-27 : Q= 0.20803=0.208(25)3=3250mm3
             T = T/Q = \frac{245000 \text{ N·mm}}{3250 \text{ mm}^3} = 75.4 \text{ mPa} \cdot 0 = \frac{P}{A} = \frac{75000 \text{ N}}{(25)^2 \text{ mm}^2} = 120 \text{ mPa}
T_{MAX} = \sqrt{\left(\frac{O}{2}\right)^2 + 1^2} = \sqrt{\frac{120}{2}\right)^2 + 754^2} = \frac{96.4 \text{ mPa}}{2}
 \frac{10.45}{T} FROM FIG. 4-27: Q = \frac{6h^2}{3+1.8(h/6)} = \frac{50(30)^2}{3+1.8(90/50)} = 11029 mm^3
T = \frac{T}{Q} = \frac{525000 \text{ N.mm}}{11029 \text{ mm}^3} = 47.6 \text{ MPa: } 0 = \frac{P}{A} = \frac{175000}{(30)/50} = 116.7 \text{ MPa}
           TMAX = V(116.7)2+ 47.62 = 75.3 MPa
```

$$\frac{10^{-46}}{7^{-27}} FROM F14.4-27: Q=0.050 Q=0.050 (50)^{3} = 6250 mm^{3}$$

$$7 = \frac{1}{Q} = \frac{775 000 N \cdot mm}{6250 mm^{3}} = 124 Mla: 0 = \frac{P}{A} = \frac{115 000}{\frac{1}{2}(50)(43.5)} = 106 Mla$$

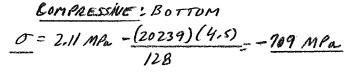
$$T_{MAX} = \sqrt{\frac{106}{2}}^{2} + 124^{2} = 135 Mla$$

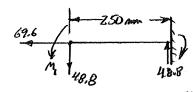
$$\frac{10-47}{A)} S_{y} = SDKSI; O_{\theta} = \frac{Sy}{3} = \frac{5000}{3} = \frac{16667}{8} = \frac{P}{A}$$

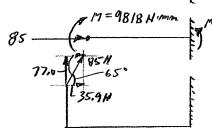
$$(A) P = O \cdot A = \frac{16667 LB}{LB} \frac{333851}{2} = \frac{40667}{2} LB$$

$$TMAX = \frac{1}{2} = \frac{8333851}{2} = \frac{1}{2} = \frac{1$$

ADDITIONAL REVIEW AND PRACTICE PROBLEMS







$$0 = \frac{-35.9}{33.0} - \frac{(23396)(25)}{/28} = -1.09 - 457.0$$

$$0 = -458 \text{ m.c.}$$

10-52 3 x 3 x 14 STEET TUBING, 5=201 IN3, A= 2.44 IN2 M,=(615.610)(15.0 IN) = 9234 LB -11 D Mz = (691 LB) (7.51N) = 12683 LB.IN) 615.6 AXIAL LOAD = 169/LB & TENSION NET BENDING MOMENT = MZ-MI MNET= 12 683 -9234 = 3449 LB-IN) PRODUCES TENSION AT A COMPR. ATB 180018 OA = (169110) + (3449 LB-W) = 693 + 1716 = 2409 PSI TENSION OB = 693 - 1716 = -1023 PSi COMPRESSION 10-53 LOAD = P= 34.0 AN Fx=102.2k 600 P=34.0 RN P=34.0 KN 2250 (RN) 0 30 -34.0 SECTION THROUGH EMF = 0 = (34.0RN) (1800mm) - AEy (1425mm) JOINTS EMC=0 = P(1800) - By (900) AEy= 42,95 RN By=34,0 RN(2)=68KN EFy=0= 4295-34.0-Fy; Fy=8.95 kn } EFy=0= Cy-340-68.0 AE = AEY/SINO = 42.95 MM/SIN ZZ.80 = 110.8 MM Cy = 102 AN TAN X= BX/BY Bx = Bytonk = 68 tan 21.80 = 27.2 kN AEX = At CUS 0= (110,8 MN) Cos 22.80 = 102,2 MN -Cx = BX AB = By/cosox = 68/co 21.80= 73.2 KM AT E: FLAT PLATE WITH CENTRAL HOLE APP. A-21-4, CURVEC .- BENDING 0= MKtC - Kt Mw = (12750 km mm) (100 mm)

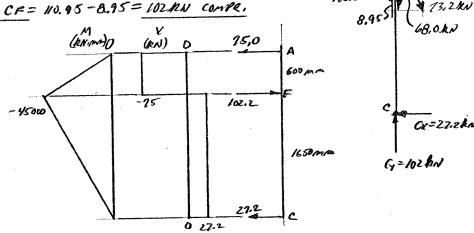
I NET (1007-d3)(t) (1007-303)(25) 20004 =52.4 MPa. (1002-303)(25) AMANY BENDENG du= 30/100 = 0.30 => Kt=110 TENSION-TOP; COMBRI-BOTTOM DIRECT COMPRESSION OF = KEAEX = (3.70)(102.7 km) 1000N = 216 MPa.

K=3.70 FOR CHAVE R Kt=3,70 FOR CVAVE B COMBINATION OF OB AND OC IS PROBLEMANC BECAUSE OBMAY OCCURS NEW TOP OR BOTTOM OF SECTION WHICE GEMAN OCCURS NEAR CENTERLINE NEAR HOLE, THAY TENSILE IS AT E TO LEFT WHERE OF = D. YMPA AND NO COMPR. STRESS. OMAX COMPR. IS TORIGHT OF E WITH AVAIVE BETWEEN 216MPG AND 216+52.4 = 268 MPW ON LOWER PART OF THE CROSS SECTION. (HEXT PAGE)

10-53 (CONTINUED)

MEMBER AFC - LOADS FROM FOO OF WHOLE STRUCTURE AXIAL LOAD; AF = 42,95+68.0= 110.95 KN COMPR.

CF= 110.95-8.95= 102.MN COMPR.



27,2 km

42,95

BENDING STRESS ATF (SAME SECTION PROPERTIES AS AT E) (KE=1.0)

$$O_{b_{\xi}}^{-} = \frac{M \, \text{KtC}}{I \, \text{HET}} = \frac{[75000 \, \text{kM-mm}] \, w}{(w^3 - d^3) \, t} = \frac{(55000 \, \text{km/mm}) \, (100 \, \text{mm})}{(100^3 - 36^2) (25) \, \text{mm}} \, \text{MeV}$$

OBF = 308MPA TENSILE ON RIGHT SIDES COM PR. ONLEFT.

COMPRESSION NEAR F USE PF=1/0.95 kN ABOVE F. K+=3.70 FOR d/w=0.30

COMBINED OF AND OF IS PROBLEMATIC AS AT & ON MEMBER DEF.

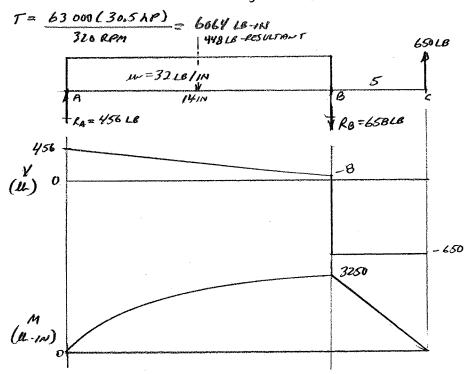
BECAUSE EFFEUT OF KE IS LOCALIZED NEAR HOLE, OF IS LIKELY TO BE MUCH LESS NEAR OUTSIDE SURFACES WHEREOF IS MAXIMUM.

ASSUME OC = - PF = (-116.5 Ren)(1800 N/RN) =-63.1 MPW NEAR OUTSIDE EDGE (100-30)(25) mm²) ABOVE F.

COMBINED STRESS - TENSIUN - BELUW F.

COMBINED STRESS - COMPRESSION - ABOVE F.

10-54 SHAFT: POWER = 30.5 KP; M = 320 RPM



MAXIMUM BENDING AND TORSION OCCUR NEAR B.
USE EQUIVMENT TURQUE METHOD, EQ (0-8).
MAX STRESS OCCURS AT STEP IN 1000 IN DIA. SHAFT

$$\frac{2P = \frac{HD^{3}}{16} = \frac{H(10M)^{3}}{16} = 0.196/N^{3}$$

$$\frac{\Delta 1 - 9}{16} = 0.03; \frac{D}{10} = \frac{1.25}{1.0} = 1.25; K_{EBEND} = 240; K_{TORS} = 1.77$$

$$Te = \sqrt{(K_{EB}M)^{2} + (K_{ET}T)^{2}} = \sqrt{(E_{1}40(3256))^{2} + (I_{1}.77(6064))^{2}} = \frac{13268(B-1N)}{12}$$

$$T_{\text{MAX}} = \frac{Te}{2p} = \frac{13\,Z68\,LB \cdot IN}{0.196\,IN^3} = 67\,694\,Psi$$

SPECIFY AISI 1010 OQT 1160 SY=552KSi, 24% ELOWAATION

OTHER STEELS COULD BE USED WITH SY > 542 KSi AND

Grood DUCTILITY.

FIND STRESS ON ELEMENTS M AND N, P= 450 N 10-55 FORCE P ACTS 18 mm to RIGHT OF CENTERLINE AND 8mm ABOVE CL. ATM:

AXIAL STRESS =
$$\frac{P}{A} = \frac{450 \text{ N}}{(20)(28) \text{ mm}^2} = 0.804 \text{ MPa} \text{ TENSION}$$

BENDING MOMENT: M, = (400 N)(8 Nm) = 3600 Nimm
$$S = \frac{b L^2}{6} = \frac{(20)(28)^2}{6} = 26/3 \text{ mm}^3$$

$$\sigma_{M, =} \frac{M_1}{S} = \frac{3600 N \cdot mm}{26/3 \text{ mm}^3} = L377 \text{ mPs} \quad \text{TENSION AT M}.$$

AT N:

AXIAL STRESS = 0.804 MPA AS AT M. (TENSION)

BENDING MOMENT!
$$M_2 = (50N)(18mm) = 8/00N \cdot mm$$

$$S = \frac{h(6)^2}{6} \frac{(28)(20)^2}{6} - 1867 mm^3$$

$$O_{M_2} = \frac{M_2}{8} = \frac{8100 \, N \cdot mm}{1867 \, mm^3} = 4.339 \, mPa$$

COMPRESSION AT N.

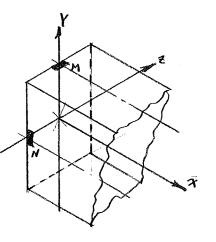
 $O_{N_{TOTAL}} = 0.864 - 4.339 = -3.535 \, mPa$

COMPRESSION AT N.

ELEMENT M IS ON NEUTRAL AXIS

FOR BENDING ABOUTY-AXIS.

ELEMENTN IS ON NEUTRALAXIS FOR BENDING ABOUT Z-AXIS



Combined Stresses - Mohr's Circle

NOTE: The complete solutions for problems 10-56 – 10-105 require the construction of the complete Mohr's circle and the drawing of the principal stress element and the maximum shear stress element. Listed below are the significant numerical results. Following the list are representative examples of the complete solutions. Note that the problems fall into groups of similar forms as described below.

- A. Problems 10-56 to 10-59: The x-axis on the Mohr's circle lies in the *first quadrant*.

 Problems 10-60 to 10-63: The x-axis on the Mohr's circle lies in the *second quadrant*.

 Problems 10-64 to 10-67: The x-axis on the Mohr's circle lies in the *third quadrant*.

 Problems 10-68 to 10-71: The x-axis on the Mohr's circle lies in the *fourth quadrant*.

 Problems 10-72 to 10-79: The x-axis on the Mohr's circle could lie in the *any quadrant*.

 Problems 10-80 to 10-83: The x-axis on the Mohr's circle lies *along the original X-axis* and the *principal stresses are the same as the normal stresses on the given element*.
- B. Problems 10-84 to 10-95: The Mohr's circle from the given data results in both principal stresses having the same sign. For this class of problems, the supplementary circle is drawn using the procedures discussed in Section 10-11 of the text. The results include three principal stresses where $\sigma_1 > \sigma_2 > \sigma_3$. Also, the maximum shear stress is found from the radius of the circle containing σ_1 and σ_3 and is equal to $\sigma_1/2$ or $\sigma_3/2$ whichever has the greatest magnitude. Angles of rotation of the resulting elements are not requested.
- C. Problems 10-96 to 10-105: The Mohr's circles from earlier problems are used to find the stress condition on the element at some specified angle of rotation. The listed results include the two normal stresses and the shear stress on the specified element.

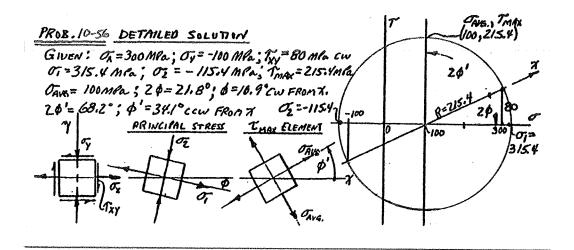
Combined Uniaxial Normal and Shear Stresses

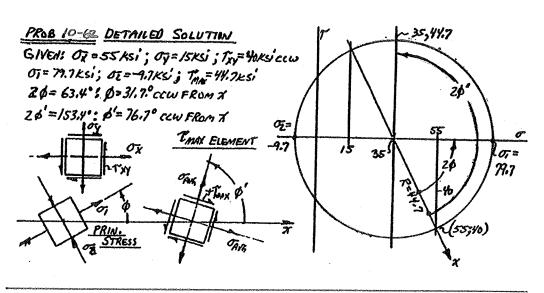
Problems 10-106 to 10-109: These use the same data as Problems 10-72 to 10-75 and each has a given uniaxial normal stress, σ_x , and a shear stress, τ_{xy} . For this special case, Equation 10-2 can be used to compute the maximum shear stress directly. The solution method is similar to that used in Problems 10-21 to 10-28.

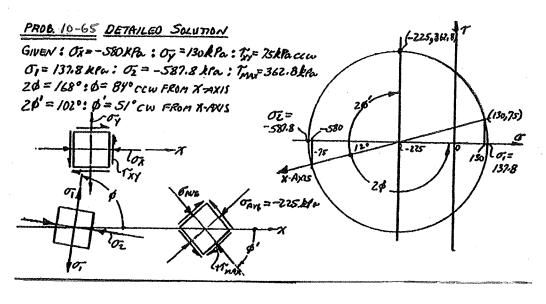
$$\tau_{\text{max}} = \sqrt{(\sigma_{\text{x}}/2)^2 + \tau_{\text{xy}}^2}$$
 (Equation 10-2)

CHAPTER 10 - PROBLEMS 10-56 TO 10-83

Prob.	. 01	doday (Doverno	0 2	o-eo-go epen	(deg)	₹max	DLP (TIP 412-122-1	Oavg	laide (Ulthorages) descript	e' (deg)) 10 100-100-100
10-56	315.4	MPa	-115.4	MPa	10.9	cw	215.4	MPa	100.0	MPa	34.1	CCW
10-57	255.2	MPa	-55.2	MPa	7.5	CW	155.2	MPa	100.0	MPa	37.5	ccw
10-58	110.0	MPa	-40.0	MPa	26.6	CW	75.0	MPa	35.0	MPa	18.4	ccw
10-59	202.1	MPa	-42.1	MPa	27.5	cw	122.1	MPa	80.0	MPa	17.5	ccw
10-60	23.5	Ksi	-8.5	Ksi	19.3	ccw	16.0	ksi	7.5	ksi	64.3	CCW
10-61	42.8	ksi	-29.8	Ksi	14.9	ccw	36.3	Ksi	6.5	Ksi	59.9	CCM
10-62	79.7	ksi	-9.7	Ksi	31.7	CCW	44.7	Ksi	. 35.0	Ksi	76.7	CCW
10-63	36.6	Ksi	-54.6	Ksi	13.0	CCW	45.6	Ksi	-9.0	ksi	58.0	CCM
10-64	677.6	kPa	-977.6	KPa	77.5	CCW	827.6	кРа	-150.0	kPa	57.5	cω
10-65	137.8	kPa	-587.8	KPa	84.0	CCW	362.8	KPa	-225.0	KPa	51.0	εw
10-66	327.0	kPa	-1202.0	KPa	60.9	CCW	764.5	KPa	-437.5	kPa	74.1	CW
10-67	79.9	KPa	-354.9	KPa	74.8	CCW	217.4	kPa	-137.5	kPa	60.2	cw
10-68	570.0	psi	-2070.0	psi	71.3	CM	1320.0	psi	-750.0	psi	26.3	cw
10-69	1676.1	psi	-6676.1	psi	81.7	cw	4176.1	psi	-2500.0	psi	36.7	CW
10-70	4180.0	psi	-5180.0	psi	71.6	CW	4680.0	psi	-500.0	psi	26.6	cw '
10-71	8600.7	psi	~150.7	psi	89.5	cw	4375.7	psi	4225.0	psi	44.5	cw
10-72	360.2	MPa	-100.2	MPa	27.8	ccw	230.2	MPa	130.0	MPa	72.8	ccw
10-73	1827.1	kPa	-377.1	kPa	24.4	cw	1102.1	KPa	725.0	кРа	20.6	CCM
10-74	23.9	ksi	-1.9	Ksi	15.9	cw	12.9	ksi	11.0	Ksi	29.1	CCM
10-75	7971.2	psi	-1221.2	psi	21.4	CCW	4596.2	psi	3375.0	psi	66.4	CCM
10-76	4.4	Ksi	-32.4	Ksi	20.3	cw	18.4	Ksi	-14.0	Ksi	24.7	CCM
10-77	527.6	MPa	-87.6	MPa	67.8	CW	307.6	MPa	220.0	MPa	22.8	CW
10-78	321.0	MPa	-61.0	MPa	66.4	CCM	191.0	MPa	130.0	MPa	68.6	CM
10-79	344.5	KPa	-1904.5	KPa	23.0	CEM	1124.5	kPa	-780.0	kPa	68.0	ccw
10-80	225.0	MPa	-85.0	MPa	0.0		155.0	MPa	70.0	MPa	45.0	ccw
10-81	6250.0	psi	-875.0	psi	0.0		3562.5	psi	2687.5	psi	45.0	CCW
10-82	775.0	KPa	-145.0	kPa	0.0		460.0	KPa	315.0	KPa	45.0	ccw
10-83	38.6	Ksi	-13.4	ƙsi	0.0		26.0	ksi	12.6	Ksi	45.0	CCM







CHAPTER 10 - PROBLEMS 10-84 TO 10-95

Prob. No.	o g	°2	0 3	Tmax
10-84	328.1 MP	71.9 MPa	0.0 MPa	164.0 MPa
10-85	264.0 MPa	136.0 MPa	0.0 MPa	132.0 MPa
10-86	214.5 MPa	75.5 MPa	0.0 MPa	107.2 MPa
10-87	161.1 MPa	68.9 MPa	0.0 MPa	80.5 MPa
10-88	35.0 Ksi	10.0 ksi	0.0 ksi	17.5 Ksi
10-89	41.8 Ksi	21.2 Ksi	0.0 Ksi	20.9 ksi
10-90	55.6 ksi	14.4 ksi	0.0 Ksi	27.8 Ksi
10-91	62.9 Ksi	19.1 ksi	0.0 ksi	31.5 Ksi
10-92	0.0 KPa	-307.9 kPa	-867.1 KPa	433.5 kPa
10-93	0.0 kPa	-37.5 KPa	-337.5 KPa	168.8 KPa
10-94	0.0 psi	-295.7 psi	-1804.3 psi	902.1 psi
10-95	0.0 psi	-2167.6 psi	-6832.4 psi	3416.2 psi

CHAPTER 10 - PROBLEMS 10-96 TO 10-105

Pro No	м	φ _A ,	⁷ A	alouphous a tha langul to
10-96	130.7 MPa	69.3 MPa	213.2 MPa	cw .
10-97	269.3 MPa	-69.3 MPa	133.2 MPa	ccw
10-98	-37.9 MPa	197.9 MPa	31.6 MPa	ccw
10-99	19.1 Ksi	-6.1 Ksi	34.0 Ksi	EEW
10-100	3.6 Ksi	-21.6 Ksi	43.9 Ksi	cw
10-101	-300.0 KPa	-150.0 KPa	355.0 KPa	E₩
10-102	-2010.3 psi	510.3 psi	392.6 psi	cw
10-103	-765.5 psi	-234.5 psi	4672.5 psi	CM
10-104	8363.5 psi	86.5 psi	1421.2 psi	CŴ
10-105	894.8 KPa	555.2 KPa	1088.9 kPa	CCM

CHAPTER 10 – PROBLEMS 10-106 TO 10-109

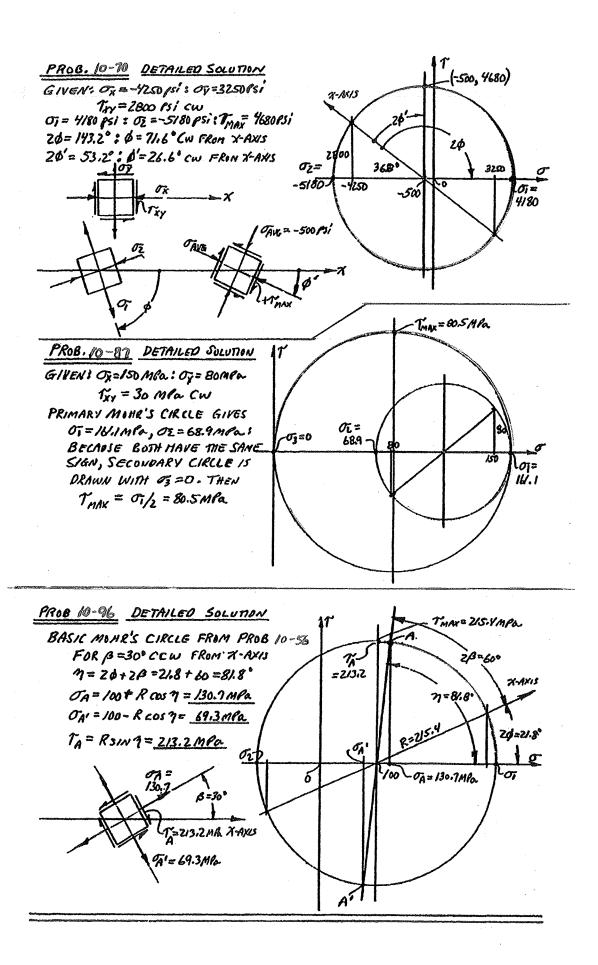
10-106 $\tau_{\text{MAX}} = \sqrt{(\sigma_{\text{X}}/2)^2 + (\tau_{\text{XY}})^2} = \sqrt{(260/2)^2 + (190)^2} = 230.2 \text{ MPa}$

Using a similar technique:

10-107 $\tau_{MAX} = 1102 \text{ kPa}$

10-108 12.9 ksi

10-109 <u>4596 psi</u>



Refer to Section 10-12 for method. Input data in shaded elements

Aluminum 6061-T6

Material Properties SI Metric Units

Modulus of Elasticity 69.0 x 10⁹ Pa

Poisson's Ratio 0.33

Rectangular [0, 45, 90 degree] Rosette Data [Uses Equations 10-22 to 10-24]

Problem 10-110

Strain from Gage 1 1480 x10⁻⁶ m/m Strain from Gage 2 165 x10⁻⁶ m/m

Strain from Gage 3 428 x10⁻⁶ m/m

Results:

Max Principal Strain 1902 x10⁻⁶ m/m

Min Principal Strain 6 >

6 x10⁻⁶ m/m

Angle β -28.2 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 147 Mpa

Min Principal Stress 49.1 Mpa

Max Shear Strain 1897 radians [Dimensionless]

Max Shear Stress 49.2 MPa [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign [Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 73.7 MPa

Delta [0, 60,120 degree] Rosette Data [Uses Equations 10-25 to 10-27]

Problem 10-118

Strain from Gage 1 1480 x10⁻⁶ m/m Strain from Gage 2 165 x10⁻⁶ m/m

Strain from Gage 3 428 x10⁻⁶ m/m

Results:

Max Principal Strain 1494 x10⁻⁶ m/m

Min Principal Strain -112 x10⁻⁶ m/m

Angle β -5.4 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 113 Mpa Min Principal Stress 29.5 MPa

Max Shear Strain 1607 radians [Dimensionless]

Max Shear Stress 41.7 MPa [in plane of initial element]

Only when Max and Min principal stresses have the same sign
[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 56.4 MPa

SPREADSHEET FOR COMPUTING PRINCIPAL STRAINS AND STRESSES FROM STRAIN GAGE ROSETTE OUTPUT DATA Refer to Section 10-12 for method. Input data in shaded elements Aluminum 7075-T6 SI Metric Units **Material Properties** Modulus of Elasticity 71.7 x 109 Pa Poisson's Ratio 0.33 Rectangular [0, 45, 90 degree] Rosette Data [Uses Equations 10-22 to 10-24] Problem 10-111 Strain from Gage 1 853 x10⁻⁶ m/m 406 x10⁻⁶ m/m Strain from Gage 2 Strain from Gage 3 641 x10⁻⁶ m/m Results: Max Principal Strain 1104 x10⁻⁶ m/m 390 x10⁻⁶ m/m Min Principal Strain Angle β -36.4 degrees [From the axis of gage 1 to the nearer principal axis] **Max Principal Stress** 99.2 Mpa Min Principal Stress 60.7 Mpa 714 x 10⁻⁶ radians [Dimensionless] Max Shear Strain 19.3 MPa [in plane of initial element] Max Shear Stress ***Only when Max and Min Principal Stresses have the same sign*** [Assuming stress = 0 perpendicular to plane of initial element] True Max Shear Stress 49.6 MPa Delta [0, 60,120 degree] Rosette Data [Uses Equations 10-25 to 10-27] Problem 10-119 853 x10⁻⁶ m/m Strain from Gage 1 406 x10⁻⁶ m/m Strain from Gage 2 641 x10⁻⁶ m/m Strain from Gage 3 Results: 892 x10⁻⁶ m/m Max Principal Strain 375 x10⁻⁶ m/m Min Principal Strain

Min Principal Strain 3/5 x10 m/m

Angle β -15.9 degrees
[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 81.7 Mpa
Min Principal Stress 53.9 MPa

Max Shear Strain 516 x 10⁻⁶ radians [Dimensionless]

Max Shear Stress 13.9 MPa [in plane of initial element]

Only when Max and Min principal stresses have the same sign

[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 40.8 MPa

Refer to Section 10-12 for method.

Input data in shaded elements

AISI 1040 cold drawn steel

Material Properties SI Metric Units

Modulus of Elasticity 207.0 x 109 Pa

Poisson's Ratio 0.29

Rectangular [0, 45, 90 degree] Rosette Data [Uses Equations 10-22 to 10-24]

Problem 10-112

Strain from Gage 1 389 x10⁻⁶ m/m Strain from Gage 2 737 x10⁻⁶ m/m

Strain from Gage 3 -290 x10⁻⁶ m/m

Results:

Max Principal Strain 816 x10⁻⁶ m/m Min Principal Strain -717 x10⁻⁶ m/m

Angle β 31.9 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 137.5 Mpa Min Principal Stress -108.6 Mpa

Max Shear Strain 1534 radians [Dimensionless]

Max Shear Stress 123.0 MPa [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign

[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 68.7 MPa

Delta [0, 60,120 degree] Rosette Data [Uses Equations 10-25 to 10-27]

Problem 10-120

Strain from Gage 1 389 x10⁻⁶ m/m Strain from Gage 2 737 x10⁻⁶ m/m Strain from Gage 3 -290 x10⁻⁶ m/m

Results:

Max Principal Strain

Min Principal Strain

882 x10⁻⁶ m/m

-324 x10⁻⁶ m/m

Angle β 39.7 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 178.0 Mpa Min Principal Stress -15.5 MPa

Max Shear Strain 1206 radians [Dimensionless]

Max Shear Stress 96.8 MPa [in plane of initial element]

Only when Max and Min principal stresses have the same sign
[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 89.0 MPa

Refer to Section 10-12 for method.

Input data in shaded elements

AISI 4140 OQT 900 steel

Material Properties SI Metric Units

Modulus of Elasticity 207.0 x 109 Pa

Poisson's Ratio 0.29

Rectangular [0, 45, 90 degree] Rosette Data [Uses Equations 10-22 to 10-24]

Problem 10-113

Strain from Gage 1 925 x10⁶ m/m Strain from Gage 2 631 x10⁶ m/m

Strain from Gage 3 552 x10⁻⁶ m/m

Results:

Max Principal Strain 2121 x10⁻⁶ m/m

Min Principal Strain -644 x10⁻⁶ m/m

Angle β -41.1 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 437.1 Mpa Min Principal Stress -6.5 Mpa

Max Shear Strain 2764 radians [Dimensionless]

Max Shear Stress 221.8 MPa [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign
[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 218.5 MPa

Delta [0, 60,120 degree] Rosette Data [Uses Equations 10-25 to 10-27]

Problem 10-121

Strain from Gage 1 925 x10⁻⁶ m/m Strain from Gage 2 -631 x10⁻⁶ m/m

Strain from Gage 3 552 x10⁻⁶ m/m

Results:

Max Principal Strain 1220 x10⁻⁶ m/m

Min Principal Strain -656 x10⁻⁶ m/m

Angle β -23.4 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 232.7 Mpa

Min Principal Stress -68.3 MPa

Max Shear Strain 1876 radians [Dimensionless]

Max Shear Stress 150.5 MPa [in plane of initial element]

Only when Max and Min principal stresses have the same sign

[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 116.4 MPa

Refer to Section 10-12 for method.

Input data in shaded elements

Copper C14500 hard

Material Properties U.S. Customary Unit System

Modulus of Elasticity 17.0 x 10⁶ psi

Poisson's Ratio 0.33

Rectangular [0, 45, 90 degree] Rosette Data [Uses Equations 10-22 to 10-24]

Problem 10-114

Strain from Gage 1 169 x10⁻⁶ in/in Strain from Gage 2 -266 x10⁻⁶ in/in Strain from Gage 3 543 x10⁻⁶ in/in

Results:

Max Principal Strain 1006 x10⁻⁶ in/in
Min Principal Strain -294 x10⁻⁶ in/in

Angle β 36.6 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 17335 psi Min Principal Stress 731 psi

Max Shear Strain 1299 radians [Dimensionless]

Max Shear Stress 8302 psi [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign
[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 8667 psi

Delta [0, 60,120 degree] Rosette Data [Uses Equations 10-25 to 10-27]

Problem 10-122

Strain from Gage 1 169 x10⁻⁶ in/in Strain from Gage 2 -266 x10⁻⁶ in/in Strain from Gage 3 543 x10⁻⁶ in/in

Resuits:

Max Principal Strain 616 x10⁻⁶ in/in
Min Principal Strain -319 x10⁻⁶ in/in

Angle β -43.8 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 9748 psi Min Principal Stress -2204 psi

Max Shear Strain 935 radians [Dimensionless]

Max Shear Stress 5976 psi [in plane of initial element]

Only when Max and Min principal stresses have the same sign [Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 4874 psi

Refer to Section 10-12 for method.
Input data in shaded elements

Titanium Ti-6Al-4V, aged

Material Properties U.S. Customary Unit System

Modulus of Elasticity 16.5 x 10⁸ psi

Poisson's Ratio 0.3

Rectangular [0, 45, 90 degree] Rosette Data [Uses Equations 10-22 to 10-24]

Problem 10-115

Strain from Gage 1 775 x10⁻⁸ in/in Strain from Gage 2 369 x10⁻⁶ in/in Strain from Gage 3 -318 x10⁻⁶ in/in

Results:

Max Principal Strain 793 x10⁻⁶ in/in
Min Principal Strain -336 x10⁻⁶ in/in

Angle β 7.2 degrees

Burne Burner - British sa

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 12548 psi Min Principal Stress -1776 psi

Max Shear Strain 1129 radians [Dimensionless]

Max Shear Stress 7162 psi [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign
[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 6274 psi

Delta [0, 60,120 degree] Rosette Data [Uses Equations 10-25 to 10-27]

Problem 10-123

Strain from Gage 1 775 x10⁻⁶ in/in Strain from Gage 2 369 x10⁻⁶ in/in Strain from Gage 3 -318 x10⁻⁶ in/in

Results:

Max Principal Strain 913 x10⁻⁶ in/in
Min Principal Strain -363 x10⁻⁶ in/in

Angle β 19.2 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 14587 psi Min Principal Stress -1607 psi

Max Shear Strain 1276 radians [Dimensionless]

Max Shear Stress 8097 psi [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign
[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 7294 psi

Refer to Section 10-12 for method.

Input data in shaded elements

Ductile Iron, ASTM A536, 80-55-6

Material Properties

U.S. Customary Unit System

Modulus of Elasticity

24.0 x 10⁶ psi

Poisson's Ratio

0.27

Rectangular [0, 45, 90 degree] Rosette Data [Uses Equations 10-22 to 10-24]

Problem 10-116

Strain from Gage 1 389 x10⁻⁶ in/in 737 x10⁻⁶ in/in Strain from Gage 2 Strain from Gage 3 -290 x10⁻⁶ in/in

Results:

Max Principal Strain

816 x10⁻⁶ in/in

Min Principal Strain -717 x10⁻⁶ in/in

Angle β

31.9 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 16117 psi

Min Principal Stress -12863 psi

Max Shear Strain 1534 radians [Dimensionless]

Max Shear Stress 14490 psi [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign [Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 8059 psi

Delta [0, 60,120 degree] Rosette Data [Uses Equations 10-25 to 10-27]

Problem 10-124

Strain from Gage 1 389 x10⁻⁶ in/in 737 x10⁻⁶ in/in Strain from Gage 2

Strain from Gage 3 -290 x10⁻⁶ in/in

Results:

Max Principal Strain

882 x10⁻⁶ in/in

Min Principal Strain

-324 x10⁻⁶ in/in

Angle β

39.7 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 20559 psi

Min Principal Stress -2236 psi

Max Shear Strain 1206 radians [Dimensionless]

Max Shear Stress 11397 psi [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign [Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 10280 psi

Refer to Section 10-12 for method.

Input data in shaded elements

Stainless Steel, AISI 501 OQT 1000

Material Properties U.S. Customary Unit System

Modulus of Elasticity 29.0 x 10⁶ psi

Poisson's Ratio 0.30

Rectangular [0, 45, 90 degree] Rosette Data [Uses Equations 10-22 to 10-24]

Problem 10-117

Strain from Gage 1 1532 x10⁻⁶ in/in

Strain from Gage 2 -228 x10⁻⁶ in/in

Strain from Gage 3 893 x10⁻⁶ in/in

Results:

Max Principal Strain 2688 x10⁻⁶ in/in

Min Principal Strain -263 x10⁻⁶ in/in

Angle β -38.7 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 83147 psi

Very high stress: s_v = 135 ksi

Min Principal Stress 17317 psi

N = 1.62 Low

Max Shear Strain 2951 x 10⁻⁶ radians [Dimensionless]

Max Shear Stress 32915 psi [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign

[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 41574 psi

Delta [0, 60,120 degree] Rosette Data [Uses Equations 10-25 to 10-27]

Problem 10-125

Strain from Gage 1 1532 x10⁻⁶ in/in

Strain from Gage 2 -228 x10⁻⁶ in/in

Strain from Gage 3 893 x10⁻⁶ in/in

Results:

Max Principal Strain 1761 x10⁻⁶ in/in

Min Principal Strain -296 x10⁻⁶ in/in

Angle β -19.5 degrees

[From the axis of gage 1 to the nearer principal axis]

Max Principal Stress 53289 psi

Min Principal Stress 7390 psi

Max Shear Strain 2058 x 10⁻⁶ radians [Dimensionless]

Max Shear Stress 22949 psi [in plane of initial element]

Only when Max and Min Principal Stresses have the same sign
[Assuming stress = 0 perpendicular to plane of initial element]

True Max Shear Stress 26644 psi

CHAPTER 11 Columns

$$\frac{11-1}{L} \frac{Le}{Lo(14)} = \frac{(lo(160))}{(2014)} = \frac{1}{160} : For Sy = \frac{33}{160}, Ce = \frac{(lo(160))}{100} : Lond (alunn)$$

$$VSE EVLER EO. (bi-4): A = TD_{ij} = T(20)_{ij} = 319 Mmn^{2}$$

$$Pce = \frac{T^{2}EA}{(Le/L)^{2}} = \frac{TT^{2}(2018)^{10}(Mn^{2})(349em^{2})}{(160)^{2}} \cdot \frac{319 Mmn^{2}}{10^{6}mm^{2}} = \frac{25\cdot120^{3}}{10^{6}mm^{2}} = \frac{25\cdot120^{3}}{10^{6}mm^{2}} = \frac{25\cdot120^{3}}{10^{6}mm^{2}} = \frac{25\cdot120^{3}}{10^{6}mm^{2}} = \frac{11\cdot2}{10^{6}mm^{2}} \cdot \frac{11\cdot2}{10^{6}mm^{2}} = \frac{11\cdot3}{10^{6}mm^{2}} \cdot \frac{11\cdot3}{10^{6}m$$

```
11-7 Ann = 12/12 = 3.46 mm; Le/n = 1.0(210)/3.46=60.6
                                          FOR SU= 469MPa-STEEL : Co = 90 - SHORT COLUMN
                                          A=1/2)(25)= 300 mm2
                                             PCR = BOD MM Y 469 N/mm ) [1- 469 x 10 Pa x (60.6) ] = 111 KH
       11-8 FOR A36 STRUCTURAL STEEL: SY = 248MPA - Co = 122; E=200XO3N/mm2
                                           FUR S6 X12.5: 12mm = TY = V1.82 INV = 0.704 IN 225.4 mm/m = 17.9 mm
                                             Le/n = (6.65)(5450)/17.9 = 198 > C_c \cdot LONG : A = 3.67 Los 2 los 4) los 2 lo
     11-9 3IN SCH 40 PIRES / = 1.164 IN: Le/ = (20)(8 FT) (1-10/FT)/1.164IN=173
                                                 Sy=30 Ks/ & Cc = /38-LONG COLUMN & E = 30x/0 Gs; FOR STEEL.
                                                   Pa = PCA = 172EA = 152(30xA6)(2.228) = 73/8 LB/COLVAN
                                                  No. of COLUMNS = TOTAL LUAD = (75 La/F7 - YZOx 40) PT = 8.20-USE 9
    11-10 Ilox 8.6462 /2 min = 1.42 IN x 25.4 mm/1N = 36.1 mm
                                           A= 7.352 IN2 x (25.4)2 mm2/IN2 = 4143 mm = I264 K12.87 (S.E)

Le/n = 1.0 (2800) /36.1 = 726: FOR Sy = 276 MPA ALUM., CE=70 - LONG COLUMN
                                         (E011-186) Pa= 352000(A) = 352000(4743) = 277 RN
       11-11 Le/h = 1400/36.1 = 38.8 - INTERMED. 2(EQ 11-176)
                                             Pa. = A [ 139 - 0.869/6/6] = 4743 mm [139 -0.869(38.8)] N/mm = 499 AN
\frac{11^{-1}2}{SR = KU_{R} = \frac{0.8(12.5FT)(121WFT)}{0.8(12.5FT)(121WFT)} = 142.9} \frac{ASTMA992}{WETHOO}
SR = \frac{0.8(12.5FT)(121WFT)}{0.840W} = 142.9
SR = 4.71 \sqrt{\frac{0.8(12.5FT)(121WFT)}{\sqrt{15}}} = 142.9
SR = 4.71 \sqrt{\frac{15}{5}} = 4.71 \sqrt{\frac{15}{5}
   SCR = 0.8775e = 0.877 \text{ TT } ^2E = 0.877(\text{T}^2)(298/6) = 1/3 - LONG COLUMNS
SCR = 0.8775e = 0.877 \text{ TT } ^2E = 0.877(\text{T}^2)(298/6) = 1/2 29205i
Pa = \frac{Pm}{1.67} = \frac{6ca)(A)}{1.67} = \frac{(12292)(2.91)}{1.67} = 21287 LB
11-13
                                                      I_{XX} = I_{YY} = 4 \left[ 1.23 + 1.44 \left( 5.164 \right)^{2} \right] = 150.5 \text{ in}^{4}
A = 4 \left( 1.44 \text{ in}^{2} \right) = 5.76 \text{ in}^{2} \quad \begin{array}{c} 5 \sqrt{236465} \\ C_{C} = 126 \end{array}
h = \sqrt{I/A} = \sqrt{158.5/5.76} = 5.246 \text{ in}
                                                      Le/2 = (1.0)(18.4 ft) (12 in/ft) / 5.246, = 42.1 < Cc - JOHNSON EQ.
                                                     P_{0} = \frac{P_{CL}}{N} = \frac{(5.76)(36000)}{3} \left[1 - \frac{36000(42.1)^{2}}{477^{4} (29 \times 10^{6})}\right] = 65300 \text{ M}
```

$$L_{XX} = 2.44 \text{ in}$$

$$L_{YY} = 2[1.53 + 2.41 (2.21)^{2}] = 26.6 \text{ in}$$

$$N_{YY} = \sqrt{L/A} = 26.6 / (2.12.41) = 2.35 \text{ in}$$

$$Le = L = 10.5 \text{ fr} (121N/\text{ fr}) = 126 / 10.$$

$$Le/A = 126 / 2.35 = 53.6 (NT.)$$

$$EQ(1-11.6) P_{0} = 2(2.41) [20.2 - 0.126(53.6)] = 64.8 \text{ kips} = 64.800 \text{ lb}$$

14:15

$$F = mq = 1320 kq \cdot 9.8 m/s^{2} = 12950 N = FV$$

$$F_{N} = F/s_{N} = 2950 / \frac{1}{12} \cdot 22.6 = 31110 N$$

$$For 5/50 \times 18.6 : M = \sqrt{\frac{E}{V/A}} = \frac{7}{7.49 \times 10^{3}} / \frac{2360}{2360} = 72.8 mm$$

$$ke/n = 2400 / 7.8 = 134.7 - Long [C_{c} = 126 Fon s_{f} = 36.65]$$

$$P_{C_{n}} = \frac{11^{2} EA}{(134.7)^{2}} = \frac{17^{2} (200 \times 64 / mm^{2})}{(134.7)^{2}} = \frac{17^{2} (200 \times 64 / mm^{2})}{(134.7)^{2}$$

1/-16 / MIN = 0.125 = 0.036 IN : A= 0.25 × 0.125 = 0.03/3 INZ FOR 1040 CD: Sy=82KSi-Ce= 83 : Le 8.40 =233 > Ce - LONG COLUMN $P_{CR} = \frac{\pi^2 E A}{(Le/h)^2} = \frac{\pi^2 (30 \times h^6) (0.03/3)}{(233)^2} = \frac{17/L8}{1}$ N = Per 17/LB = 3,4/ OK $\frac{11+7}{1} \text{ FOR AISI 1/4/ OOT 1300: } S_y = 469MPa : C_c = 95: A = \frac{10^2 \text{ M(12)}^2}{4} = 1/3 \text{ m/m}^2$ $\Lambda = \frac{0}{4} = \frac{12}{4} = 3.0 \text{ m/m} : \frac{Lc}{\Lambda} = \frac{(0.8 \text{ X}/90)}{3.0} = 50.7 < C_C - \text{SHIRT COLUMN}$ PCR = (13 mm²) (469 N/mm²) [1- 469 MPa (50.7)2]= 45.2 KN FOR N=3; Pa = Pca = 45.2 KN = 15.1 KN 11-18 FOR AISI 1020 HR; Sy=48 KSi; Ce 2/05 1 = 0.800 IN = 0.200 IN: LE = 28.5 = 142.5 - LONE: A= 110.02 0.508 IN2 $P_{CR} = \frac{17^{2}EA}{(le IA)^{2}} = \frac{77^{2}(30 \times 10^{6})(0.503)}{(192.5)^{2}} = \frac{7339' LB^{2}}{(1335)} = \frac{7339'}{(1335)} =$ 11-19 ZIN SCH. YO PIPE: 1=0.787 IN : A=1.075 IN 28 FIXED/PHINED - K=0.8 Le (0,8)(HAF)(/218/FT) = 171 : FOR ALSI 1040 HR, Sy =48KS; - Cc = 105 - LONG $P_{CR} = \frac{\pi^2 E A}{(Le/h)^2} = \frac{\pi^2 (30 \times N^4)(1.075)}{(171)^2} = \frac{10914 LB}{10914 LB}$ EACH COLUMN CARRIES 5000 LOS N = PCR = 10914LB = 2.18 -MARGINAL 11-20 LACK OF RESTRAINT AT TOP OF COLUMNS MAKE THEM FREE. FOR FIXED-FREE: Le (20)(14 FT)(12 IN/FT) = 448 - VERY LONG

PCR = \frac{17 \cdot EA}{(\lambda \cdot A)} = \frac{17 \cdot (30x/06)(1.675)}{(448)^2} = \frac{1584L8}{(584L8)} \cdot P_{ACTUAL} = 5000L8 - FAILURE 11-21 1 = 1.25 in/VI2 = 0,36/ : A=(1,25in) = 1,563in2 COLUMNS ARE FIXED-FREE; Le =2/10/=84 /11. Le/2 = BY /0.361 = 233 -LONG ALUMINUM 6061-76; Sy = 40000poi; Cc = 10 Par = IT = A = TT (10×10)(1.563) = 2849 D EACH COLUMN CARRIES 1500 LB N = Par/p = 2849/1500=1.90 -LOW

11-22 ASSUME FIXED-PINNED ENDS: 12MN = 2.00 = 0.577 IN Le = 6.80) (12.75FT) (12.10/FT) = 2/2 : AISI 1040 WOT 1/00; Sy=80KS; -Cc=85 $P_{CR} = \frac{\pi^2 E A}{(L \cdot I_A)^2} = \frac{\pi^2 (30 \times 0.5 \times 0.1 M^2) (6.0 / M^2)}{(2/2)^2} = 39.525 LB$ $N = \frac{\rho_{CR}}{\rho} = \frac{39525}{12.500} = 3.16 \text{ OK}$ THIS IS PROBABLY CONSERVATIVE BECAUSE PIN MAY PROVIDE SOME RESTRAINT AGAINST BUCKLING WITH RESPECT TO VERTICAL AXIS. THUS LE /1 WOULD BE SMALLER; PCR AND N WOULD BE LARGER. ASSUME A LONG COLUMN : EQ.11-5:Le=6.8)(12.75 FT)(121N/FT) =122.1N $\frac{11-24}{ASSUME} LET E = 29 \times 10^{6} 15i FOR STRUCTURAL STEEL: Sy = 36 \times 5i : Cc = 130}{ASSUME COLUMN IS LONG: <math>I_{MIN} = \frac{NPL^{2}}{\Pi^{2}E} = \frac{(4.0)15001211^{2}}{\Pi^{2}(29 \times 0^{6})} = 2.60 \text{ IN}^{4}$ $USE 3 \text{ IN SCH.40: } I = 3.017 \text{ IN}^{4}; \Lambda = 1.164 \text{ IN: } \frac{Le}{\Lambda} = \frac{122}{1.164} = 1.05 < Cc - SHORT$ $P_{0} = \frac{ASy}{N} \left[1 - \frac{Sy fe/\Lambda}{4\Pi^{2}E}\right] = \frac{(2.228 \text{IN}^{2})[3600010]_{10^{2}}}{4(11)^{2}} \left[1 - \frac{(36000)(105)^{2}}{4(11)^{2}(29 \times 0^{6})}\right] = \frac{13.114 \text{ LB}}{OK}$ 14-25 FOR BUCKLING ABOUT Y-X AXIS - FIXED-PINNED : Le=0.8)(12:05FT)(12W/FT)=/22M FOR Y-Y AXIS- FIXEO-FIXED: Le=0.65(12.75)(12) = 99.5 IH: ASSUME LOVE COLUMN $I_{X_{MIN}} = \frac{NPLe^2}{\pi^2 E} = \frac{4(12500)(122)^2}{\pi^2 (/0 \times 10^4)} = 7.54_{IN}^4 - ISX3.700 \text{ BEAM SHAPE REGIO$ IYMIN = 4(12501)(99.5)= 5.02 IN4 - I 7x5.800 REOD \$ 14=1.08 IN Le = 99.5 IN = 92.1: FOR GOW-TE: SY = YOKSI; Cc = 70-LONG COLUAN-OK 11-26 Le=0.8L=0.8(16.5FT)(121N/FT)=1581N:3X3x4 -1=1.111N;A=244 M2 Le/n = 158/1,11 = 142 : FOR ASTM ASOO, GRADEB: Sy = 46KS' - Cc=110-LONG Per = \frac{\pi^2 \in A}{(Le/n)^2} = \frac{\pi^2 (29 \times 0^4)(244)}{(142)^2} = 34 635 LB \cdot R = \frac{\text{Pea}}{N} = \frac{34 635}{2} = 115452B 11-27 Le= 0.8L =0.8U6.5)(12)=1581N: FOR 4x2x 4, RMN=0.77901:A=244 IN2 Le/n = 158/0.779=203: Cc=110 (PROB 11-76) -LONG PCR = \frac{\pi^2(29\times)(Z.94)}{(203)^2} = 16947LB: Pa = \frac{PcR}{N} = \frac{16947}{3} = \frac{5649}{16947} \frac{1}{16947} = \frac{1 11-18 FROM 11-26:Le=158 IN: Sy=36KS; -Ce=130 Ix=Iy=2(I+A) = 2[1.23+1.44C0.6642)] =3.73/1.4 1x=Iy=2(I+A) = 2[1.23+1.44C0.6642)] =3.73/1.4 1x=I/A = \frac{3.73/2.88}{1.138 m.; \frac{Le}{L} = \frac{1.58}{1.138} = 139 - LONG $P_{a} = \frac{R_{R}}{N} = \frac{H^{2}(29 \times 10^{6})(2.68)}{(2)(1.39)2} = \frac{42730 LB}{3} = 14.343 LB}$

11-29 Alsi 1020 HR & Sy =331 MR: C= 105: h=40 = 11.55 mm PIXED-FIXED : Le=0.65 (750) = 488 mm : Le = 488 = 42.2 - SHORT

PCR = A Sy [1- \frac{5y(Le/\lambda)^2}{4\pi^2}] = (2400 mm^2) \frac{331 M/mm^2}{477 \left(207X188/m/m)} = 737 km LET N=3: Pa = Per = 137 KN = 145 KN 11-30 6061-74: Sy=145MPa-Cc = 98: C102 × 2.568, /2, = 16.26 mm Le = 4250 mm = 261 - LONG: A = 954 mm (APRA-10 (SI)) Pa = Pce = #2EA = #2(69×10 1/2mm2)(958 mm2) = 2376 N

NO IMPROVEMENT BECAUSE COLUMN IS STILL LONG AND BULLING LOAD FROM EVLER FORMULA IS INDEPENDENT OF STREATH. E IS THE SAME.

11-32 W12 x65, A=19.11N, Iy=1741N4 /2 MIN = /2 y= \IY/A = \1741N4/19.11N2=3.021N ASTMA9921 Sy=50 000 PSi, E=29×106 PSi $SR = \frac{Le}{R} = \frac{(0.8)(22.5FT)(121N/FT)}{3.02} = 71.5$ SR = 4.71 /E/SV = 4.71/29 ×106/5000 = 1/3 SR < SR + USE EQ 11-10 SCR = [(0.658)] Sy Se= TT2E/SRZ = TT2(29X/06) = 55987PSi d = 50000/55987 = 0.893 Sca = (0.658) 0.893 50000 = 34406 851 Pm = Sca A = 34406LB/102 (19.1102)=657,153LB $P_a = \frac{P_m}{1.67} = \frac{657153}{1.67} = 39350516$

COLUMN ANALYSIS - SUMMARY OF RESULTS OF PROBLEMS 11-33 TO 1143

Ø @	9420 lb	7801 lb	219 lb	3871 lb	75 KN	3.8 KN	
	ග්		Ø	7		o C	
Eqn.	Euler	Johnsor	Euler	Johnsor	Euler	Johnson	3x1/4)
ő D	28260	53403	18656	62613	, 173	281	tube (3x;
N	ന	ო	ന	ო	2.27	က	X6.4
S S	7	တ္ထ	174	တ္တ	134	8	76x76
L.	0.751 in	0.751 in	0.751 in	dom dom dom dom	19.8 mm	28.2 mm	> HSS 76x76x6.4 tube (3x3x1/4)
4	1.97 in ²	1.97 in ²	1.97 in ²	2.44 in ²	1570 mm ²	1570 mm ²	
ပံ	126	126	126	126	126	126	3
Ш		29E06 psi					
'n	36 ksi	36 ksi	36 ks	36 kei	248 MPs	240 1400	240 IVIL A
7	106.2 in	66.6 in	130 G in	106.4 in	2650 mm	2000 11111	
×	0.65	0.80	080	20.0	3 5	3 5	3
- 1	163.2 in	83.2 in	463.2 in	163 2 in	2650 mm	2000 111111	IIIIII OCOZ
2	<u> </u>			 			

ろうりに		>					
\ ! ! !	ers	Listing of compression members only		ص"	2253 lb	750 lb	654 lb
	Problem 11-39 Truss Analysis + Design of Compression Members	Listing of compi		Material	15/16 in ASTM A36	ASTM A36	11/16 in ASTM A36
	gn of Com	ns		Size			11/16 in
	sis + Desi	Example data only. Many possible designs		Shape		Circular	ircular
	s Analy	fany pos	1=3.0	_		25 in	40 in C
	1-39 Trus	ata only. N	tor on load	Member Load	1925 lb	750	650
	Problem 1	Example d	Design factor on load = 3.0	Member	AC	S	빙

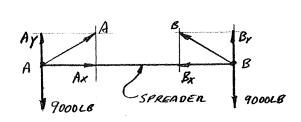
bers	Listing of compression members only		đ _a	5950 lb	5950 lb	3613 lb	2950 lb	2950 Ib
Problem 11-40 Truss Analysis + Design of Compression Members	Listing of com		Material	ASTM A501	ASTM A501	ASTM A501	ASTM A501	ASTM A501
yn of Com	ns Su		Size	2x2x1/4	2x2x1/4	2x2x1/4	2x2x1/4	2x2x1/4
ysis + Desig	Example data only. Many possible designs		7 Shape	120 in Steel tube	Steel tube	154 in Steel tube	120 in Steel tube	4141 lb 120 in Steel tube
s Anal	lany po	= 2.5	7		120 in	154 in	120 in	120 in
1-40 Trus	lata only. N	Design factor on load = 2.5	Foad	4609 lb	3625 lb	1101 lb	3625 lb	4141 lb
Problem 1	Example d	Design fac	Member	AC	၅	盂	Ш	H

	3613 lb	2950 lb	2950 lb	
	ASTM A501	e 2x2x1/4 ASTM A501	ASTM A501	
	2x2x1/4	2x2x1/4	2x2x1/4	
	154 in Steel tube	3625 lb 120 in Steel tube	120 in Steel tube	
	1101 lb	3625 lb	4141 lb	
)	Ш	Щ	H	

Problem 11-41 Truss Analysis + Design of Compression Members

		201				
gn 1ac	tor on load	C.7				
nber	Foad	-	Shape	Size	Material	
Щ	2300 N	.25 m	Square	S mm	Alum. 6061-T6	
20	2597 N	.297 m	Square	mm /	Alum. 6061-T6	
ш	2300 N	.20 m	Square	8 mm	Alum. 6061-T6	2324 N
n Q	550 N	.15 m	Square	5 mm	Alum. 6061-T6	
· 당	800 N	.16 m	Square	e mm	CF 800 N .16 m Square 6 mm Alum 6061-T6	

11-42 The support cables for the sling act at 30° to the horizontal and exert a direct axial compressive force on the spreader as shown below. Assume central loading of a straight column. The horizontal (axial) component of the cable force is 15 588 lb.



$$A_y = B_y = 9000 LB$$

 $A = B = 9000 LB/SIN30' = 18000 LB$
 $A_x = B_x = 18000 LB((as30') = 15588 LB$

Design decision: Use a hollow steel tube made from ASTM A501 structural steel. The column buckling analysis spreadsheet (Figure 14-9) was used to determine that the lightest size with adequate capacity is a 3x3x1/4 hollow steel tube. Other results are summarized below.

 $L = L_e = 96$ in; r = 1.11 in; SR = 86.5; A = 2.44 in²; $s_v = 36\,000$ psi; $E = 29\times10^6$ psi; $C_c = 126$; Use N = 2.5 (design decision); Column is short; Use Johnson formula; $P_{cr} = 67180$ lb; $P_a = 26872$ lb.

11-43 The analysis is similar to Problem 11-42. With the angle of 15°, the axial force on the tube is 33 588 lb. The spreader now must be a HSS 4x4x1/4 steel tube with $A = 3.37 \text{ in}^2$; r = 1.52 in; SR = 63.2; Short column; From the Johnson formula, $P_{cr} = 106 103 \text{ lb}$; $P_a = 42441 \text{ lb}$.

Crooked Columns

For Problems 11-44 to 11-49 loading data were taken from earlier problems as listed in the problem statements. The amount of initial crookedness is given. The Crooked Column Analysis spreadsheet (Figure 11-15) was used to determine the critical buckling load and the allowable load for a design factor of 3.0. The spreadsheet solves Equation 11-19. Results are summarized in the table on the following page.

Eccentrically-Loaded Columns

For Problems 11-50 to 11-58, data from the problem statements were entered into the Eccentric Column Analysis spreadsheet (Figure 11-16). Where the problem asks for the maximum stress and deflection, the design factor N = 1.0 was entered at the lower left column. For design problems, the requested design factor (typically N = 3.0) was entered. Results are summarized in the table on the following page.

Problem 11-59

Straight and crooked column analysis required for the 2-in schedule 40 steel pipe, 156 in long. The spreadsheets in Figures 11-9 (Straight columns) and 11-15 (crooked columns) were used to determine the following results.

- a) Straight pipe: SR = 198; C_c = 126; Long column; P_{cr} = 7831 lb; P_a = 2610 lb. b) Crooked pipe: a = 1.25 in; C_1 in Eqn. 11-19 = -21 766; C_2 = 3.36x10 7 ; Euler buckling load = 7831 lb; $P_a = 1676$ lb.

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CROOKED COLUMN ANALYSIS - SUMMARY OF RESULTS OF PROBLEMS 11-44 to 11-49
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Equation 11-19

C ₂ P _a	9E08 5.71 kN	60.6 3 111 kN -146962 2.61E09 20.6 kN	1E10 122 KN	4E+08 8143 lb	28260 lb -53938 2.23E+08 4505 lb	1.068 173 kN -862416 5.91E+10 75.0 kN	, = 75 KN
ပ်	-56362 2.89E08	-146962 2.6	-761829 7.8	-92180 6.8	-53938 2.23	-862416 5.9	> Iterated to find N for P ₃ = 75 kN
م م	25.06 KN	111 KN	537 KN	41612 lb	28260 lb	8 173 KN	> Iterated t
SR N	ო	60	m m	n	n	8	I
	160	60. 6	77.(143	4	134	
•	314 mm ² 5.00 mm	93.3 300 mm ² 3.46 mm 6	² 36.1 mm	0.841in	0.751 in	19.8 mm	
⋖	314 mm ²	300 mm ²	4743 mm	2.96 in ²	1.97 in ²	126 1570 mm ²	
ပ	6 6 6	93.3	70.2	107	126	126	
ш	207 GPa	207 GPa	69 GPa	29E06 psi	29E06 psi	200 GPa	
^s	331 MPa	469 MPa	276 MPa		36 ksi	248 MPa	
7	800 mm	210 mm	2800 mm	120 in	106.1 in	2650 mm	
×	1.00	1.00	5.	0.80	0.65	9.	
-1	800 mm	210 mm	2800 mm	150 in	163.2 in	ŧν	
ø	4.00 mm	1.60 mm	14.0 mm	0.75 in	1.25 in	32.0 mm	
Prob.	11-44	1.45	1146	11-47	11-48	4.40	

ECCENTRICALLY LOADED COLUMN ANALYSIS - SUMMARY OF RESULTS OF PROBLEMS 11-50 to 11-58

Value of N in Eqn. 11-21 set equal to 1.0 to find maximum stress in column.

ecant for:	SR N Stress Defl. Stress Y max	116 1 1.1527 1.1527 3456 psi 0.092 in	a 207 GPa 111 1438 mm² 29.55 mm 108 1 1.1716 1.1716 211 MPa 25.8 mm	1.1511 6687 psi 0.045 in
Value of secant for:	Stress	1.1527	1.1716	1.1511
	2	4	-	has
	SR	116	108	204
	3	97 1.563 in ² 0.361 in	29.55 mm	0.072 in
	⋖	1.563 in ²	1438 mm ²	0.063 in ²
	ပံ	97	£	118
	ш	10E06 psi	207 GPa	40.0 ksi 28E06 psi
	'n	21.0 ksi	331 MPa	40.0 ksi
	J	42.0 in	3200 mm	14.75 in
•	×	1.00	00.	5 .
¥	-1	42.0 in	3200 mm	11-52 0.30 in 14.75 in 1.00 14.75 in
	ø	11-50 0.60 in	11-51 150 mm	0.30 in
	Prob.	11-50	47-	11-52

Problems 11-53 to 11-58 Eccentrically Loaded Column Analysis

Value of N = 3 used to evaluate safety

	y max	0.035 in		0.006 in	
	SR N Stress Defl. Redd sy Y max	1.0703 103 ksi 0.035 in	fe.	3 48.4 ksi	
secant r	Defi.	1.070	hat is sa	1.0123	am.
Value of secant for:	Stress	26.3 3 1.239	eel tube ti	1.038	e press n
	Z	ന	st st	ო	to th
	SR	26.3	d lighte	0.4	oarallel
	7	1.51 in	ned to fin	2.85 in	e flat and l
	ব	3.37 in ²	is redesig	5.24 in ²	if ends ar
	ပ	107	, Prop	107	safer
	Ш	50.0 ksi 29E06 psi 107 3.37 in² 1.51 in	greater than given s_{y} . Prop is redesigned to find lightest steel tube that is safe.	50.0 ksi 29E06 psi 107 5.24 in ² 2.85 in 14.0 3 1.038 1.0123 48.4 ksi 0.006 in	Square steel tube 8x4x1/4. Assumed pinned ends. Would be safer if ends are flat and parallel to the press ram.
	Sy	50.0 ksi	is greater th	50.0 ksi	l pinned enc
	L	40.0 in	redds,	40.0 in	Assumed
	×	8	pecausi	 8	X4X114.
	7	40.0 in	Design is not safe because reqd sy is	11-53a 0.50 in 40.0 in 1.00 40.0 in	feel tube 8
	ø	11-53 0.50 in	Design is	0.50 in	Square S
	Prob.	11-53		11-53a	

0.90 in 72 in 1.00 72.0 in 90.0 ksi 30E06 psi 81.1 1.28 in² 0.231 in 312 1 1.4289 1.4289 8319 psi 0.386 in This is the maximum stress in the column for an assumed design factor of N = 1.0. 90.0 ksi 30E06 psi 81.1 1.28 in² 0.231 in 312 3 5.2212 1.4289 84.9 ksi 0.386 in 11-54a 0.90 in

This gives the required yield strength (84.9 ksi) of the material for N = 3. Specify AISI 1040 WQT 900 steel; $s_y = 90.0 \text{ ksi}$. 72.0 in 0.1 72 in 11-54b

Problems 11-53 to 11-58 Eccentrically Loaded Column Analysis (Continued) Value of N = 3 used to evaluate safety

Prob. e L K 11-55 0.467 in 112 in 1.0 The design is not safe u The eccentricity is the d	Value of secant for:	L _e S _y E C _c A r SR N Stress Deft. Redd S _y y _{max}	3.0 ksi 29E06 psi 126 2.64 in ² 0.486 in	sing a desired value of $N=3$. Required yield strength is over 2.5 times higher that given yield strength.	istance from the centoidal axis and the middle of the flance width. $C5x9$ Steel channel: $c = 1.412$ in
e L K 0.467 in 112 in 1.00 The design is not safe usi The eccentricity is the dis		S	36.0 ksi 29E	$Value\ of\ N=3.$	he centoidal ax
•		7	112 in	g a desired	ance from t
•		×	7.00	afe usin	the dist
•		_	112 in	ın is not s	ntricity is
•		0	0.467 in	The desig	The eccer
		Prob.	11-55	· -	•

0.225 in 1.0749 46.0 ksi The load for these data is 19,263 lb, found by iterating Equation 14-20 using the spreadsheet until the required yield strength 1.2576 n 1.41 in 71.5 46.0 ksi 29E06 psi 112 6.02 in² became less than the given 46,000 psi. HSS 4x4x1/2 Steel tube; c = 2.00 in 100.8 0.80 126 in 11-56 3.00 in

0.233 in 40.0 ksi 10E06 psi 70.2 0.600 in² 0.433 in 92.4 3 1.5127 1.1333 39.1 ksi The load for these data is 675 lb, found by iterating Equation 11-21 using the spreadsheet until the required yield strength became less than the given 40,000 psi. 11-57a 1.75 in 40.0 in 1.00 40.0 in

The analysis was done assuming that the loading in the plane of the drawing was critical. IT IS NOT! See the analysis below. 11-575 Buckling about the thickness of the bar is now checked assuming that the load is centrally applied.

347 0.1154 in The allowable load for buckling about this axis is only 164 lb. This is the limiting load. 40.0 in 1.00 40.0 in 40.0 ksi 10E06 psi 70.2 0.60 in² Column analysis spreadsheet is used to determine allowable load for N = 3,

ማ

1.4512 1.1205 389 MPa 2.41 mm The design is safe because the required yield strength is less than the actual yield strength of the given material. 20 mm 750 mm 1.00 750 mm 931 MPa 200 GPa 65.1 314 mm² 7.29 mm 103 3 11-58

Problem 11-59 has two-parts. The first analysis is for a straight pipe. The second analysis is for the crooked pipe.

ç.	9	5	(Pr
ø.	2610 lb	1676	1-59(a
ບັ	,	-21766 3.37E07 1676 lb	Problem 1
ပ်	•	-21766	Equation 11-4 used for Problem 11-59(a)
م م	7831	7831	ation 114
Z	ო	ന	Equ
SRN	198 3	198	
b	0.787 in	0.787 in	ðď.
4	1.075 in ²	1.075 in ²	e is crook
ပ	126	126	he pip
ш	36.0 ksi 29E06 psi 126 1.075 in ² 0.787 in	36.0 ksi 29E06 psi 126 1.075 in ² 0.787 in 198 3	10 lb to 1676 lb when the pipe is crooked.
S	36.0 ksi		610 lb to 16
Le	156 in	156 in	es from 2
×	1.00 15	 8	decreas
T	156 in	156 in 1.00	The allowable load decreases from 2610
ø	0	1-59b 1.25 in	Гће аво
Prob.	11-59a	11-596	

Equation 11-19 used for Problem 11-59(b)

CHAPTER 12 Pressure Vessels

12-6 Da = Di +t = 80+3.5=83.5 MM; Da/6= 83.5/3,5= 23.9 THIN 0= PD= (185 MPa (83.5 mm) - 34.0 MPa 2t 2(3.5 mm) 12-7 ASSUME THIN WALL & OJ = SY = 565, MPM = 141,3 MPM = PD t = PD = (1.7 MPM \(\frac{1}{300 mm} \) = 1.80 mm 2 03 2 (191.3 MPM) = 1.80 mm Dm = Do = 300 - 1.81 = 298.2: 0m/t=298.4; 80 = 164-V5RY THIN 12-8 t= PD = (15.2 MA)(250 mm) = 13.45 mm

205 2(141-3/9/0)

Dm = Do-t = 250-13.45 = 236.5 mm = Dm/c= 236.5 /3.45 = 17.6 - THICK WALL USE EQ. FOR ON FROM TABLE 12-1. TRY E= 14.0 man Di= Do-2t= 250-2(14)= 222 mm; a=111 mm, b=125 mm. OK FOR Od = 141.3 MPL BUT SOMEWHAT LOW. FOR t= 13.0 mm; Di=224 mm; a= 1/2 mm, b=/25 mm 0 = 139.0MPa OK USE t=/3.0 mm 12-9 Dm = Do -t = 450 - 2.20 = 447.8 mm : 07/2=4428/220 = 204 -THIN 0= fDm = (250×103Pa)(447.8 mm) = 76.3 mPa N = SY = 290 MPa = 3,80 1270 ASSUME THIN WALL: 05=SV/4=44/4=103MPa=PO t= PO (750 XIN Pa) (1800 Mmm) = 6.55mm LETE=7-0 mm Dm = Do-t= 1800 - 10 = 1793 man 8 Da/t = 1793/10= 25 6 VERY THIN Dm= Do-t= 250 - 18 = 232 mm : Dm/t = 232/18 = 12.9 < 20 - THICK WALL b= 250/2=/25 mm : a= b-t=/25-18=107 mm $\sigma_{MAX} = \frac{\rho(b^2 + 2a^3)}{2(b^3 - a^3)} = \frac{(01.0 \text{ M/a})(125^3 + 2(100)^2)}{2(125^3 - 100^2)} = \frac{2/2 \text{ M/a}}{2(2000^2)} = \frac{2}{2} \frac{1}{2} \frac{1}{$ OZMAN = - P = - 70.0 MPON RADIAL 12-12 Do = 0.840 in ; Di = 0.622; Don=(Do+02)/2=0.731; Don/2=0.701=6.71 b=00/2=0.420in ja=02/2=0.3/1 in $\sigma_{z} = \frac{p a^{2}}{b^{2} - a^{2}} = \frac{(250 \text{ psi})(0.311)^{2}}{(0.420)^{2} - (0.311)^{2}} = \frac{303 \text{ psi} \text{ Longityonal}}{(0.420)^{2} - (0.311)^{2}}$ $O_{1} = \frac{\mu(b^{2}+a^{2})}{b^{2}-a^{2}} \frac{(250 \text{ psi})(6.920^{2}+0.311^{2})}{4.920^{2}-4.921^{2}} = 857 \text{ psi} \text{ Hoop}$ Oi =-p= -250 psi RADIAL

$$\frac{D_{m}}{k} = \frac{(300+320)/2}{(300-320)/2} = 6.5 \quad (THCK) = 110 \text{ mm}; b = 150 \text{ mm}$$

$$O_{1} = \frac{\mu a^{2} (b^{2} + h^{2})}{h^{2} (b^{2} - a^{2})} = \frac{b^{2} + h^{2}}{h^{2} h^{2} - a^{2}} = \frac{b^{2} + h^{2}}{h^{2} (50 \text{ Mb}) (10)^{2}} = 58.17 \frac{b^{2} + h^{2}}{h^{2}}$$

$$\frac{h}{h^{2} (b^{2} - a^{2})} = \frac{b^{2} + h^{2}}{h^{2} h^{2} - a^{2}} = \frac{b^{2} + h^{2}}{h^{2} (50 \text{ Mb}) (10)^{2}} = 58.17 \frac{b^{2} + h^{2}}{h^{2}}$$

$$\frac{h}{h^{2} (b^{2} - a^{2})} = \frac{b^{2} + h^{2}}{h^{2} h^{2} - a^{2}} = \frac{b^{2} + h^{2}}{h^{2} (50 \text{ Mb}) (10)^{2}} = 58.17 \frac{b^{2} + h^{2}}{h^{2}}$$

$$\frac{h}{h^{2} (b^{2} + h^{2})} = \frac{b^{2} + h^{2}}{h^{2} h^{2} - a^{2}} = \frac{b^{2} + h^{2}}{h^{2} (50 \text{ Mb}) (10)^{2}} = 58.17 \frac{b^{2} + h^{2}}{h^{2}}$$

$$\frac{h}{h^{2} (b^{2} + h^{2})} = \frac{b^{2} + h^{2}}{h^{2} - a^{2}} = \frac{b^{2} + h^{2}}{h^{2} (50 \text{ Mb}) (10)^{2}} = 58.17 \frac{b^{2} + h^{2}}{h^{2}}$$

$$\frac{h}{h^{2} (b^{2} - a^{2})} = \frac{h^{2} + h^{2}}{h^{2} - a^{2}} = \frac{b^{2} + h^{2}}{h^{2} (50 \text{ Mb}) (10)^{2}} = 58.17 \frac{b^{2} + h^{2}}{h^{2}}$$

$$\frac{h}{h^{2} (b^{2} - a^{2})} = \frac{h^{2} + h^{2}}{h^{2} - a^{2}} = \frac{b^{2} + h^{2}}{h^{2} - h^{2}} = \frac{b^{2} + h^{2}}{h^{2}} = \frac{b^{2} + h^{2}}{h^{2} - h^{2}} = \frac{b^{2} + h^{2}}{h^{2} - h^{2}} = \frac{b^{2} + h^{2}}{h^{2}} = \frac{b^{2} + h^$$

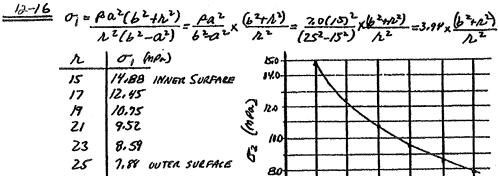
$$D_m = (p_0 + p_{\lambda})/2 = (l \cdot 900 + l \cdot 610)/2 = l \cdot 755$$
 $D_m/x = l \cdot 755/0. PMS = l \cdot 1755/0. PMS =$

USING THIN-WALLED EQN.

$$\sigma_{i} = \frac{pD}{2t} = \frac{(0.0MPa)(1.755mm)}{2(0.145mm)} = 60.5MPa$$

$$\frac{12.45}{D_{m} = (D_{0} + D_{1})/2 = (50 + 30)/2 = 40 \text{ mm} : t = (D_{0} - D_{1})/2 = (50 - 30)/2 = 10 \text{ mm}}$$

$$\frac{D_{m}/t = \frac{40}{10} = 4.0 - TH/CK : b = D_{0}/2 = 25 \text{ mm} : a = D_{1}/2 = 30/2 = 15 \text{ mm}}{0.0000 + 10000 = 100000 = 100000 = 100000 = 100000 = 100000 = 100000 = 10000 = 100000 = 100000 = 100000 = 100000 = 1000000$$



70:

RADIUS (mm)

$$\frac{D-17}{h^{2}(\delta^{2}-\Delta^{2})} = \frac{-\rho \alpha^{2}}{b^{2}a^{2}} \times \frac{b^{2}-h^{2}}{h^{2}} = \frac{-h0l(5^{2})}{h^{2}} \times \frac{b^{2}-h^{2}}{h^{2}} = \frac{399}{h^{2}} \frac{b^{2}-h^{2}}{h^{2}}$$

$$\frac{h}{h^{2}(\delta^{2}-\alpha^{2})} = \frac{-\rho \alpha^{2}}{b^{2}a^{2}} \times \frac{b^{2}-h^{2}}{h^{2}} = \frac{399}{h^{2}} \frac{b^{2}-h^{2}}{h^{2}}$$

$$\frac{h}{h^{2}} = \frac{1}{4} \frac{1}{4} \frac{1}{4} \times \frac{1}{4} \times \frac{1}{4} \frac{1}{4} \times \frac{1}{$$

OUTER SURFACE

$$\frac{12-21}{\sigma_{3}^{2}} = \frac{-\rho \alpha^{3} (b^{3}-h^{3})}{n^{3} (b^{3}-h^{3})} = \frac{-\rho \alpha^{3}}{n^{3} (b^{3}-h^{3})} = \frac{-\rho \alpha^{3}}{n$$

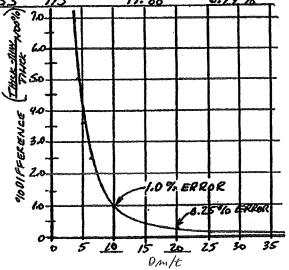
				64.	RADJUS (mm)	
12-22	Do= 400 mm		THIN		THICK OF P(64A)	- Diversity
(mm)	Dm=Do-t	Day't	07 = PD-41	$a = \frac{D_0 - 2t}{2}$	62-a2)	% = THICE-THIN THICE ** 100%
5	395	79	395 MPa	195	395,06 MB	0.015%
15	385	25.61	1283	185	128,53	0.179 %
19.05	380.95	20.0	100.0	180.95	100.25	0.25%
25	375	15.0	75.0	175	75,33	0.44%
35	365	10.43	52.14	165	52.62	0.91%
36.36	363.63	10.0	50.0	163.63	50,50	0.99%
.45	355	7.89	39.44	. 155	40.08	1.60%
55	345	6.27	3/.36	145	32./6	2.49 %
65	335	5,15	25.71	/35	26.74	3.63%
75	325	4.33	21.67	125	22.82	5.04 %
85	315	3.71	18.53	115	19.88	6.79 %

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220 230

NOTES &

- *Partt=200 ADDED TO SHOW
 THAT ARBITEALY DIVISION
 BETWEEN THICK AND THEN
 WALL CYLINDERS RESULTS
 IN LESS THAN 0.2546 BROR
 FOR THIN-WALLED THEORY.
- FOR Dom /t >10, ERROR IS LESS
 THAN 110%
- ERCOR INCREASES RAPIDLY FOR Dale < 10.



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PROBLEMS 12-26 TO 12-35:

These problems are design problems so there may be more than one possible acceptable result. The approach taken in the following spreadsheets is to maintain the inner radius, a, at the stated minimum in the problem and then to adjust the outside radius, b, so that the maximum stress achieves the desired design factor. Attention was paid to whether the resulting design produced a thin-walled or thick-walled vessel. The spreadsheets are similar to that shown in Figure 12-7 in the text, augmented to enable the computation of the design stress and the volume of material in the cylinder or sphere. Both cylinders and spheres can be analyzed with the spreadsheet and the unused part of the sheet has been crossed out, leaving only the desired data.

Problems 12-26 through 12-30 call for a design stress of $s_n/8$ as the primary parameter. Secondarily, they call for computing the design factor based on yield strength if the maximum pressure was double the original design pressure. This approach reflects that the design pressure may be experienced many thousands of times in the life of the vessel and that fatigue of the material may be a failure mode. The higher pressure is considered a burst pressure test pressure that will be experienced only once or a few times in the life of the vessel.

PROBLEMS 12-26 TO 12-28 and 12-30:

These problems have the same design objectives with regard to the operating pressure and the length and inside diameter of a cylindrical pressure vessel. The material for the vessel is different for each problem. Following the given solution for Problem 12-30, a summary of the results for all four problems is given, comparing the wall thickness, volume of material in the cylinder, and the weight or of the cylindrical portion, not counting any end pieces or closures. This should give the student and the reader a feel for how material selection affects the final product design.

STRESSES IN THIC	K-WALLED	CYLINDERS AND SP	HERES		
Data Required Pressure = $p = 1$ Inside radius = $a = R_1 = 1$ Outside radius = $b = R_0 = 1$	450 psi	Problem Number: Wall thickness = t = Mean diameter = D_m = Ratio: D_m/t = If Ratio < 20, Vesse	0.25 in 6.25 in 25.0 Thin		
Analysis of a Sph	ere			Thin-wa	ll sphere
Max Tangential Stress =	•			2812.5	psi
- Max Radial Stress =	450 рsi -				
Analysis of a Cylii	nder			Thin-wal	cylinder
Max Tangential Stress =	5634 psi	Volume of cylinder =	73.63 in ³	5625	psi
Max Longitudinal Stress =	2592 psi	Weight of cylinder =	7.363 lb	2812.5	psi
Max Radial Stress =	-450 psi	[Alum: 0.10 lb/in ³]			
Ultimate strength =	45000 psi		Thin-walled		
Su/8 =	5625 psi	Actual N for su =	8.00		
Yield strength =	40000 psi				
Sy/4 =	10000 psi		7.11		
		N for <i>p</i> = 900 psi =	3.556		

STRESSES IN THICK-WALLED	CYLINDERS AND SPHERES	
Data Required: Pressure = p = 450 psi Inside radius = a = R_i = 3.000 in	Problem Number: 12-27 Wall thickness = $t = 0.065$ in Mean diameter = $D_m = 6.065$ in	
Outside radius = $b = R_o = 3.065$ in	Ratio: $D_m/t = 93.3$ Thin If Ratio < 20, Vessel is thick	
- Analysis of a Sphere - Max Tangential Stress = 10388 psi - Max Radial Stress = 450 psi		Thin-wall sphere
Analysis of a Cylinder		Thin-wall cylinder
Max Tangential Stress = 20997 psi Max Longitudinal Stress = 10273 psi Max Radial Stress = -450 psi	Volume of cylinder = 18.58 in ³ Weight of cylinder = 2.972 lb [Titanium: 0.16 lb/in ³]	20994 psi 10497 psi
Ultimate strength = 170000 psi Su/8 = 21250 psi Yield strength = 155000 psi	Thin-walled Actual N for su = 8.10	
Sy/4 = 38750 psi	Actual N for sy = 7.38 N for <i>p</i> = 900 psi = 3.691	

STRESSES IN THICK-WALLED	CYLINDERS AND SPHERES	• J
Data Required: Pressure = $p = 450$ psi Inside radius = $a = R_i = 3.000$ in	Problem Number: 12-28 Wall thickness = $t = 0.052$ in Mean diameter = $D_m = 6.052$ in	
Outside radius = $b = R_o = 3.052$ in	Ratio: $D_m/t = 116.4$ Thin	
	If Ratio < 20, Vessel is thick	
Analysis of a Sphere		Thin-wall sphere-
Max Tangential Stress = 12983 psi Max Radial Stress = 450 psi		13093 psi ⊸
Analysis of a Cylinder		
Analysis of a Cylinder		Thin-wall cylinder
Max Tangential Stress = 26188 psi	Volume of cylinder = 14.83 in ³	26187 psi
Max Longitudinal Stress = 12869 psi	Weight of cylinder = 4.167 lb	13093 psi
Max Radial Stress = -450 psi	[St. Stl.: 0.281 lb/in ³]	
Ultimate strength = 210000 psi	Thin-walled	
Su/8 = 26250 psi	Actual N for su = 8.02	
Yield strength = 185000 psi		
Sy/4 = 46250 psi	Actual N for sy = 7.06	
	N for $p = 900 \text{ psi} = 3.532$	

STRESSES IN THIC	K-WALLED	CYLINDERS AND SP	HERES	
Data Required Pressure = $p = 1$ Inside radius = $a = R_i = 1$ Outside radius = $a = 1$: 450 psi 3.000 in	Problem Number: Wall thickness = t = Mean diameter = D_m = Ratio: D_m/t = If Ratio < 20, Vesse	12-30 0.039 in 6.039 in 154.5 Thin	
- Analysis of a Sph - Max Tangential Stress - - Max Radial Stress -				Thin-wall sphere
Analysis of a Cylir	nder	Graphite/Epoxy cor	nposite	Thin-wall cylinder
Max Tangential Stress = Max Longitudinal Stress = Max Radial Stress =	17152 psi	Volume of cylinder = Weight of cylinder = [Composite: 0.057 lb/in ³]	11.13 in ³	34752 psi 17376 psi
il no	278000 psi 34750 psi 185000 psi	Actual N for su =	Thin-walled 8.00	
Sy/4 =	46250 psi	Actual N for su = N for $p = 900$ psi =	8.00 4	

	SUMMARY OF RESULTS OF PROBLEMS 12-26 - 12-28 AND 12-30				
Prob. No.	Material	Wall thickness	Weight	Ratio of weights based on composite design	
12-26	Aluminum 6061-T6	0.250 in	7.363 lb	11 61	
	Titanium Ti-6Al-4V	0.065 in	2.972 lb	4.69	
	Stainless steel 17-4PH H900	0.052 in	4.167 lb	6.57	
12-30	Graphite/epoxy composite	0.039 in	0.634 lb	1.00	

PROBLEMS 12-31 TO 12-33:

These problems have the same design objectives with regard to the operating pressure, design factor, and inside diameter of a spherical pressure vessel. The material for the vessel is different for each problem. Following the given solution for Problem 12-33, a summary of the results for all three problems is given, comparing the wall thickness, volume of material in the sphere, and the weight or of the sphere. This should give the student and the reader a feel for how material selection affects the final product design.

STRESSES IN THIC	K-WALLED	CYLINDERS AND SP	HERES	
Data Required Pressure = p = Inside radius = a = R _i = Outside radius = b = R _o =	3000 psi 9.000 in	Problem Number: Wall thickness = t = Mean diameter = D_m = Ratio: D_m/t =	0.475 in 18.48 in	
		If Ratio < 20, Vesse	I	c
Analysis of a Sph	iere	AISI 501 OQT 1000 St. S	steel	Thin-wall sphere
Max Tangential Stress =		Volume of sphere =	509.5 in ³	29171 psi
Max Radial Stress =	-3000 psi	Weight of sphere =	142.6 lb	
		St. Steel density =	0.280 lb/in ³	
-Analysis of a Cylii	nder⊸			Thin-wall-cylinder
		- Volume of cylinder = -Weight of cylinder = -[St. Steel: 0.280 lb/in³]-		58342 psi -29171 psi
Su/6 = [175000 psi 29167 psi 135000 psi	Actual N for su =	Thin-walled 6.00	
Sy/4 =	33750 psi	Actual N for sy = N for <i>p</i> = 6000 psi =	4.63 2.314	· .

STRESSES IN THIC	K-WALLED	CYLINDERS AND SP	HERES	
Data Required Pressure = p = Inside radius = a = R ₁ =	3000 psi	Problem Number: Wall thickness = t = Mean diameter = D _m =	0.984 in	
Outside radius = b = R _o =	9.9840 in	Ratio: <i>D_m/t</i> = If Ratio < 20, Vesse		
Analysis of a Sph	ere	Aluminum 7075-T6		Thin-wall sphere
Max Tangential Stress =	13823 psi	Volume of sphere =	1115 in ³	14470 psi
Max Radial Stress =	-3000 psi	Weight of sphere =	111.5 lb	
		Aluminum density =	0.100 lb/in ³	
Analysis of a Cylir	ider			Thin-wall cylinder
Max Tangential Stress = -Max Lengitudinal Stress = Max Radial Stress =	29017 psi⊸ 13008 psi⊸ 3000 psi	Volume of cylinder — Weight of cylinder —		-28939-psi 14470-psi
Ultimate strength = Su/6 = Yield strength =	83000 psi 13833 psi 73000 psi	Actual N for su =	Thick-walled 6.00	
Sy/4 =	18250 psi	Actual N for sy = N for $p = 6000$ psi =	5.28 2.641	

STRESSES IN THICK-WALLE	CYLINDERS AND SPHERES	
Data Required: Pressure = $p = 3000$ psi Inside radius = $a = R_1 = 9.000$ in	Problem Number: 12-33 Wall thickness = $t = 0.49$ in Mean diameter = $D_m = 18.49$ in	
Outside radius = $b = R_o = 9.4900$ in	Ratio: $D_m/t = 37.7$ Thin	
	· If Ratio < 20, Vessel is thick	
Analysis of a Sphere	Ti-6Al-4V Titanium	Thin-wall sphere
Max Tangential Stress = 27604 psi	Volume of sphere = 526.4 in ³	28301 psi
Max Radial Stress = -3000 psi	Weight of sphere = 84.23 lb	
	Titanium density = 0.160 lb/in ³	
Analysis of a Cylinder		Thin-wall cylinder
-Max Tangential Stress = 56642 psi	Volume of cylinder = 426.9 in ³	-56602 psi
Max Longitudinal Stress = 26821 psi	Weight of cylinder = 68.31 lb	-28301 psi
Max Radial Stress = 3000 psi	Titanium density = 0.160 lb/in ³	
Ultimate strength = 170000 psi	Thin-walled	
Su/6 = 28333 psi	Actual N for su = 6.01	
Yield strength = 155000 psi		
Sy/4 = 38750 psi	Actual N for sy = 5.48	
	N for $p = 6000 \text{ psi} = 2.738$	

PROBLEMS 12-26 TO 12-33: Summary of Results

	SUMMARY OF RESULTS OF PROBLEMS 12-31 - 12-33				
Prob.	Material	Wall	Weight	Ratio of weights based	
No.		thickness		on titanium design	
1	AISI 501 OQT 1000 St. Steel	0.475 in	142.6 lb	1.69	
12-32	Aluminum 7075-T6	0.984 in	111.5 lb	1.32	
12-33	Titanium Ti-6Al-4V	0.490 in	84.23	1.00	

LED CYLINDERS AND SPHERES	
Problem Number: 12-34 Wall thickness = t = 25.9 mm Mean diameter = D_m = 475.9 mm Ratio: D_m/t = 18.4 Thick	
If Ratio < 20, Vessel is thick	
Aluminum 6061-T6	-Thin-wall sphere
a Volume of sphere = 0.018446 m³- a Mass of sphere = 51.10 kg	-19.29 MPa-
Aluminum density = 2770 kg/m ³	Thin-wall cylinder
a Volume of cylinder = 0.023234 m³ a Weight of cylinder = 64.36 kg a Aluminum density = 2770 kg/m³	38.59 MPa 19.29 MPa
a Actual N for su = 8.01 a Actual N for sy = 7.13	
	Wall thickness = t = 25.9 mm Mean diameter = D_m = 475.9 mm Ratio: D_m/t = 18.4 Thick If Ratio < 20, Vessel is thick Aluminum 6061-T6 Volume of sphere = 0.018446 m ³ Mass of sphere = 51.10 kg Aluminum density = 2770 kg/m ³ Length of cylinder = 600 mm Volume of cylinder = 0.023234 m ³ Weight of cylinder = 64.36 kg Aluminum density = 2770 kg/m ³ Actual N for su = 8.01

STRESSES IN THIC	K-WALLED	CYLINDERS AND SF	PHERES	
Data Required Pressure = p = Inside radius = a = R _i =	300 psi	Problem Number: Wall thickness = t = Mean diameter = D _m =	0.301 in	
Outside radius = b = R _o =	12.301 in	Ratio: $D_m/t =$	80.7 Thin	
		If Ratio < 20, Vesse	el is thick	
-Analysis of a Spl	iere-	AISI 1040 CD Steel		Thin-wall-sphere
Max Tangential Stress =	—5983-psi-	-Volume of sphere =	-558.5 in ³	-6055.1 psi-
-Max Radial Stress =	300 psi	-Weight of sphere =-	- 158 lb-	CONTRACTOR
		Steel density =	0.283 lb/in ³	
Analysis of a Cyli	nder	Length of cylinder =	30 in3	Thin-wall cylinder
Max Tangential Stress = Max Longitudinal Stress =	12112 psi 5906 psi	Volume of cylinder = Weight of cylinder =	689.4 in ³ 195.1 lb	12110 psi 6055.1 psi
Max Radial Stress =	-300 psi	Steel density =	0.283 lb/in ³	
	12125 psi	Actual N for su =	Thin 8.01	
Yield strength = Sy/4 =	82000 psi 20500 psi	Actual N for sy = N for $p = 600$ psi =		·

CHAPTER 13 Connections

13-10) FIG. P13-160; 2 14-IN CARBONSTEEL RIVETS; A36 STER! Sy= 36 KSi, SM = SBKSi RIVET CAPACITY: 700LB/RIVETXZRIVETS=1400LB(SHEAR) BEARING ON A36: Oba= 1.28 = 1.2(58)=69.6Ks1 F6= 06 a. A6= (89 60018/1N2)(2) DE= 69 600(2)(0.25)(0.375) LB Fb=13 050 LB TENSIBN : Fta = Ota At OFA = 0.605y = 0.60(36000) = 21600Psi At=[w-Z(D)]t=[3.00-2(0,25)]0.375=0.9375/N2 Fra = (21660LB/IN2) (0.9375112) = 20250LB LIMITING LOAD = FS = 1400 LB FIG. 13-1 (b): 3 3/16-IN CARBON STEEL RIVETS FROM 13-1(a): Oba=69.6Ksi, Ota=216008si (A365 PEEL) SHEAR! FS = (540LB/IN) (3 RIVETS) = 1620LB LIMIT BEARING: F6 = Oba Ab = 69600LB/102/3)(0.18751/0.325)/N2 Fo= 1468/ LB TENSION: Ft = Ota At = \$1600LB/1N2)(3-3(0.1875)(0.375)IN2 Fe = 19744 LB FIG. 13-1 (c): 2 3/10-IN CARBON STEEL RIVETS; A36 STEEL PLATES FROM 13-1(a): Opa= 69-6KS1, OBA= 21.6KSF; 3/88LATE ISCRINGAL. SHEMI: Fs = & YOLB/RIVET) (ZRIVETS)(2) = 2160LB (POUBLES MEAR) BEARING: F6=O60 A6= 69600LB/13 (2)(0.1875)(0.375) IN2 Fb= 9788LB TENSION: Fta = Ota At= (21600LB/N2) (3-2(6.1875)) (0.375) 1N2 Fta= 2/263LB 13-1(d) SAME AS 13-1(c): FS= 2160LB LIMIT

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13-2(b) FIG. 13-2(b): 6 \$732-IN RIVETS-STAINLESS STEEL, 650LB/RIVET

A151 430 PLATES: 060=108000B; , 06248006 PSi (FROM 13-2(0))

SHEAR! F3 = (650LB/RIVET)(6RIVETS)(2) = 7800LB LIMIT

DOUBLE SHEAR

BEARING: F6=060 A6 = (08000LB/IN-)(6)(0.156)(0.5)IN²

F6=50625LB

TENSIAN: F2 = 060 Ac = (48000LB/IN-)(4-3(0.156))(0.50)IN²

F2 = 84750LB

13-2(C) FIG. 13-2(c): 4 3/16/N RIVETS - STAINLESS STEEL, 930LB/RIVET

AISI 430 PLATES: OBE 108000 PSI; Oto 48000PS; (FROM 13-2(D))

SHEAR: Fo = \$\frac{1}{150\LB}/RIVET\$)(4RIVETS)(2) = \frac{1}{1500\LB} (\$\text{POVBLE SHEAR})

BEARING: Fo = Obo Ab = (08000\LB/IN^2)(4)(0.1875)(0.5) = \frac{4}{15000\LB}

TENSION: \(\frac{1}{15} = Ofo 'At = \frac{1}{18000\LB}/IN^2)(4-2(.1875))(0.5) IN = \frac{8}{1000\LB}

LIMIT = Fo = 7660 LB

13-2(d) FIG. 13-2(d): 2 14 TN RIVETS - STAINLESS STEEL, 1700 LB/RIVET

ALSI 430 PLATES: OBG = 1080 FOLB/INZ; OEL = 4800 LB/NZ; FROM 13-Z(D)

SHEAR: FS = (1700 LB/RIVET)(2 RIVET)(2) = 6800 LB (D OUBLE S/16AD)

BEARING: Fb = OBG: AB = (108060 LB/NZ)(4-2(0,ZS))(0.S)/NZ = 189000 LB

LIMIT = 6800 LB = FS

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13 - 3(a)
              FIG. 13-1(9); ASTM A307 STEEL BOLTS-2-14 MOVA.
              PLATES & ASTM A242 HSLA; SY=50KS1, SM=20KSi
                  Oba=1.25 m=1.2(70KS) = 84KS;
Ota=0.65y=0.6(50KSi)=30KS;
               BOLIST TO = 12 KSI (NOTHREADS IN SHEAR PEANE)
             SHEAR: FS=TaAs=(12000LB/1N2/2)(TT)(0.251A)2/4=1178LB
           BEARING: Fb= Oba Ab= (84000LB/1) (2) (0.25)(0.375) 10 - 15750 LB
           TENSION: Ft = OFa: At=BOCOOLG/10-)(3.0-2(0.25+0.063))(0.315)IN2
                     Ft = 2670BLB [HOLE DIA. = D+/16/N]
                LIMIT = F5 = 1178 LB
13-3(b) FIG. 13-1(b): 3 3/16/N BOLTS -SEE PROB. 13-3(0) FOR DATA.
          SHEAR: F5= Ta: As = (2000LB/12) (3) (T(0.1815) /4) 1N= 994 LB
         BEARING: Fb = 010. Ab -(84000 LB/, N2)(3)(0,1875)(0,375)(N=17719 LB
         TENSISM: F= Teo. A+ = BO COOLG/N2) (3.0-3(0.1828+0.083) (0.375) IN-
                   Ft= 25296LB
              LIMIT = F= 994LB
13-3(c) FIG. 13-1(c): 2 3/15-18 BOLTS - DOUBLESHEAR - SEE PROP. 13-3(a)
       SHEAR: F= Ta: As = (12000 LB/12)(2)(2)(17(0,1875) 74)/12=1325 LB
      BEARING: F6 = Oba · A6 (8400018/102) (2) (0.1875) (0.375) 112= 11813 LB
       TENSIEW: FE = Ota As = (30000 LB/M2) (3.0-2(0,1875+0.063)) (0.375) M2
             \frac{F_c = 28114LB}{LIMIT = F_s = 1325LB}
13-3(d) FIG. 13-3(d): SAME AS 13-3(c), Fs=1325LB
13-4 (a) FIG. 13-2(a): 4 3/16-INBOLTS, ASTM A325 STEEL, Ta=30KSi
           ASTM ASTY ALLOYSTEEL: SY= 100KS; SW=110KS/
               Oba = 1.25 m = 1.2(110) = 132KS !
OEA = 0.654 = 0.6(100ESi) = 60KS!
          SHEAR: F= TaiAs=(30000 LB/M2)(4)(1100.1875)79)12=3313 LB
        BEARING: F6 = Oba A6 = 632000LB/N2)(4)(0,1875)(0,5)18 = 49 500 LB
        TENSION : FE = OEA · At = (60 000 LE/IN-) (4.0-2(0.187510.063))(0.5)/N-
                   Ft = 1/2485 LB
               LIMIT & ES 23313 LES
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13-4(6) FIG. 13-2(6): 6 932 BOLTS, DOUBLE SHEM, SEEPLOS 13-4(A)
           SMERQ 1 Ps = Ta · As = (30000 LB/1/2)(6)(2)(T(0.150)2/4)/N2
                     F3 = 6903 18
          BEARING: Fb = Oba Ab= (32000 LB/MZ)(6)(0.156)(0.5) 1N2=6/875LB
          TENSION: Fo = Ota At = (60000 LOPAT) (4.0-3(0.156+0.663)) (0.5)/N2
                     F5 = 100 262 LB
                 LIMIT = F= 6903LB
13-4(c) FIG. 13-2(c): 4 3/16-IN BOLTS, DOUBLE SHEAR, SEE PROB. 13-4(c)
            SHEAR! F3 = 12. A5 = (30 000LB/1/2)(4)(2)(9T (0.1875)/4)112= 662716
         BEARING! Fo = Oba: Ab = (132000 LB/, N)(4)(0.1815)(0.5)1N = 49500 LB
         TENSION: Ft= Ota: At = (60000LB/M2)(4.0-Z(0.1875+0.063))(0.5)M2 =
                     Ft = 104976LB
               LIMIT = Fs = 6627LB
13-4(d) F14. 13-2(d): 2 14-INBOLTS, DOUBLE SHEAR, SEE PROB. 13-4(a)
           SHEAR: F= Ta: As = (30000 LB/(N2) (2)(0)(17(0.25)/4) /N= 5890 LB
          BEARING: F6 = Oba: Ab = (13200018/12)(2)(0,25)(0,50)12=3300018
         TENSIAN: Ft = Ota At = (60 000 LB/INZ) (4.0-2(0.25+0.083) (0.5)/N2=
                    FE=10/220LB
                 LIMITEFS= 5890 LB
13-5 FIG. P13-5 P=6500LB, M=P.40=6500LB/(40/N)=312000LB.IN
        LOADS SHARED BY CONNECTIONS ON TWO SIDES OF COLUMNS
         EACH SIDE: P=3250LB, M=156000LBIN-SIKBOLTS ASTM A325
            RP=3250LB/6=542LB/BOLT +
                                                                   10=30KSi
          E(x2+M2) = 6(2.0)2+4(2.5)2=491N2
         FOR OPPER RIGHT BOLT;

R_{IX} = \frac{M M_{II}}{\Sigma(X^2 + m_I^2)} = \frac{(156000 LB \cdot IN)(Z_{ISIN})}{49 IN^2} = 7959 LB
R_{IY} = \frac{M \pi_{I}}{S(X^2 + Y^2)} = \frac{(156000 (Z_{IS}))}{49} = 6367 LB A
R_{RI} = \sqrt{(7959^2 + (542 + 6367)^2)} = 10206 LB
          REO'D. A = RRI /Ta = 10206LB/30000LB/M2 = 0,340/N2 = TTD'/4
                  DMIN = 14A/AT = 14CO.390INT = 0.65BIN
SPECIFY 3/4IN = 0.750IN BOLTS
          CHECK BEARING ON 3/8 IN A36 STEEL PLATE: Su=58KSI
               Oba=1.25=1.2(58000)=69600 LB/182
               Ob= Fb = 10206 LB = 36288 LB 6 Oba OK
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POSSIBLE SOLUTION -Px = 2011-30= 13.0 EN 100mm Py=Pcm30= 22.5 kN M=(23)(85)=9125 kN.mm7 100mm 12-ASTM A325 BOLTS -Ta=30.0 KSi = 201 MPa ON BOLT (D) Pr = 13.0 km = 1.083 kN -PY = 22.5 km = 1.875 km \$ FORCES DUE TO MOMENT E(12+12) = 6(50)2+6(100)2+8(100)2= 155000mm2 RIX= MAY = 19125 RN-mm (100 mm) = 12.34 RN -RIV = MXi = 19/25 Nomm (10mm) = 12.34kN } R, = (1.083 + 12.34)2 + (1.875 +12.34)2) 12= 19.55 kN REO'D. A = R1 = 19550N = 94.4 mm² = Tro/4

Dmin = 14A = 14(94.4 mm² = 10.96 mm SPECIFY MIZ BOLT, D=12.0 mm

F16, P13-1 (W) P= Ta, Lt = (8000 a/i2) (6.in) (0.701) (0.3125i) =23360 (b-cs) ON STRAPS P = 162 (3)(4))=(0.6)(36000R/22)(32 X0.3752)-24 300R WELDS GOVERN JOINT STRENGTH

F16. P13-2(c) 13-0 P=Talt=(2/000 B/x2)(Bis)(0.707)(0.250in)=29700 llay uses. ON STRAPS @=6.6/50000 M/i2) (0.5in)(4in)=60000 De

THE SOLUTIONS SHOWN BELOW FOR PROBLEMS 13-9, 13-10, AND 13-11 ARE JUST SAMPLES OF MANY POSSIBLE SOLUTIONS. THE GENERAL CONFIGURATION AND NUMBER OF FASTENERS SHOWN IN FIG. 13-1 ARE USED, BUT OTHERS COULD BEUSED.

TOTAL LUAD = 15.0Mg = (15.0X/0 pg) (9.81 m/sz) = 147.150 N 4SUPPERTS: LOAD/SUPPORT = 147150/4=36788N DOUBLE SHEAR USE 6 RIVETS AS SHOWN. FS = 36 788N/(2)(6) = 3066N SPECIFY 6.35 mm (14-IN) CARBONSTEEL RIVETS, 3114 N CAPY,

CHECK BEARING ON WEB OFTEE, t=10.6 mm, A36 STEEL

5y=248 MPa, Sn=400MPa; Oba=1,25n=1,2(400)=480MPa

06= F = 2(3066N) = 91.1 N/mm²=91.1 MPa 4980MPa

06=06=06.35)(10.6) mm²=06

DEFERMINE THICKNESS OF STRAPS (2)

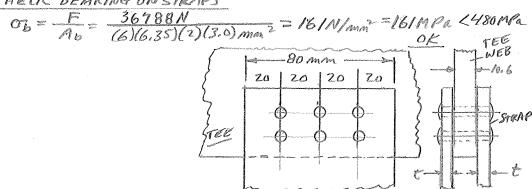
TENSION: OF = 0.6 Sy=0.6 (ZY8MPA)=148.8 MPA

FE = Ota: At; At= (W-30)2t= [80-3(6.35)](2)t=121.9t

3678BN=(48.8 N/mm2)(121.9t)=18139t

TMIN = 367891/18/39 = 2.03 mm SPECIFY t= 3,0 mm

CHECK BEARING ON STRAPS



13-10 SEE FIG. 13-1. FORCE ON JOINT = 36780 N (PROS 13-9) USE 2 BOLTS, DOUBLE SHEAR, ASTM A325, Ta=ZOTMPE $T = \frac{F_{s}}{A_{s}} \stackrel{?}{.} A_{s} = \frac{F_{s}}{T_{o}} = \frac{36789N}{207N/mm^{2}} = 177.7 mm^{2} TOTAL$ $A_{BOLT} = \frac{A_{s}}{(280LIS)(2)} = 44.43 m m^{2} = 77 p_{y}^{2}$ L DOUBLE SHERRDMIN = \frac{14A}{17} = \frac{14(44.43)}{17} = 7.52 mm; SPECIFY MB BOLTS
B = 8.0 mm CHECK TENSION ON STRAPS OF a = 148,8 MPa (PROB 13-9) Ot = F/At 3 At = (80-2(8)(2)(3) = (w-2D)(2)(t)=384mm2 07 = 36788 N = 95.8MPa < 148.8MPa - OK CHECK BEARING ON STRAPS OBE = 480MPa (PROB. 13-9) 06 = F = 36788N (2)(8)(2)(3)mm2 = 383MPa 4060-0K STRAP SEEFIG. 13+1. WELDED JOINT FORCE ON JOINT = 36788N (PROB 13-9) s-80 ASTM A36 STEEL - E 60 ELECTRODE a-10 mm WELDS -10= 124 MPa 1 = F = 36288N TAB ASTMA36 L=2a; t=0.787 w W=WELDLEGSIZE=5.0mm (SPECIFIED) t=0.701(5)=3,535 nom REO'D L= F/Pat-36788N (124 Nyma) (3.535 mm) Lmw = 83.93 mm = 20 amn = 83.93/2 = 41.96 mm

SPECIFY a= 45 mm